Sustainable Energy– without the hot air

David J.C. MacKay

Draft 2.9.0 - August 28, 2008

Department of Physics University of Cambridge

http://www.withouthotair.com/

Back-cover blurb

Sustainable energy — without the hot air

Category: Science.

How can we replace fossil fuels? How can we ensure security of energy supply? How can we solve climate change?

We're often told that "huge amounts of renewable power are available" – wind, wave, tide, and so forth. But our current power *consumption* is also huge! To understand our sustainable energy crisis, we need to know how the one "huge" compares with the other. We need numbers, not adjectives.

In this book, David MacKay, Professor in Physics at Cambridge University, shows how to estimate the numbers, and what those numbers depend on. As a case study, the presentation focuses on the United Kingdom, asking first "could Britain live on sustainable energy resources alone?" and second "how can Britain make a realistic post-fossil-fuel energy plan that adds up?"

These numbers bring home the size of the changes that society must undergo if sustainable living is to be achieved.

Don't be afraid of this book's emphasis on numbers. It's all basic stuff, accessible to high school students, policy-makers and the thinking public. To have a meaningful discussion about sustainable energy, we need numbers.

This is **Draft 2.9.0** (August 28, 2008). You are looking at the low-resolution edition (i.e., some images are low-resolution to save bandwidth). Feedback welcome. Thanks!

What's this book about?

I'm concerned about cutting UK emissions of twaddle – twaddle about sustainable energy. Everyone says getting off fossil fuels is important, and we're all encouraged to 'make a difference', but many of the things that allegedly make a difference don't add up.

Twaddle emissions are high at the moment because people get emotional (for example about wind farms or nuclear power) and no-one talks about numbers. Or if they do mention numbers, they select them to sound big, to make an impression, and to score points in arguments, rather than to aid thoughtful discussion.

This is a straight-talking book about the numbers. The aim is to guide the reader around the claptrap to actions that really make a difference and to policies that add up.





The author, July 2008. Photo by David Stern.

How to operate this book

Some chapters begin with a quotation. Please don't assume that my quoting someone means that I agree with them. Think of these quotes as provocations, as hypotheses to be critically assessed.

Many of the early chapters (numbered 1, 2, 3, ...) have longer technical chapters (A, B, C, ...) associated with them. These technical chapters start on page 272.

At the end of each chapter are further notes and pointers to sources and references. I find footnote marks distracting if they litter the main text of the book, so the book has no footnote marks. If you love footnote marks, feel free to add them – almost every substantive assertion in the text will have an associated endnote giving sources or further information.

The text also contains pointers to web resources. When a web-pointer is monstrously long, I've used the TinyURL service, and put the tiny code in the text like this – [yh8xse] – and the full pointer at the end of the book on page 389. yh8xse is a shorthand for a tiny URL, in this case: http://tinyurl.com/yh8xse.

A complete list of all the URLs in this book is provided at http://tinyurl.com/yh8xse.

If you find a URL doesn't work any more, you may be able to find the page on the Wayback Machine internet archive [f754].

An electronic version of this book is available for free on the website www.withouthotair.com.

I welcome feedback and corrections. I am aware that I sometimes make booboos, and in earlier drafts of this book some of my numbers were off by a factor of two. While I hope that the errors that remain are smaller than that, I expect to further update some of the numbers in this book as I continue to learn about sustainable energy.

How to cite this book:

David J. C. MacKay. Sustainable Energy – Without the Hot Air. UIT Cambridge, 2008. ISBN 9780954452933. Available free online from www.withouthotair.com.

This is a free book: you are free to use *all* the material in this book, *except* for the cartoons and the photos with a named photographer, under the Creative Commons Attribution-Non-Commercial-Share Alike 2.0 UK: England & Wales Licence; (The photos are excepted because the photographers have generally given me permission only to include their photo, *not* to share it under a Creative Commons license.) You are especially welcome to use my materials for educational purposes. My website includes separate files for each of the figures in the book. You may use these figures under any of the following Creative Commons licenses: Attribution ShareAlike; Sharealike; Attribution-nocommercial-sharealike. Please don't propagate poor-quality copies of my diagrams when high quality ones are



available. Most of the figures have numbered captions, but sometimes I try to avoid clutter by omitting captions – for example, from maps.

Contents

I	Nu	mbers, not adjectives	1		
	1	Motivations	2		
	2	The balance sheet	23		
	3	Cars	31		
	4	Wind	34		
	5	Planes	37		
	6	Solar	40		
	7	Heating and cooling	54		
	8	Hydroelectricity	59		
	9	Light	61		
	10	Offshore wind	64		
	11	Gadgets	72		
	12	Wave	77		
	13	Food and farming	80		
	14	Tide	85		
	15	Stuff	93		
	16	Geothermal	103		
	17	Public services	107		
	18	Can we live on renewables?	110		
П	Making a difference				
	19	Every BIG helps	122		
	20	Better transport	126		
	21	Smarter heating	148		
	22	Efficient electricity use	165		
	23	Sustainable fossil fuels?	167		
	24	Nuclear?	170		
	25	Living on other countries' renewables?	190		
	26	Fluctuations and storage	201		
	27	Five energy plans for Britain	218		
	28	Putting costs in perspective	230		
	29	What to do now	242		
	30	Energy plans for Europe, America, and the World	258		
	31	The last thing we should talk about	264		

	Ack	knowledgments	269
Ш	Tec	chnical chapters	271
	A	Cars II	272
	В	Wind II	282
	C	Planes II	289
	D	Solar II	302
	E	Heating II	308
	F	Waves II	325
	G	Tide II	330
	Н	Stuff II	344
	I	Storage II	351
	J	Carbon II	353
IV	Useful data		358
	K	Terminology	359
	L	Populations and areas	368
	M	UK energy history	376
	N	Quick reference	378
	List of web links		389
	Bib	liography	394
	Ind	ex	401

Part I Numbers, not adjectives

We live at a time when emotions and feelings count more than truth, and there is a vast ignorance of science.

James Lovelock

I recently read two books, one by a physicist, and one by an economist. In *Out of Gas*, Caltech physicist David Goodstein describes an impending energy crisis brought on by The End of the Age of Oil. This crisis is coming soon, he predicts: the crisis will bite, not when the last drop of oil is extracted, but when oil extraction can't meet demand – perhaps as soon as 2015 or 2025. Moreover, even if we magically switched all our energy-guzzling to nuclear power right away, Goodstein says, the oil crisis would simply be replaced by a *nuclear* crisis in just twenty years or so, as uranium reserves also became depleted.

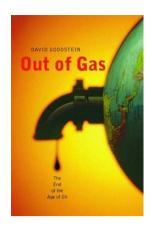
In *The Skeptical Environmentalist*, Bjørn Lomborg paints a completely different picture. "Everything is fine." Indeed, "everything is getting better." Furthermore, "we are not headed for a major energy crisis," and "there is plenty of energy."

How could two smart people come to such different conclusions? I had to get to the bottom of this.

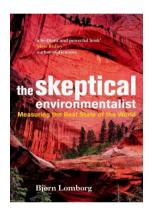
Energy made it into the British news in 2006. Kindled by tidings of great climate change and a tripling in the price of natural gas in just six years, the flames of debate are raging. How should Britain handle its energy needs? And how should the world?

"Wind or nuclear?", for example. Greater polarization of views among smart people is hard to imagine. During a discussion of the proposed expansion of nuclear power, Michael Meacher, former environment minister, said "if we're going to cut greenhouse gases by 60% ... by 2050 there is no other possible way of doing that except through renewables"; Sir Bernard Ingham, former civil servant, speaking in favour of nuclear expansion, said "anybody who is relying upon renewables to fill the [energy] gap is living in an utter dream world and is, in my view, an enemy of the people."

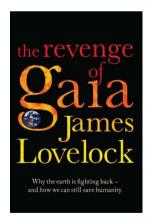
Similar disagreement can be heard within the ecological movement. All agree that *something* must be done urgently, but *what?* Jonathan Porritt, chair of the Sustainable Development Commission, writes: "there is no justification for bringing forward plans for a new nuclear power programme at this time, and ... any such proposal would be incompatible with [the Government's] sustainable development strategy;" and "a non-nuclear strategy could and should be sufficient to deliver all the carbon savings we shall need up to 2050 and beyond, and to ensure secure access to reliable sources of energy." In contrast, James Lovelock, "the founding historical and cultural leader of environmentalism" writes in his book, *The Revenge of Gaia*: "Now is much too late to establish sustainable develop-



David Goodstein's Out of Gas (2004).



Bjørn Lomborg's *The Skeptical Environmentalist* (2001).



The Revenge of Gaia: Why the earth is fighting back – and how we can still save humanity.

James Lovelock (2006). © Allen Lane.

ment." In his view, power from nuclear fission, while not recommended as the long-term panacea for our ailing planet, is "the only effective medicine we have now." Onshore wind turbines are "merely ... a gesture to prove [our leaders'] environmental credentials."

This heated debate is fundamentally about numbers. How much energy could each source deliver, at what economic and social cost, and with what risks? But actual numbers are rarely mentioned. In public debates, people just say "Nuclear is a money pit" or "We have a *huge* amount of wave and wind." The trouble with this sort of language is that it's not sufficient to know that something is huge: we need to know how the one "huge" compares with another "huge," namely *our huge energy consumption*. To make this comparison, we need numbers, not adjectives.

Where numbers are used, their meaning is often obfuscated by enormity. Numbers are chosen to impress, to score points in arguments, rather than to inform. "Los Angeles residents drive 142 million miles – the distance from Earth to Mars – every single day." "Each year, 27 million acres of tropical rainforest are destroyed." "14 billion pounds of trash are dumped into the sea every year." "British people throw away 2.6 billion slices of bread per year." "The waste paper buried each year in the UK could fill 103 448 double-decker buses."

If all the ineffective ideas for solving the energy crisis were laid end to end, they would reach to the moon and back.... I digress.

The result of this lack of meaningful numbers and facts? We are inundated with a flood of crazy innumerate codswallop. The BBC doles out advice on how we can do our bit to save the planet – for example "switch off your mobile phone charger when it's not in use"; if anyone objects that mobile phone chargers are not *actually* our number one form of energy consumption, the mantra "every little helps" is wheeled out. Every little helps? A more realistic mantra is:

if everyone does a little, we'll achieve only a little.

Companies also contribute to the daily codswallop as they tell us how wonderful they are, or how they can help us "do our bit." BP's website, for example, celebrates the reductions in carbon dioxide (CO₂) pollution they hope to achieve by changing the paint used for painting BP's ships. Does anyone fall for this? Surely everyone will guess that it's not the exterior paint job, it's the stuff *inside* the tanker that deserves attention, if society's CO₂ emissions are to be significantly cut? BP also created a web-based carbon absolution service, "targetneutral.com," which claims that they can "neutralize" all your carbon emissions, and that it "doesn't cost the earth" – indeed, that your CO₂ pollution can be cleaned up for just £40 per year. How can this add up? – if the true cost of fixing climate change were £40 per person then the government could fix it with the loose change in the Chancellor's pocket!

Even more reprehensible are companies that exploit the current concern for the environment by offering "water-powered batteries," "recyclable mobile phones," "environment-friendly phone calls," and other pointless tat.

Campaigners also mislead. People who want to promote renewables over nuclear, for example, say "offshore wind power could power all UK homes;" then they say "new nuclear power stations will do little to tackle climate change" because 10 new nuclear stations would "reduce emissions only by about 4%." This argument is misleading because the playing field is switched half-way through, from the "number of homes powered" to "reduction of emissions". The truth is that the amount of electrical power generated by the wonderful windmills that "could power all UK homes" is exactly the same as the amount that would be generated by the 10 pathetic nuclear power stations that would "reduce emissions only by about 4%"!

Perhaps the worst offenders in the kingdom of codswallop are the people who really should know better – the media publishers who promote the codswallop – for example, New Scientist with their article about the "water-powered car".*

In a climate where people don't understand the numbers, newspapers, campaigners, companies, and politicians can get away with murder.

We need simple numbers, and we need the numbers to be comprehensible, comparable, and memorable.

With numbers in place, we will be better placed to answer questions such as these:

- 1. Can a country like Britain conceivably live on its own renewable energy sources?
- 2. If everyone turns their thermostats one degree closer to the outside temperature, drives a smaller car, and switches off phone chargers when not in use, will an energy crisis be averted?
- 3. Should the tax on transportation fuels be significantly increased? Should speed-limits on roads be halved?
- 4. Is someone who advocates windmills over nuclear power stations "an enemy of the people"?
- 5. If climate change is "a greater threat than terrorism," should governments criminalize "the glorification of travel" and pass laws against "advocating acts of consumption"?
- 6. Will a switch to "advanced technologies" allow us to eliminate carbon dioxide pollution without changing our lifestyle?
- 7. Should people be encouraged to eat more vegetarian food?
- 8. Is the population of earth six times too big?
- © David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

*See this chapter's notes (p19) for the awful details. Every chapter has endnotes giving references, sources, and details of arguments. To avoid distracting the reader, I won't include any more footnote marks in the text.



Figure 1.1. This Greenpeace leaflet arrived with my junk mail in May 2006. Do beloved windmills have the capacity to displace hated cooling towers?

Why are we discussing energy policy?

Three different motivations drive today's energy discussions.

First, fossil fuels are a finite resource. It seems possible that cheap oil (on which our cars and lorries run) and cheap gas (with which we heat many of our buildings) will run out in our lifetime. So we seek alternative energy sources. Indeed given that fossil fuels are a valuable resource, useful for manufacture of plastics and all sorts of other creative stuff, perhaps we should save them for better uses than simply setting fire to them.

Second, we're interested in security of energy supply. Even if fossil fuels are available somewhere in the world, perhaps we don't want to depend on them if that would make our economy vulnerable to the whims of untrustworthy foreigners. (I hope you can hear my tongue in my cheek.) Going by figure 1.2, it certainly looks as if "our" fossil fuels have peaked. The UK has a particular security-of-supply problem looming, known as the "energy gap." A substantial number of old coal power stations and nuclear power stations will be closing down during the next decade (figure 1.3), so there is a risk that electricity demand will sometimes exceed electricity supply, if adequate plans are not implemented.

Third, it's widely held that using fossil fuels changes the climate. Climate change is blamed on several human activities, but the biggest contributor to climate change is the increase in greenhouse effect produced by carbon dioxide (CO_2). Most of the carbon dioxide emissions come from fossil-fuel burning. And the main reason we burn fossil fuels is for energy. So to fix climate change, we need to sort out a new way of getting energy. The climate problem is essentially an energy problem.

Whichever of these three concerns motivates you, we need energy numbers, and policies that add up.

The first two concerns are straightforward selfish motivations for drastically reducing fossil fuel use. The third concern, climate change, is a more altruistic motivation – the brunt of climate change will be borne not by us but by future generations over many hundreds of years. Some people feel that climate change is not their responsibility. They say things like "What's the point in my doing anything? China's out of control!" So I'm going to discuss climate change a bit more now, because while writing this book I learned some interesting facts that shed light on these ethical questions. If you have no interest in climate change, feel free to fast-forward to the next section on p16.

The climate-change motivation

The climate-change motivation is argued in three steps: one: human fossilfuel burning causes carbon dioxide concentrations to rise; two: carbon dioxide is a greenhouse gas; three: increasing the greenhouse effect increases average global temperatures (and has many other effects).

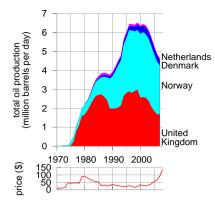


Figure 1.2. Are "our" fossil fuels running out? Total crude oil production from the North Sea, and oil price in 2006 dollars per barrel.

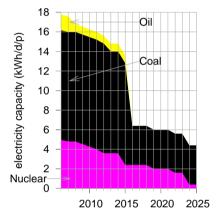


Figure 1.3. The energy gap created by UK power station closures, as projected by energy company EdF. This graph shows the predicted capacity of nuclear, coal, and oil power stations, in kilowatt-hours per day per person. The capacity is the maximum deliverable power of a source.

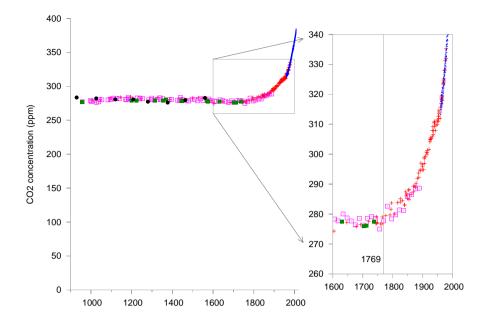


Figure 1.4. Carbon dioxide (CO₂) concentrations (in parts per million) for the last 1100 years, measured from air trapped in ice cores (up to 1977) and directly in Hawaii (from 1958 onwards).

I think something new may have happened between 1800 AD and 2000 AD. I've marked the year 1769, in which James Watt patented his steam engine. (The first practical steam engine was invented seventy years earlier in 1698, but Watt's was much more efficient.)

We start with the fact that carbon dioxide concentrations are rising. Figure 1.4 shows measurements of the CO_2 concentration in the air from the year 1000 AD to the present. Some "sceptics" have asserted that the recent increase in CO_2 concentration is a natural phenomenon. Does "sceptic" mean "a person who has not even glanced at the data"? Don't you think, just possibly, *something* may have happened between 1800 AD and 2000 AD? Something that was not part of the natural processes present in the preceding thousand years?

Something did happen, and it was called the Industrial Revolution. I've marked on the graph the year 1769, in which James Watt patented his steam engine. While the first practical steam engine was invented in 1698, Watt's more efficient steam engine really got the Industrial Revolution going. One of the steam engine's main applications was the pumping of water out of coal mines. Figure 1.5 shows what happened to British coal production from 1769 onwards. In 1800, coal was used to make iron, to make ships, to heat buildings, to power locomotives and other machinery, and of course to power the pumps that enabled still more coal to be scraped up from inside the hills of England and Wales. Britain was terribly well endowed with coal: when the Revolution started, the amount of carbon sitting in coal under Britain was roughly the same as the amount sitting in oil under Saudi Arabia.

In the thirty years from 1769 to 1800, Britain's annual coal production doubled. After another thirty years (1830), it had doubled again. The next doubling of production-rate happened within *twenty* years (1850), and another doubling within twenty years of that (1870). This coal allowed Britain

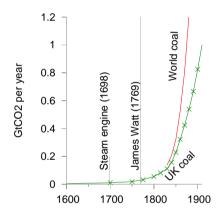
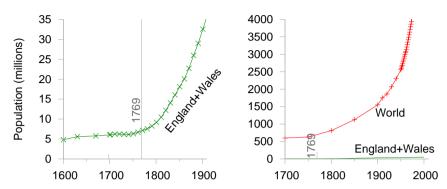
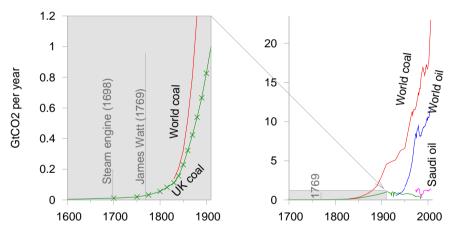


Figure 1.5. The history of UK coal production and world coal production from 1650 to 1910. Production rates are shown in billions of tons of CO_2 – an incomprehensible unit, yes, but don't worry: we'll personalize it shortly.

to turn the globe pink. The prosperity that came to England and Wales was reflected in a century of unprecented population growth.



Eventually other countries got in on the act too as the Revolution spread. Figure 1.6 shows British coal production and world coal production on the same scale as figure 1.5, sliding the window of history fifty years later. British coal production peaked in 1910, but meanwhile world coal production continued to double every twenty years. It's difficult to show the history of coal production on a single graph. To show what happened in the *next* 50 years on the same scale, the book would need to be one metre tall! To cope with this difficulty, we can either scale down the vertical axis:



or we can squish the vertical axis in a non-uniform way, so that small quantities and large quantities can be seen at the same time on a single graph. A good way to squish the axis is called a logarithmic scale, and that's what I've used in the bottom two graphs of figure 1.7 (p8). On a logarithmic scale, all ten-fold increases (from 1 to 10, from 10 to 100, from 100 to 1000) are represented by equal distances on the page. On a logarithmic scale, a quantity that grows at a constant percentage per year looks like a straight line. Logarithmic graphs are great for understanding growth. Whereas the ordinary graphs in figures on pages 6 and 7 convey the messages that

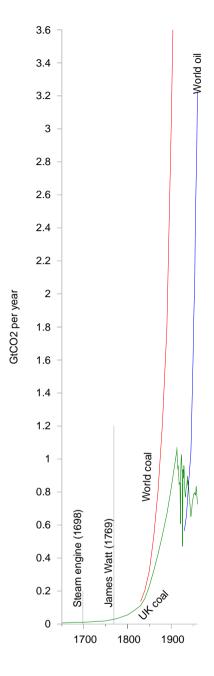


Figure 1.6. What happened next. The history of UK coal production and world coal production from 1650 to 1960, on the same scale as figure 1.5.

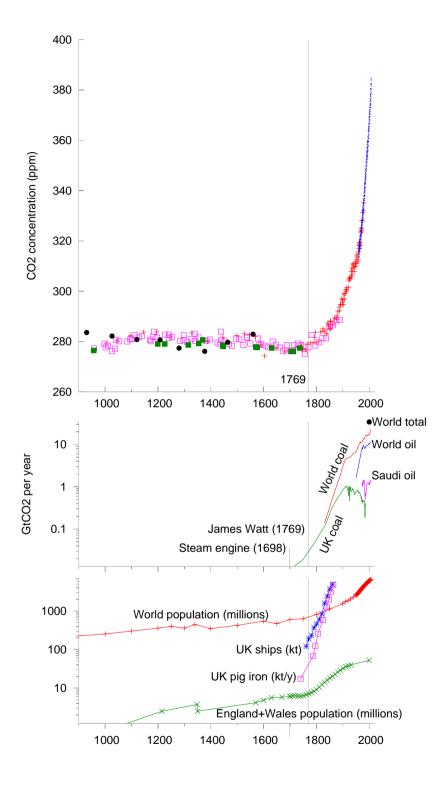


Figure 1.7. The upper graph shows carbon dioxide (CO₂) concentrations (in parts per million) for the last 1100 years, measured from air trapped in ice cores (up to 1977) and directly in Hawaii (from 1958 onwards).

I've marked the year 1769, in which James Watt patented his steam engine. (The first practical steam engine was invented seventy years earlier in 1698, but Watt's was much more efficient.)



The middle graph shows (on a logarithmic scale) the history of UK coal production, Saudi oil production, world coal production, world oil production, and (by the top right point) the total of all greenhouse gas emissions in the year 2000.

The bottom graph shows (on a logarithmic scale) some consequences of the Industrial Revolution: sharp increases in the population of England, and, in due course, the world; and remarkable growth in British pig-iron production (in thousand tons per year); and growth in the tonnage of British ships (in thousand tons).

In contrast to the ordinary graphs on the previous pages, the logarithmic scale allows us to show both the population of England and the population of the World on a single diagram, and to see interesting features in both.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

British and world coal production grew remarkably, and that British and world population grew remarkably, the relative growth rates are not evident in the ordinary graphs. The logarithmic graphs allow us to compare growth rates. Looking at the slopes of the population curves, for example, we can see that the world population's growth rate in the last 50 years was a little bigger than the growth rate of England and Wales in 1800.

From 1769 to 2006, world annual coal production increased 800-fold. Coal production is still increasing today. Other fossil fuels are being extracted too – figure 1.7 shows oil production for example – but in terms of CO_2 emissions, coal is still king.

The burning of fossil fuels is the principal reason why CO_2 concentrations have gone up. This is a fact, but, hang on: I hear a persistent buzzing noise coming from a bunch of climate-change inactivists. What are they saying? Here's Dominic Lawson, a columnist from the *Independent*:

"The burning of fossil fuels sends about seven gigatons of CO_2 per year into the atmosphere, which sounds like a lot. Yet the biosphere and the oceans send about 1900 gigatons and 36 000 gigatons of CO_2 per year into the atmosphere – . . . one reason why some of us are sceptical about the emphasis put on the role of human fuel-burning in the greenhouse gas effect. Reducing man-made CO_2 emissions is megalomania, exaggerating man's significance. Politicians can't change the weather."

Now I have a lot of time for scepticism, and not everything that sceptics say is a crock of manure – but irresponsible journalism like Dominic Lawson's deserves a good flushing.

The first problem with Lawson's offering is that *all three numbers* that he mentions (seven, 1900, and 36 000) are *wrong!* The correct numbers are 26, 440, and 330. Leaving these errors to one side, let's address Lawson's main point, the relative smallness of man-made emissions.

Yes, natural flows of CO₂ are larger than the additional flow we switched on two hundred years ago when we started burning fossil fuels in earnest. But it is terribly misleading to quantify only the large natural flows *into* the atmosphere, failing to mention the almost exactly equal flows *out* of the atmosphere back into the biosphere and the oceans. The point is that these *natural* flows in and out of the atmosphere have been almost exactly in balance for millenia. So it's not relevant at all that these natural flows are larger than human emissions. The natural flows *cancelled themselves out*. So the natural flows, large though they were, left the concentration of CO₂ in the atmosphere and ocean *constant*. Burning fossil fuels, in contrast, creates a *new* flow of carbon that, though small, is *not cancelled*. Here's a simple analogy, set in the passport-control arrivals area of an airport. One thousand passengers arrive per hour, and there are exactly enough clockwork officials to process one thousand passengers per hour. There's a modest queue, but because of the match of arrival rate to service rate,

the queue isn't getting any longer. Now imagine that owing to fog an extra stream of flights is diverted here from a smaller airport. This stream adds an extra fifty passengers per hour to the arrivals lobby – a small addition compared to the original arrival rate of one thousand per hour. Initially at least, the authorities don't increase the number of officials, and the officials carry on processing just one thousand passengers per hour. So what happens? Slowly but surely, the queue grows. Burning fossil fuels is undeniably increasing the CO₂ concentration in the atmosphere and in the surface oceans. No scientist disputes this fact. When it comes to CO₂ concentrations, man *is* significant.

OK. Fossil fuel burning increases CO_2 concentrations significantly. But does it matter? "Carbon is nature!", the oilspinners remind us, "Carbon is life!" If CO_2 had no harmful effects, then indeed carbon emissions would not matter. However, carbon dioxide is a greenhouse gas. Not the strongest greenhouse gas, but a significant one nonetheless. Put more of it in the atmosphere, and it does what greenhouse gases do: it absorbs infrared radiation (heat) heading out from the earth and reemits it in a random direction; the effect of this random redirection of the atmospheric heat traffic is to impede the flow of heat from the planet, just like a duvet. So carbon dioxide has a warming effect. This fact is based not on complex historical records of global temperatures but on the simple physical properties of CO_2 molecules. Greenhouse gases are a duvet, and CO_2 is one layer of the duvet.

So, if humanity succeeds in doubling or tripling CO₂ concentrations (which is where we are certainly heading, under business as usual), what happens? Here, there is a lot of uncertainty. Climate science is difficult. The climate is a complex, twitchy beast, and exactly how much warming CO₂-doubling would produce is uncertain. The consensus of the best climate models seems to be that doubling the CO₂ concentration would have roughly the same effect as increasing the intensity of the sun by 2%, and would bump up the global mean temperature by something like 3 °C. This would be what historians call a Bad Thing. I won't recite the litany of probable drastic effects, as I am sure you've heard it before. The litany begins "the Greenland icecap would gradually melt, and, over a period of a few hundred years, sea-level would rise by about 7 metres." The brunt of the litany falls on future generations. Such temperatures have not been seen on earth for at least 100 thousand years, and it's conceivable that the ecosystem would be so significantly altered that the earth would stop supplying some of the goods and services that we currently take for granted.

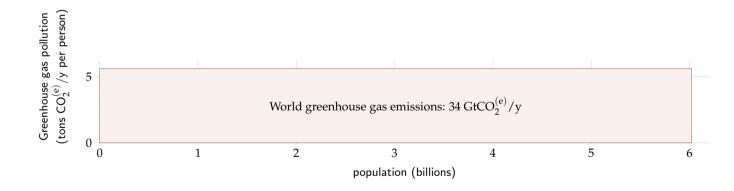
Climate modelling is difficult and is dogged by uncertainties. But uncertainty about exactly how the climate will respond to extra greenhouse gases is no justification for inaction. If you were riding a fast-moving motorcycle in fog near a cliff-edge, and you didn't have a good map of the cliff, would the lack of a map justify *not* slowing the bike down?

So, who should slow the bike down? Who should clean up carbon

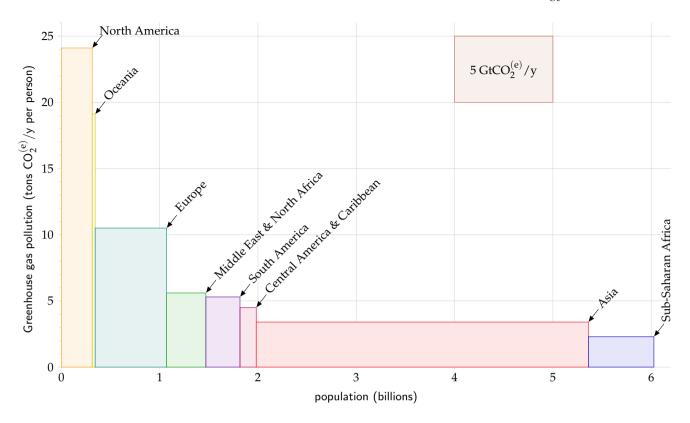
[©] David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

emissions? Who is responsible for climate change? This is an ethical question, of course, not a scientific one, but ethical discussions must be founded on facts. Let's now explore the facts about greenhouse gas emissions. First, a word about the units in which they are measured. Greenhouse gases include carbon dioxide, methane, and nitrous oxide; each gas has different physical properties; it's conventional to express all gas emissions in "equivalent amounts of carbon dioxide", where "equivalent" means "having the same warming effect over a period of 100 years." One ton of carbon-dioxide-equivalent may be abbreviated as " $1 \, {\rm tCO}_2^{(e)}$," and one billion tons (one thousand million tons) as " $1 \, {\rm Gt} \, {\rm CO}_2^{(e)}$ " (one gigaton). In this book 1 t means one metric ton (1000 kg). I'm not going to distinguish imperial "short" and "long" tons, because they differ by less than 10% from the metric ton or tonne.

In the year 2000, world greenhouse gas emissions stood at about 34 billion tons of CO_2 -equivalent per year. An incomprehensible number. But we can render it more comprehensible and more personal by dividing by the number of people on the planet, 6 billion, so as to obtain the greenhouse-gas pollution *per person*, which is $5^{1/2}$ tons $CO_2^{(e)}$ per year per person. We can thus represent the world emissions by a rectangle whose width is the population (6 billion) and whose height is the per-capita emissions.



Now, all people are created equal, but we don't all emit $5^{1/2}$ tons of CO_2 per year. We can break down the emissions of the year 2000, showing how the 34 billion-ton rectangle is shared between the regions of the world.

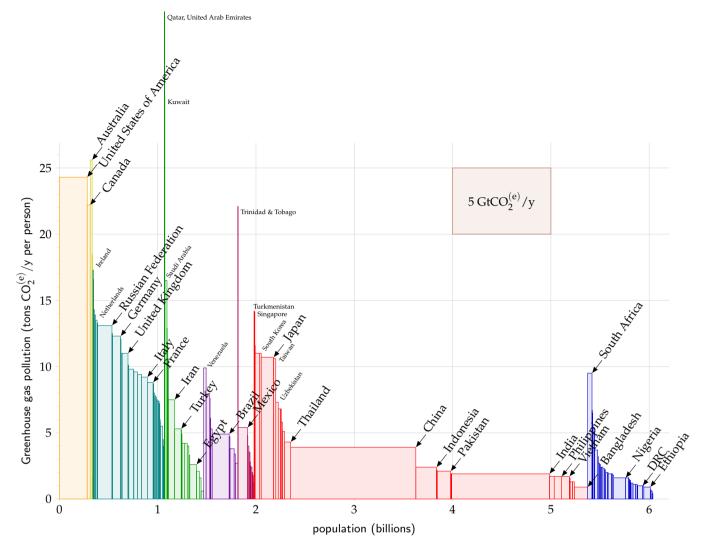


This picture, which is on the same scale as the previous one, divides the world into eight regions. Each rectangle represents the greenhouse gas emissions of one region. The width of the rectangle is the population of the region, and the height is the average per-capita emissions in that region.

In the year 2000, Europe's per-capita greenhouse gas emissions were twice the world average; and North America's were four times the world average.

We can continue subdividing, splitting each of the regions into countries. This is where it gets really interesting.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com



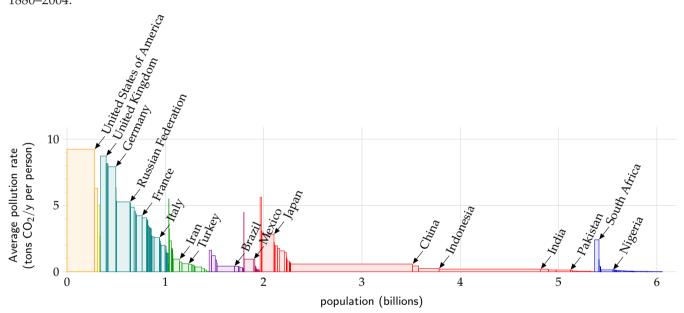
The major countries with the biggest per-capita emissions are Australia, the USA, and Canada. European countries, Japan, and South Africa are notable runners up. Among European countries, the United Kingdom is resolutely average. What about China, that naughty "out of control" country? Yes, the area of China's rectangle is about the same as the USA's, but the fact is that their per-capita emissions are *below* the world average. India's per-capita emissions are less than *half* the world average.

So, assuming that "something needs to be done" about climate change, assuming that the world needs to reduce greenhouse gas emissions, who has a special responsibility to do something? Well, that's an ethical question. But I find it hard to imagine any system of ethics that denies that the responsibility falls especially on the countries to the left hand side of this diagram – the countries whose emissions are two, three, or four times the

world average. Countries like Britain and the USA, for example.

Historical responsibility for climate impact

There's another factual foundation I'd like to explore. If we assume that the climate has been damaged by human activity, and that someone needs to fix it, who should pay? Some people say "the polluter should pay." The preceding pictures showed who's doing the polluting today. But it isn't the *rate* of CO₂ pollution that matters, it's the cumulative *total* emissions; much of the emitted carbon dioxide (one third of it) will hang out in the atmosphere for at least 50 or 100 years. If we accept the ethical idea that "the polluter should pay" then we should ask how big is each country's historical footprint. The next picture shows each country's cumulative emissions of CO₂, expressed as an average emission rate over the period 1880–2004.



Congratulations, Britain! The UK has made it onto the winners' podium. We may be only an average European country today, but in the table of historical emissions, per capita, we are second only to the USA.

OK, that's enough ethics. What do scientists reckon needs to be done, to avoid a risk of giving the earth a 2 °C temperature rise (2 °C being the rise above which they predict lots of bad consequences)? The consensus is clear. We need to get off our fossil fuel habit, and we need to do so fast. Some countries, including Britain, have committed to a 60% reduction in greenhouse-gas emissions by 2050, but it must be emphasized that such cuts, radical though they are, are unlikely to cut the mustard. If the world's emissions were gradually reduced by 60% by 2050, climate scientists reckon it's more likely than not that global temperatures will rise

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

by more than 2 °C. The sort of cuts we need to aim for are shown in figure 1.8. This figure shows two possibly-safe emissions scenarios presented by Baer and Mastrandrea [2006] in a report from the Institute for Public Policy Research. The lower curve assumes that a decline in emissions started in 2007, with total global emissions falling at roughly 5% per year. The upper curve assumes a brief delay in the start of the decline, and a 4% drop per year in global emissions. Both scenarios are believed to offer a modest chance of avoiding a 2 °C temperature rise. In the lower scenario, the chance that the temperature rise will *exceed* 2 °C is estimated to be 9–26%. In the upper scenario, the chance of exceeding 2 °C is estimated to be 16–43%. These possibly-safe emissions trajectories, by the way, involve significantly sharper reductions in emissions than any of the scenarios presented by the Intergovernmental Panel on Climate Change (IPCC), or by the Stern Review, or by Socolow [2006].

These possibly-safe trajectories require global emissions to fall by 70% or 85% by 2050. What would this mean for a country like Britain? If we subscribe to the idea of "contraction and convergence," which means that all countries aim eventually to have equal per-capita emissions, then Britain needs to aim for cuts greater than 85%: it should get down from its current 11 tons of $CO_2^{(e)}$ per year per person to roughly 1 ton per year per

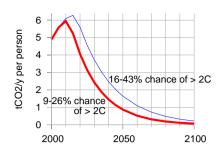
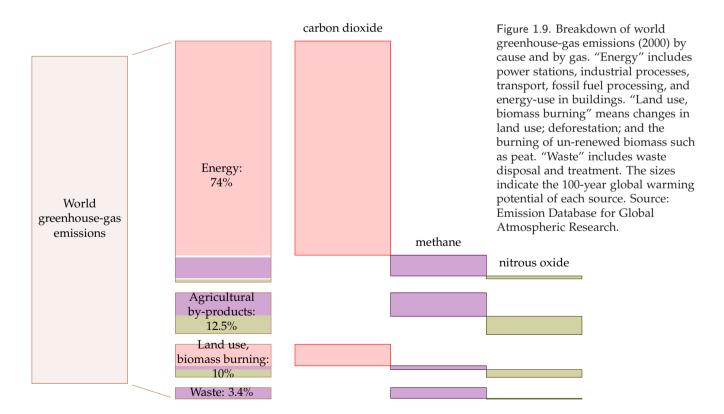


Figure 1.8. Global emissions for two scenarios considered by Baer and Mastrandrea, expressed in tons of CO₂ per person, using a world population of six billion. Both scenarios are believed to offer a modest chance of avoiding a 2 °C temperature rise.



Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

person by 2050. This is such a deep cut, I suggest the best way to think about it is *no more fossil fuels*.

One last thing about the climate-change motivation: while a range of human activities cause greenhouse-gas emissions, the biggest cause by far is **energy use**. Some people justify not doing anything about their energy use by excuses such as "methane from burping cows causes more warming than jet travel." Yes, agricultural by-products contributed one eighth of greenhouse-gas emissions in the year 2000. But energy-use contributed three quarters (figure 1.9). The climate change problem is principally an energy problem.

Warnings to the reader

OK, enough about climate change. I'm going to assume we are motivated to get off fossil fuels. Whatever your motivation, the aim of this book is to help you figure out the numbers and do the arithmetic so that you can evaluate policies; and to lay a factual foundation so that you can see which proposals add up. I'm not claiming that the arithmetic and numbers in this book are new; the books I've mentioned by Goodstein, Lomborg, and Lovelock, for example, are full of interesting numbers and back-of-envelope calculations, and there are many other helpful sources on the internet too (see the notes at the end of each chapter).

What I'm aiming to do in this book is to make these numbers simple and memorable; to show you how you can figure out the numbers for yourself; and to make the situation so clear that any thinking reader will be able to draw striking conclusions. I don't want to feed you my own conclusions. Convictions are stronger if they are self-generated, rather than taught. Understanding is a creative process. When you've read this book I hope you'll have reinforced the confidence that you can figure anything out.

I'd like to emphasize that the calculations we will do are deliberately imprecise. Simplification is a key to understanding. First, by rounding the numbers, we can make them easier to remember. Second, rounded numbers allow quick calculations. For example, in this book, the population of the United Kingdom is 60 million, and the population of the world is 6 billion. I'm perfectly capable of looking up more accurate figures, but accuracy would get in the way of fluent thought. For example, if we learn that the world's greenhouse gas emissions in 2000 were 34 billion tons of $\rm CO_2$ -equivalent per year, then we can instantly note, without a calculator, that the average emissions per person are $\rm 5^{1/2}$ tons of $\rm CO_2$ -equivalent per person per year. This rough division (34 divided by 6 is $\rm 5^{1/2}$) is not exact, but it's quick and it's good enough to inform interesting conversations. For instance, if you learn that a round-trip intercontinental flight emits nearly two tons of $\rm CO_2$ per passenger, then knowing the average emissions yardstick ($\rm 5^{1/2}$ tons per year per person) helps you realize that



"Look – it's Low Carbon Emission Man"

Figure 1.10. Reproduced by kind permission of PRIVATE EYE / Peter Dredge www.private-eye.co.uk.

just one such plane-trip per year corresponds to over a third of the average person's carbon emissions.

I like to base my calculations on everyday knowledge rather than on trawling through impersonal national statistics. For example, if I want to estimate the typical wind speeds in Cambridge, I ask "is my cycling speed usually faster than the wind?" The answer is yes. So I can deduce that the wind speed in Cambridge is only rarely faster than my typical cycling speed of 20 km/h (5.6 m/s, or 12 miles per hour). I back up these everyday estimates with other peoples' calculations and with official statistics. (Please look for these in each chapter's end-notes.) This book isn't intended to be a definitive store of super-accurate numbers. Rather, it's intended to illustrate how to use approximate numbers as a part of constructive consensual conversations.

In the calculations, I'll mainly use the United Kingdom and occasionally Europe, America, or the whole world, but you should find it easy to redo the calculations for whatever country or region you are interested in.

Let me close this chapter with a few more warnings to the reader. Not only will we make a habit of approximating the numbers we calculate; we'll also neglect all sorts of details that investors, managers, and economists have to attend to, poor folks. If you're trying to launch a renewable technology, just a 5% increase in costs may make all the difference between success and failure, so in business every detail must be tracked. But 5% is too small for this book's radar. This is a book about factors of 2 and factors of 10. It's about fundamental limits to sustainable energy, not current economic feasibility. While economics is always changing, the fundamental limits won't ever go away. We need to understand these limits.

Debates about energy policy are often confusing and emotional because people mix together *factual* assertions and *ethical* assertions.

Examples of **factual assertions** are "global fossil-fuel burning emits 34 billion tons of carbon dioxide equivalent per year"; and "if CO₂ concentrations are doubled then average temperatures will increase by 1.5–5.8°C in the next 100 years"; and "a temperature rise of 2°C would cause the Greenland ice cap to melt within 500 years"; and "the complete melting of the Greenland ice cap would cause a 7-metre sea-level rise."

A factual assertion is either true or false; figuring out *which* may be difficult; it is a scientific question. For example, the assertions I just gave are either true or false. But we don't know whether they are all true. Some of them are currently judged "very likely." The difficulty of deciding which factual assertions are true leads to debates in the scientific community. But given sufficient scientific experiment and discussion, the truth or falsity of most factual assertions can eventually be resolved, at least "beyond reasonable doubt."

Examples of **ethical assertions** are "it's wrong to exploit global resources in a way that imposes significant costs on future generations"; and "polluting should not be free"; and "we should take steps to ensure that

it's unlikely that CO₂ concentrations will double"; and "politicians should agree a cap on CO₂ emissions"; and "countries with the biggest CO₂ emissions over the last century have a duty to lead action on climate change"; and "it is fair to share CO₂ emission rights equally across the world's population." Such assertions are not "either true or false." Whether we agree with them depends on our ethical judgment, on our values. Ethical assertions may be incompatible with each other; for example, Tony Blair's government declared a radical policy on CO₂ emissions: "the United Kingdom should reduce its CO₂ emissions by 60% by 2050"; at the same time Gordon Brown, while Chancellor in that government, repeatedly urged oil-producing countries to *increase* oil production.

This book is emphatically intended to be about facts, not ethics. I want the facts to be clear, so that people can have a meaningful debate about ethical decisions. I want everyone to understand how the facts constrain the options that are open to us. Like a good scientist, I'll try to keep my views on ethical questions out of the way, though occasionally I'll blurt something out – please forgive me.

Whether it's *fair* for Europe and North America to hog the energy cake is an ethical question; I'm here to remind you of the *fact* that we can't have our cake and eat it too; to help you weed out the pointless and ineffective policy proposals; and to help you identify energy policies that are compatible with your personal values.

We need a plan that adds up!



"Okay – it's agreed; we announce – 'to do nothing is not an option!' then we wait and see how things pan out..."

Figure 1.11. Reproduced by kind permission of PRIVATE EYE / Paul Lowe www.private-eye.co.uk.

Notes and further reading

At the end of each chapter I'll note details of ideas in that chapter, sources of data and quotes, and pointers to further information.

page no.

- 2 "... no other possible way of doing that except through renewables"; "anybody who is relying upon renewables to fill the [energy] gap is living in an utter dream world and is, in my view, an enemy of the people." The quotes are from Any Questions?, 27 January 2006, BBC Radio 4 [ydoobr]. Michael Meacher was UK environment minister from 1997 till 2003. Sir Bernard Ingham was an aide to Margaret Thatcher when she was prime minister, and was Head of the Government Information Service. He is secretary of Supporters of Nuclear Energy.
- Jonathan Porritt (March 2006). Is nuclear the answer? Section 3. Advice to Ministers. http://www.sd-commission.org.uk/
- James Lovelock. http://www.ecolo.org/lovelock/
- 3 "Nuclear is a money pit", "We have a huge amount of wave and wind." Ann Leslie, journalist. Speaking on Any Questions?, Radio 4, 10 February 2006.
- Los Angeles residents drive ... from Earth to Mars [The Earthworks Group, 1989, page 34].
- targetneutral. com charges just £4 per ton of CO₂ for their "neutralization." (A significantly lower price than any other "offsetting" company I have come across.) At this price, a typical Brit could have his 11 tons per year
- © David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

"neutralized" for just £44 per year! Evidence that BP's "neutralization" schemes don't really add up comes from the fact that its projects have not achieved the Gold Standard http://www.cdmgoldstandard.org/ (Michael Schlup, personal communication). Many "carbon offset" projects have been exposed as worthless by Fiona Harvey of the Financial Times [2jhve6].

4 People who want to promote renewables over nuclear, for example, say "offshore wind power could power all UK homes."

At the end of 2007, the UK government announced that they would allow the building of offshore wind turbines "enough to power all UK homes." Friends of the Earth's renewable energy campaigner, Nick Rau, said the group welcomed the government's announcement. "The potential power that could be generated by this industry is enormous," he said. [25e59w]. From the Guardian [5o7mxk]: John Sauven, the executive director of Greenpeace, said that the plans amounted to a "wind energy revolution." "And Labour needs to drop its obsession with nuclear power, which could only ever reduce emissions by about 4% at some time in the distant future." Friends of the Earth's renewable energy campaigner, Nick Rau, said: "We are delighted the government is getting serious about the potential for offshore wind, which could generate 25% of the UK's electricity by 2020." A few weeks later, the government announced that it would permit new nuclear build. "Today's decision to give the go-ahead to a new generation of nuclear power stations ... will do little to tackle climate change," Friends of the Earth warned [5c4o1c].

In fact, the two proposed expansions – of offshore wind and of nuclear – would both deliver just the same amount of electricity per year. The total permitted offshore wind power of 33 GW would on average deliver 10 GW, which is 4 kWh per day per person; and the replacement of all the retiring nuclear power stations would deliver 10 GW, which is 4 kWh per day per person. Yet in the same breath, anti-nuclear campaigners say that the nuclear option would "do little," while the wind option would "power all UK homes." The fact is, "powering all UK homes" and "only reducing emission by about 4%" are the same thing.

- "water-powered car" New Scientist, 29th July 2006, p. 35. This article, headlined "Water-powered car might be available by 2009", opened thus:
 - "Forget cars fuelled by alcohol and vegetable oil. Before long, you might be able to run your car with nothing more than water in its fuel tank. It would be the ultimate zero-emissions vehicle.
 - "While water is not at first sight an obvious power source, it has a key virtue: it is an abundant source of hydrogen, the element widely touted as the green fuel of the future."
 - The work New Scientist was describing was not ridiculous if I recall correctly, it was actually about a car using *Aluminium* as a fuel, with an Aluminium/water reaction as one of the first chemical steps. Why did New Scientist feel the urge to turn this into a story suggesting that water was the fuel? Water is not a fuel. It never has been, and it never will be. It is already burned! The first law of thermodynamics says you can't get energy for nothing; you can only convert energy from one form to another. The energy in any engine must come from somewhere. Fox News peddled an even more absurd story [2fztd3].
- Climate change is a far greater threat to the world than international terrorism. Sir David King, Chief Scientific Advisor to the UK government, January, 2004. [26e8z]
- the glorification of travel an allusion to the offence of "glorification" defined in the UK's Terrorism Act which came into force on 13 April, 2006. [ykhayj]
- 5 *Figure 1.2.* This figure shows production of crude oil including lease condensate, natural gas plant liquids, and other liquids, and refinery processing gain. Sources: EIA, and BP statistical review of world energy.
- 6 The first practical steam engine was invented in 1698. In fact, Hero of Alexandria described a steam engine, but given that Hero's engine didn't catch on in the following 1600 years, I deem Savery's 1698 invention the first practical steam engine.

- Figures 1.4 and 1.7: Graph of carbon dioxide concentration. The data are collated from Keeling and Whorf [2005] (measurements spanning 1958–2004); Neftel et al. [1994] (1734–1983); Etheridge et al. [1998] (1000–1978); and Siegenthaler et al. [2005] (950–1888 AD); and Indermuhle et al. [1999] (from 11 000 to 450 years before present). This graph, by the way, should not be confused with the "hockey stick graph" – the hockey stick graph shows the history of global temperatures. Attentive readers will have noticed that the climate-change argument I presented makes no mention of historical temperatures.

Figures 1.5–1.7: Coal production numbers are from Jevons [1866], Malanima [2006], Netherlands Environmental Assessment Agency [2006], National Bureau of Economic Research [2001], Hatcher [1993], Flinn and Stoker [1984], Church et al. [1986], Supple [1987], Ashworth and Pegg [1986]. Jevons was the first "Peak Oil" author. He estimated Britain's easily-accessible coal reserves, looked at the history of exponential growth in consumption, and predicted, in 1865, the end of the exponential growth and the end of the British dominance of world industry. "We cannot long maintain our present rate of increase of consumption. ... the check to our progress must become perceptible within a century from the present time. ... the conclusion is inevitable, that our present happy progressive condition is a thing of limited duration." Jevons was right. Within a century British coal production indeed peaked, and there were two world wars.

Dominic Lawson, a columnist from the Independent. My quote is adapted from Dominic Lawson's column in the Independent, 8 June, 2007. It is not a verbatim quote: I edited his words to make them briefer but took care not to correct any of his errors. All three numbers he mentions are incorrect. Here's how he screwed up. First, he says "carbon dioxide" but gives numbers for carbon: the burning of fossil fuels sends 26 gigatonnes of CO₂ per year into the atmosphere (not 7 gigatonnes). A common mistake. Second, he claims that the oceans send 36 000 gigatonnes of carbon per year into the atmosphere. This is a far worse error: 36 000 gigatonnes is the total amount of carbon in the ocean! The annual flow is much smaller – about 90 gigatonnes of carbon per year (330 Gt CO₂/y), according to standard diagrams of the carbon cycle [16y5g] [I believe this 90 Gt C/y is the estimated flow rate, were the atmosphere suddenly to have its CO₂ concentration reduced to zero]. Similarly his "1900 gigatonne" flow from biosphere to atmosphere is wrong. The correct figure according to the standard diagrams is about 120 gigatonnes of carbon per year $(440 \text{ Gt CO}_2/\text{y})$.

The weights of an atom of carbon and a molecule of CO_2 are in the ratio 12 to 44, because the carbon atom weighs 12 units and the two oxygen atoms weigh 16 each. 12 + 16 + 16 = 44.

Incidentally, the observed rise in CO_2 concentration is nicely in line with what you'd expect, assuming most of the human emissions of carbon remained in the atmosphere. From 1715 to 2004, roughly 1160 Gt CO_2 have been released to the atmosphere from the consumption of fossil fuels and cement production [Marland et al., 2007]. If all of this CO_2 had stayed in the atmosphere, the concentration would have risen by 160 ppm (from 280 to 440 ppm). The actual rise has been 97 ppm (from 280 to 377 ppm). So roughly 60% of what was emitted is now in the atmosphere.

10 Carbon dioxide has a warming effect. The over-emotional debate about this topic is getting quite tiresome, isn't it? "The science is now settled." "No it isn't!" "Yes it is!" I think the most helpful thing I can do here is direct anyone who wants a break from the shouting to a brief report written by Charney et al. [1979]. This report's conclusions carry weight because the National Academy of Sciences commissioned the report and selected its authors on the basis of their expertise, "and with regard for appropriate balance." The study group was convened "under the auspices of the Climate Research Board of the National Research Council to assess the scientific basis for projection of possible future climatic changes resulting from man-made releases of carbon dioxide into the

atmosphere." Specifically, they were asked: "to identify the principal premises on which our current understanding of the question is based, to assess quantitatively the adequacy and uncertainty of our knowledge of these factors and processes, and to summarize in concise and objective terms our best present understanding of the carbon dioxide/climate issue for the benefit of policy-makers."

The report is just 33 pages long, it is free to download [5qfkaw], and I recommend it. It makes clear which bits of the science were already settled in 1979, and which bits still have uncertainty.

Here are the main points I picked up from this report. First, doubling the atmospheric CO_2 concentration would change the net heating of the troposhere, oceans, and land by an average power per unit area of roughly $4\,\text{W/m}^2$, if all other properties of the atmosphere remained unchanged. This heating effect can be compared with the average power absorbed by the atmosphere, land, and oceans, which is $238\,\text{W/m}^2$. So doubling CO_2 concentrations would have a warming effect equivalent to increasing the intensity of the sun by 4/238 = 1.7%. Second, the consequences of this CO_2 -induced heating are hard to predict, on account of the complexity of the atmosphere/ocean system, but the authors predicted a global surface warming of between $2\,^{\circ}C$ and $3.5\,^{\circ}C$, with greater increases at high latitudes. Finally, the authors summarize: "we have tried but have been unable to find any overlooked or underestimated physical effects that could reduce the currently estimated global warmings due to a doubling of atmospheric CO_2 to negligible proportions or reverse them altogether." They warn that, thanks to the ocean, "the great and ponderous flywheel of the global climate system," it is quite possible that the warming would occur sufficiently sluggishly that it would be difficult to detect in the coming decades. Nevertheless "warming will eventually occur, and the associated regional climatic changes ... may well be significant."

The foreword by the chairman of the Climate Research Board, Verner E. Suomi, summarizes the conclusions with a famous cascade of double negatives. "If carbon dioxide continues to increase, the study group finds no reason to doubt that climate changes will result and no reason to believe that these changes will be negligible."

- 10 The litary of probable drastic effects of climate change I'm sure you've heard it before. See [2z2xg7] if not.
- 12 Breakdown of world greenhouse gas emissions by region and by country. Data source: Climate Analysis Indicators Tool (CAIT) Version 4.0. (Washington, DC: World Resources Institute, 2007).
- 14 Congratulations, Britain! ... in the table of historical emissions, per capita, we are second only to the USA. Sincere apologies here to Luxembourg, whose historical per-capita emissions actually exceed those of America and Britain; but I felt the winners' podium should really be reserved for countries having both large per-capita and large total emissions. In total terms the biggest historical emitters are, in order, USA (322 Gt CO₂), Russian Federation (90 Gt CO₂), China (89 Gt CO₂), Germany (78 Gt CO₂), UK (62 Gt CO₂), Japan (43 Gt CO₂), France (30 Gt CO₂), India (25 Gt CO₂), and Canada (24 Gt CO₂). The per-capita order is: Luxembourg, USA, United Kingdom, Czech Republic, Belgium, Germany, Estonia, Qatar, and Canada.
- 15 Figure 1.8. In the lower scenario, the chance that the temperature rise will exceed 2 °C is estimated to be 9–26%; the cumulative carbon emissions from 2007 onwards are 309 Gt C; CO₂ concentrations reach a peak of 410 ppm, CO₂^(e) concentrations peak at 421 ppm, and in 2100 CO₂ concentrations fall back to 355 ppm. In the upper scenario, the chance of exceeding 2 °C is estimated to be 16–43%; the cumulative carbon emissions from 2007 onwards are 415 Gt C; CO₂ concentrations reach a peak of 425 ppm, CO₂^(e) concentrations peak at 435 ppm, and in 2100 CO₂ concentrations fall back to 380 ppm.
- there are many other helpful sources on the internet. I recommend, for example: BP's Statistical Review of World Energy [yyxq2m], the Sustainable Development Commission www.sd-commission.org.uk, the Danish Wind Industry Association www.windpower.org, Environmentalists For Nuclear Energy www.ecolo.org, Wind Energy Department, Risø University www.risoe.dk/vea, DEFRA www.defra.gov.uk/environment/statistics, especially the book Avoiding Dangerous Climate Change [dzcqq], the Pembina Institute www.pembina.org/publications.asp, and the DTI (now known as BERR) www.dti.gov.uk/publications/.

- 17 factual assertions and ethical assertions... Ethical assertions are also known as 'normative claims', and factual assertions are known as "positive claims." Ethical assertions usually contain verbs like "should" and "must," or adjectives like "fair," "right," and "wrong." For helpful further reading see Dessler and Parson [2006].
- 18 *Gordon Brown*. On 10th September, 2005, Gordon Brown said the high price of fuel posed a significant risk to the European economy and to global growth, and urged OPEC to raise oil production. Again, six months later, he said "we need ... more production, more drilling, more investment, more petrochemical investment" (22nd April, 2006). [y98ys5]
 - I'd like to temper this criticism of Gordon Brown by praising one of his more recent initiatives, namely the promotion of electric vehicles and plug-in hybrids. As you'll see later, one of this book's conclusions is that electrification of most transport is a good part of a plan for getting off fossil fuels.

2 The balance sheet

Nature cannot be fooled.

Richard Feynman

The first part of this book is about energy consumption and energy production.

We're going to make two stacks. In the left-hand stack we will add up our energy consumption, and in the right-hand stack, we'll add up sustainable energy production. At the moment, most of the energy the developed world consumes is produced from fossil fuels; that's not sustainable. Exactly how long we could keep living on fossil fuels is an interesting question, but it's not the question we'll address in this book. I want to think about living without fossil fuels.

The question addressed in this book is "can we *conceivably* live sustainably?" So, we will add up all *conceivable* sustainable energy sources and put them in the right-hand stack.

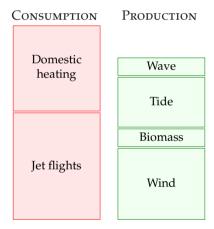


Figure 2.1. Our balance sheet. This picture shows what it might look like after we've added two forms of consumption and four forms of sustainable production.

In the left-hand, red stack, we'll estimate the consumption of a "typical moderately-affluent person"; I encourage you to tot up an estimate of your *own* consumption, creating your own personalized left-hand stack too. Later on we'll also find out the current average energy consumption of Europeans and Americans.

As we estimate our consumption of energy for heating, transportation, manufacturing, and so forth, the aim is not only to compute a number for the left-hand stack of our balance sheet, but also to understand what each number depends on, and how susceptible to modification it is.

In the right-hand, green stack, we'll add up the sustainable production estimates for the United Kingdom. This will allow us to answer the question "can the UK conceivably live on its own renewables?"

Whether the sustainable energy sources that we put in the right-hand stack are *economically* feasible is an important question, but let's leave that question to one side, and just add up the two stacks first. Sometimes people focus too much on economic feasibility and they miss the big picture. For example, people discuss "is wind cheaper than nuclear?" and forget to ask "how *much* wind is available?" or "how much uranium is left?"

Some key forms of consumption for the left-hand stack will be:

- transport
 - cars, planes, freight
- · heating and cooling
- lighting
- information systems and other gadgets
- food
- manufacturing.

In the right-hand sustainable-production stack, our main categories will be:

- wind
- solar
 - photovoltaics, thermal, biomass
- hydroelectric
- wave
- tide
- geothermal
- nuclear? (with a question-mark, because it's not clear whether nuclear power counts as "sustainable")

The outcome when we add everything up might look like this:

Total conceivable sustainable production

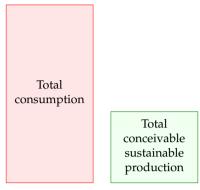
Total consumption

If we find consumption is much less than conceivable sustainable production, then we can say "good, *maybe* we can live sustainably; let's look into the economic, social, and environmental costs of the sustainable alternatives, and figure out which of them deserve the most research and development; if we do a good job, there *might* not be an energy crisis."

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

2 — The balance sheet 25

On the other hand, the outcome of our sums might look like this:



– a much bleaker picture. This picture says "it doesn't matter what the economics of sustainable power are: there's simply *not enough* sustainable power to support our current lifestyle; massive change is coming."

Energy and power

Most discussions of energy consumption and production are confusing because of the proliferation of *units* in which energy and power are measured, from "tons of oil equivalent" to "terawatthours" (TWh) and "exajoules" (EJ). Nobody but a specialist has a feeling for what "a barrel of oil" or "a million BTUs" means in human terms. In this book, we'll express everything in a single set of personal units that everyone can relate to.

The unit of **energy** I have chosen is the kilowatt-hour (kWh). This quantity is called "one unit" on electricity bills, and it costs a domestic user about 10p in the UK in 2008. As we'll see, most individual daily choices involve amounts of energy equal to small numbers of kilowatt-hours.

When we discuss **powers** (rates at which we use or produce energy), the main unit will be the kilowatt-hour per day (kWh/d). We'll also occasionally use the watt ($40\,\mathrm{W} \simeq 1\,\mathrm{kWh/d}$) and the kilowatt ($1\,\mathrm{kW} = 1000\,\mathrm{W} = 24\,\mathrm{kWh/d}$), as I'll explain below. The kilowatt-hour per day is a nice human-sized unit: most personal energy-guzzling activities guzzle at a rate of a small number of kilowatt-hours per day. For example, one $40\,\mathrm{W}$ lightbulb, kept switched on all the time, uses **one** kilowatt-hour per day. Some electricity companies include graphs in their electricity bills, showing energy consumption in kilowatt-hours per day.

One kilowatt-hour per day is roughly the power you could get from one human servant. The number of kilowatt-hours per day you use is thus the effective number of servants you have working for you.

People use the two terms energy and power interchangeably in ordinary speech, but in this book we must stick rigorously to their scientific definitions. *Power is the rate at which something uses energy.*



Figure 2.4. Distinguishing energy and power. Each of these 60 W light bulbs has a *power* of 60 W when switched on; it doesn't have an "energy" of 60 W. The bulb uses 60 W of electrical *power* when it's on; it emits 60 W of *power* in the form of light and heat (mainly the latter).

Maybe a good way to explain energy and power is by an analogy with water and water-flow from taps. If you want a drink of water, you want a *volume* of water – one litre, say (if you're thirsty). When you turn on a tap, you create a *flow* of water – one litre per minute, perhaps, if the tap yields only a trickle; or ten litres per minute, from a more generous tap. You can get the same volume (one litre) either by running the trickling tap for one minute, or by running the generous tap for one tenth of a minute. The *volume* delivered in a particular time is equal to the *flow* multiplied by the *time*.

$$volume = flow \times time$$

We say that a *flow* is a *rate* at which *volume* is delivered. If you know the volume delivered in a particular time, you can get the flow by dividing the volume by the time.

$$flow = \frac{volume}{time}$$

Here's the connection to energy and power. Water *volume* is like *energy*: water *flow* is like *power*.

If someone throws a jug of water into the garden, we say "they threw away a *volume* of water (perhaps a litre)." Similarly if someone sets fire to a can of petrol, we could say "they wasted a lot of *energy* there! (perhaps 40 kWh of energy)."

If someone leaves a tap trickling, we might say "that *flow* is wasting one litre per minute!" Similarly if someone leaves a lightbulb switched on, we might say "the *power* wasted by that bulb is about one kilowatt-hour per day".

When a tap is set trickling, a *flow* is created. A trickling flow might deliver one litre per minute; or, to put it another way, sixty litres per hour. Similarly, whenever a toaster is switched on, it starts to consume *power* at a rate of one kilowatt. It continues to consume one kilowatt until it is switched off. To put it another way, the toaster (if it's left on permanently) consumes one kilowatt-hour (kWh) per hour; it also consumes twenty-four kilowatt-hours per day.

You can work out the energy used by a particular activity by multiplying the power by the duration.

$$energy = power \times time$$

The joule is the standard international unit of energy, but sadly it's far too small to work with. The kilowatt-hour is equal to 3.6 million joules (3.6 megajoules).

Powers are so useful and important, they have something that flows don't have: they have their own special units. When we talk of a flow, we might measure it in "litres per minute," "gallons per hour," or "cubic-metres per second;" these units' names make clear that the flow is "a volume per unit time." A power of *one joule per second* is called *one watt*. One

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

volume is measured in litres is measured in litres per minute

energy power is measured in kWh kWh per day

thousand joules per second is called one kilowatt. Let's get the terminology straight: the toaster uses one kilowatt. It doesn't use "one kilowatt per second." The "per second" is already built in to the definition of the kilowatt: one kilowatt means "one kilojoule per second."

Other examples of units that, like the watt, already have a "per time" built in are the knot – "our yacht's speed was ten knots!" (a knot is one nautical mile *per* hour); the hertz – "I could hear a buzzing at 50 hertz" (one hertz is a frequency of one cycle *per* second); the ampere – "the fuse blows when the current is higher than 13 amps" (*not* 13 amps per second); and the horsepower – "that stinking engine delivers 50 horsepower" (*not* 50 horsepower per second, nor 50 horsepower per hour, nor 50 horsepower per day, just 50 horsepower). Similarly we say "a nuclear power station generates one gigawatt." One gigawatt, by the way, is one million kilowatts, or a thousand megawatts. So one gigawatt is a million toasters. And the "g"s in gigawatt are pronounced hard, the same as in "giggle." And, while I'm tapping the blackboard, we capitalize the "g" and "w" in "gigawatt" only when we write the abbreviation "GW."

Please, never, ever say "one kilowatt per second," "one kilowatt per hour," or "one kilowatt per day;" none of these is a valid measure of power. The urge that people have to say "per something" when talking about their toasters is one of the reasons I decided to use the "kilowatt-hour per day" as my unit of power. I'm sorry that it's a bit cumbersome to say and to write.

Here's one last thing to make clear: If I say "someone used a gigawatt-hour of energy," I am simply telling you *how much* energy they used, not *how fast* they used it. Talking about a gigawatt-hour *doesn't* imply the energy was used *in one hour*. You could use a gigawatt-hour of energy by switching on one million toasters for one hour, or by switching on a thousand toasters for one thousand hours.

Picky details

Isn't energy conserved? We talk about "using" energy, but doesn't one of the laws of nature say that energy can't be created or destroyed?

Yes, I'm being imprecise. This is really a book about *entropy* – a trickier thing to explain. When we "use up" one kilojoule of energy, what we're really doing is taking one kilojoule of energy in a form that has *low entropy* (for example, electricity), and *converting* it into an exactly equal amount of energy in another form, usually one that has much higher entropy (for example, hot air or hot water). When we've "used" the energy, it's still there; but we normally can't "use" the energy over and over again, because only *low entropy* energy is "useful" to us. Sometimes these different grades of energy are distinguished by adding a label to the units: one kWh(e) is one kilowatt-hour of electrical energy – the highest grade of energy. One

energy is measured in kWh or MI power
is measured in
kWh per day
or
kW
or
W (watts)
or
MW (megawatts)
or
GW (gigawatts)
or
TW (terawatts)

kWh(th) is one kilowatt-hour of thermal energy – for example the energy in ten litres of boiling-hot water. Energy lurking in higher-temperature things is more useful (lower entropy) than energy in tepid things. A third grade of energy is chemical energy. Chemical energy is high-grade energy like electricity.

It's a convenient but sloppy shorthand to talk about the energy rather than the entropy, and that is what we'll do most of the time in this book. Occasionally, we'll have to smarten up this sloppiness; for example, when we discuss refrigeration, power stations, heat pumps, or geothermal power.

Are you comparing apples and oranges? Is it valid to compare different forms of energy such as the chemical energy that is fed into a petrolpowered car and the electricity from a wind turbine?

By comparing consumed energy with conceivable produced energy, I do not wish to imply that all forms of energy are equivalent and interchangeable. The electrical energy produced by a wind turbine is of no use to a petrol engine; and petrol is no use if you want to power a television. In principle, energy can be converted from one form to another, though conversion entails losses. Fossil-fuel power stations, for example, guzzle chemical energy and produce electricity (with an efficiency of 40% or so). And aluminium plants guzzle electrical energy to create a product with high chemical energy – pure aluminium (with an efficiency of 30% or so).

In some summaries of energy production and consumption, all the different forms of energy are put into the same units, but multipliers are introduced, rating electrical energy from hydroelectricity for example as being worth 2.5 times more than the chemical energy in oil. This bumping up of electricity's effective energy value can be justified by saying, "well, 1 kWh of electricity is equivalent to 2.5 kWh of oil, because if we put that much oil into a standard power station it would deliver 40% of 2.5 kWh, which is 1 kWh of electricity." In this book, however, I will usually use a one-to-one conversion rate when comparing different forms of energy. It is not the case that 2.5 kWh of oil is inescapably equivalent to 1 kWh of electricity; that just happens to be the perceived exchange rate in a worldview where oil is used to make electricity. Yes, conversion of chemical energy to electrical energy is done with this particular inefficient exchange rate. But electrical energy can also be converted to chemical energy. In an alternative world (perhaps not far-off) with relatively plentiful electricity and little oil, we might use electricity to make liquid fuels; in that world we would surely not use the same exchange rate – each kWh of gasoline would then cost us something like 3 kWh of electricity! I think the timeless and scientific way to summarize and compare energies is to hold 1 kWh of chemical energy equivalent to 1 kWh of electricity. My choice to use this one-to-one conversion rate means that some of my sums will look a bit different from other people's (for example, BP's Statistical Review of World Energy rates 1 kWh of electricity as equivalent to $100/38 \simeq 2.6$ kWh of oil; on the other

[©] David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

2 — The balance sheet 29

hand, the government's *Digest of UK Energy Statistics* uses the same one-to-one conversion rate as me). And I emphasize again, this choice does not imply that I'm suggesting you could convert either form of energy directly into the other. Converting chemical energy into electrical energy always wastes energy, and so does converting electrical into chemical energy.

Physics and equations

Throughout the book, my aim is not only to work out numbers indicating our current energy consumption and conceivable sustainable production, but also to make clear *what these numbers depend on*. Understanding what the numbers depend on is essential if we are to choose sensible policies to change any of the numbers. Only if we understand the physics behind energy consumption and energy production can we assess assertions such as "cars waste 99% of the energy they consume; we could redesign cars so that they use one hundred times less energy." Is this assertion true? To explain the answer, I will need to use equations like

kinetic energy =
$$\frac{1}{2}mv^2$$
.

However, I recognize that to many readers, such formulae are a foreign language. So, here's my promise: I'll keep all this foreign-language stuff in technical chapters at the end of the book. Any reader with a high-school qualification in maths, physics, or chemistry should enjoy these technical chapters. The main thread of the book is intended to be accessible to everyone who can add, multiply, and divide. It is especially aimed at our dear elected and unelected representatives, the Members of Parliament.

One last point, before we get rolling: I don't know everything about energy. I don't have all the answers, and the numbers I offer are open to revision and correction. (Indeed I expect corrections and will publish them on the book's website.) The one thing I *am* sure of is that the answers to our sustainable energy questions will involve *numbers*; any sane discussion of sustainable energy requires numbers. This book's got 'em, and it shows how to handle them. I hope you enjoy it!

Notes and further reading

page no.

27 Please, never, ever say "one kilowatt per second." There are specific, rare exceptions to this rule. If talking about a growth in demand for power, we might say "British demand is growing at one gigawatt per year." In Chapter 26 when I discuss fluctuations in wind power, I will say "one morning, the power delivered by Irish windmills fell at a rate of 84 MW per hour." Please take care! Just one accidental syllable can lead to confusion: for example, your electricity meter's reading is in kilowatt-hours (kWh), not 'kilowatts-per-hour'.

I've provided a chart on p413 to help you translate between kWh per day per person and the other major units in which powers are discussed. The most commonly used units in public documents discussing power options are:

terawatt-hours per year (TWh/y).

1000 TWh/y per United Kingdom is roughly equal to 45 kWh/d per person.

2.5 GW per UK is 1 kWh/d per person.

million tons of oil equivalent per year (Mtoe/y).

2 Mtoe/y per UK is roughly 1 kWh/d per person.

1 Mtoe/y per UK is roughly 0.53 kWh/d per person.

As I said, I'll usually quote powers in kWh/d per person. One reason for liking these personal units is that it makes it much easier to move from talking about the UK to talking about other countries or regions. For example, imagine we are discussing waste incineration and we learn, in the standard units, that UK waste incineration delivers a power of 7TWh/y and that Denmark's waste incineration delivers 10TWh/y. Does this help us say whether Denmark does "more" waste incineration than the UK? While the total amount of energy produced from waste in each country may be interesting, I think that what we usually want to know is the amount of waste incineration *per person*. (For the record, that is: Denmark, 5kWh/d per person; UK, 0.3kWh/d per person.) By discussing everything per-person from the outset, we end up with a more transportable book, one that will hopefully be useful for sustainable energy discussions worldwide.

3 Cars

For our first chapter on consumption, let's study that icon of modern civilization: the car.

How much power does a regular car-user consume? Once we know the conversion rates, it's simple arithmetic:

$$\frac{\text{energy used}}{\text{per day}} = \frac{\text{distance travelled per day}}{\text{distance per unit of fuel}} \times \text{energy per unit of fuel}$$

For the **distance travelled per day**, let's use 50 km (30 miles).

For the **distance per unit of fuel**, also known as the **economy** of the car, let's use 33 miles per UK gallon (taken from an advertisement for a family car):

33 miles per imperial gallon = 12 km per litre.

What about the **energy per unit of fuel** (also called the **calorific value** or **energy density**)? Instead of looking it up, it's fun to estimate this sort of quantity by a bit of lateral thinking. Automobile fuels (whether diesel or petrol) are all hydrocarbons; and hydrocarbons can also be found on our breakfast table, with the calorific value conveniently written on the side: 8 kWh per kg (figure 3.2). Since we've estimated the economy of the car in miles per unit *volume* of fuel, we need to express the calorific value as an energy per unit *volume*. To turn our fuel's "8 kWh per kg" (an energy per unit *mass*) into an energy per unit volume, we need to know the density of the fuel. What's the density of butter? Well, butter just floats on water, as do fuel-spills, so its density must be a little less than water's, which is 1 kg per litre. If we guess a density of 0.8 kg per litre, we obtain a calorific value of:

```
8 kWh per kg \times 0.8 kg per litre = 7 kWh per litre.
```

Rather than wilfully perpetuate an inaccurate estimate, let's switch to the official value, for petrol, of 10 kWh per litre.

```
energy per day = \frac{\text{distance travelled per day}}{\text{distance per unit of fuel}} \times \text{energy per unit of fuel}
= \frac{50 \, \text{km/day}}{12 \, \text{km/litre}} \times 10 \, \text{kWh/litre}
\simeq \frac{40 \, \text{kWh/day}}{12 \, \text{km/loop}} \times 10 \, \text{kWh/loop}
```

Congratulations! We've made our first estimate of consumption.

This is the estimate for a typical car-driver driving a typical car today. Later chapters will discuss the *average* consumption of all British people, taking into account the fact that not everyone drives. We'll also discuss in





Figure 3.1. Cars. A red BMW dwarfed by a spaceship from the planet Dorkon.



NUTRIT	ION,
Typical Values	Per 100 g
Energy kJ	3080

Figure 3.2. Want to know the energy in car fuel? Look at the label on a pack of butter or margarine. The calorific value is 3000 kJ per 100 g, or about 8 kWh per kg.

calorific values		
petrol	10 kWh per litre	
diesel	11 kWh per litre	

Energy per distance car doing 33 mpg (12 km per litre)		
occupants		
1	80 kWh per 100 person-km	
4	20 kWh per 100 person-km	

Table 3.3. Facts worth remembering: passenger transport efficiencies.

part II what the consumption *could* be, with the help of other technologies such as electric cars.

Why does the car deliver 33 miles per gallon? Where's that energy going? Could we make cars that do 3300 miles per gallon? If we are interested in trying to reduce cars' consumption, we need to understand the physics behind cars' consumption. These questions are answered in the accompanying technical chapter A (p272), which provides a cartoon theory of cars' consumption. I encourage you to read the technical chapters if formulae like $\frac{1}{2}mv^2$ don't give you medical problems.

Chapter 3's conclusion: a typical car-driver uses about 40 kWh per day. Now we need to find out about sustainable production.

Queries

What about the energy-cost of producing the car's fuel?

Good point. When I estimate the energy consumed by a particular activity, I tend to choose a fairly tight "boundary" around the activity. This choice makes the estimation easier, but I agree that it's a good idea to try to estimate the full energy impact of an activity. It's been estimated that it takes 1.4 units of oil and other primary fuels to make 1 unit of petrol [Treloar et al., 2004].

What about the energy-cost of manufacturing the car?

Yes, that cost fell outside the boundary of this calculation too. We'll talk about car-making in Chapter 15.

Notes and further reading

page no.

31 For the distance travelled per day, let's use 50 km. This corresponds to 18 000 km (11 000 miles) per year. Roughly half of the British population drive to work. The total amount of car travel of the UK is 686 billion passenger-km per year, which corresponds to an "average distance travelled by car per British person" of 30 km per day. Source: Department for Transport [5647rh]. As I said on p23, I aim to estimate the consumption of a "typical moderately-affluent person" – the consumption that many people aspire to. Some people don't drive much. In this chapter, I

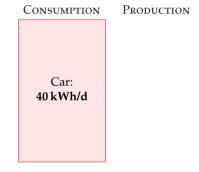


Figure 3.4. Chapter 3's conclusion: a typical car-driver uses about 40 kWh per day. Now we need to find out about sustainable production.

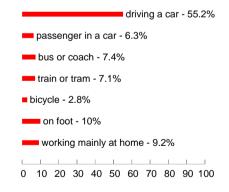


Figure 3.5. How British people travel to work, according to the 2001 census.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

want to estimate the energy consumed by someone who chooses to drive, rather than depersonalize the answer by reporting the UK average, which mixes together the drivers and non-drivers. If I said "the average use of energy for car driving in the UK is $24\,\mathrm{kWh/d}$ per person", I bet some people would misunderstand and say: "I'm a car driver so I guess I use $24\,\mathrm{kWh/d}$."

- 31 *let's use 33 miles per UK gallon.* 33 miles per gallon was the average for UK cars in 2005 [27jdc5]. Petrol cars have an average fuel consumption of 31 mpg; diesel cars, 39 mpg; new petrol cars (less than two years old), 32 mpg [Department for Transport, 2007]. Honda, "the most fuel-efficient auto company in America," records that its fleet of new cars sold in 2005 has an average top-level fuel economy of 35 miles per UK gallon. [28abpm]
- Let's guess a density of 0.8 kg per litre. Petrol's density is 0.737. Diesel's is 0.820-0.950 [nmn41].
- the official value of 10 kWh per litre. ORNL [2hcgdh] provide the following calorific values: diesel: 10.7 kWh/l; jet fuel: 10.4 kWh/l; petrol: 9.7 kWh/l.

When looking up calorific values, you'll find "gross calorific value" and "net calorific value" listed (also known as "high heat value' and "low heat value"). These differ by only 6% for motor fuels, so it's not crucial to distinguish them here, but let me explain anyway. The gross calorific value is the actual chemical energy released when the fuel is burned. One of the products of combustion is water, and in most engines and power stations, part of the energy goes into vaporizing this water. The net calorific value measures how much energy is left over assuming this wasted energy is discarded.

When we ask "how much energy does my lifestyle consume?" the gross calorific value is the right quantity to use. The net calorific value, on the other hand, is of interest to a power station engineer, who needs to decide which fuel to burn in his power station. Throughout this book I've tried to use gross calorific values.

A final note for party-pooping pedants who say "butter is not a hydrocarbon": OK, butter is not a *pure* hydrocarbon; but it's a good approximation to say that the main component of butter is long hydrocarbon chains. The proof of the pudding is, this approximation got us within 30% of the correct answer. Welcome to guerrilla physics.



4 Wind

The UK has the best wind resources in Europe.

Sustainable Development Commission

Wind farms will devastate the countryside pointlessly.

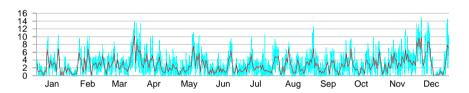
James Lovelock

How much wind power could we plausibly generate?

We can make an estimate of the potential of *on-shore* (land-based) wind in the United Kingdom by multiplying the average power per unit landarea of a wind farm by the area per person in the UK:

power per person = wind power per unit area \times area per person

Chapter B (p282) explains how to estimate the power per unit area of a wind-farm in the UK. If the typical windspeed is $6 \,\mathrm{m/s}$ (13 miles per hour, or $22 \,\mathrm{km/h}$), the power per unit area of wind-farm is about $2 \,\mathrm{W/m^2}$.



This figure of $6\,\text{m/s}$ is probably an over-estimate for many locations in Britain. For example, figure 4.1 shows daily average windspeeds in Cambridge during 2006. The daily average speed reached $6\,\text{m/s}$ on only about 30 days of the year – see figure 4.6 for a histogram. But some spots do have windspeeds above $6\,\text{m/s}$ – for example, the summit of Cairngorm in Scotland (figure 4.2).

Plugging in the British population density: 250 people per square kilometre, or 4000 square metres per person, we find that wind power could

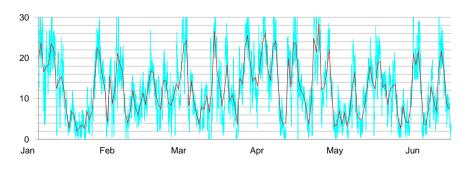




Figure 4.1. Cambridge mean wind speed in metres per second, daily (red line), and half-hourly (blue line) during 2006.



Figure 4.2. Cairngorm mean wind speed in metres per second, during six months of 2006.

35

plausibly generate

$$2 \text{ W/m}^2 \times 4000 \text{ m}^2/\text{person} = 8000 \text{ W per person}$$

if wind turbines were packed across the *whole* country. Converting to our favourite power units, that's

maximum conceivable wind power $\simeq 200 \,\text{kWh/d}$ per person.

Let's be realistic. What fraction of the country can we really imagine covering with windmills? Maybe 10%? Taking 10% of the maximum conceivable wind power, we obtain

maximum conceivable wind power (assuming 6 m/s and 10% filling) = 20 kWh/d per person.

Our conclusion: if we covered the windiest 10% of the country with windmills, we might be able to generate 20 kWh/d per person, which is *half* of the energy used by everyone driving an average fossil-fuel car 50 kmper day.

Britain's onshore wind energy resource may be "huge," but it's evidently not as huge as our huge consumption. We'll come to offshore wind later.

I should emphasize how generous an assumption I'm making. Let's compare this estimate of British wind potential with current installed wind power worldwide. The windmills that would be required to provide the UK with 20 kWh/d per person amount to fifty times the entire wind hardware of Denmark; seven times all the wind-farms of Germany; and double the entire fleet of all wind turbines in the world.

Please don't misunderstand me. Some readers seem to assume that I'm saying that we shouldn't bother building wind farms. Not at all. I'm simply trying to convey a helpful fact, namely that if we want wind power to truly make a difference, the wind farms must cover a very large area.

This conclusion – that the greatest that onshore wind could add up to, albeit "huge," is much less than our consumption – is important, so let's check the key figure, the assumed power per unit area of wind-farm (2 W/m^2) , against a real UK wind-farm.

The Whitelee wind-farm being built near Glasgow in Scotland has 140 turbines with a combined *peak* capacity of 322 MW in an area of 55 km². That's 6 W/m², *peak*. The average power produced is smaller because the turbines don't run at peak output all the time. The ratio of the average power to the peak power is called the "load factor" or "capacity factor," and it varies from site to site, and with the choice of hardware plopped on the site; a typical factor for a good site with modern turbines is 30%. If we assume Whitelee has a load factor of 33% then the average power production per unit land area is 2 W/m² - exactly the same as the power density we assumed earlier.

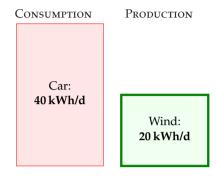


Figure 4.3. Chapter 4's conclusion: the maximum plausible production from on-shore windmills in the United Kingdom is 20 kWh per day per person.

Power per unit area	
wind-farm	2 W/m^2
(speed 6 m/s)	

Table 4.4. Facts worth remembering: wind-farms.

Population density of Britain $250 \text{ per km}^2 \leftrightarrow 4000 \text{ m}^2/\text{person}$

Table 4.5. Facts worth remembering: population density. See pages 190 and 368 for more population densities.

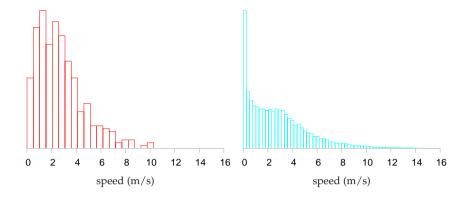


Figure 4.6. Histogram of Cambridge average wind speed in metres per second: daily averages (left), and half-hourly averages (right).

Queries

Wind turbines are getting bigger all the time. Do bigger wind turbines change this chapter's answer?

Chapter B explains. Bigger wind turbines deliver financial economies of scale, but they don't greatly increase the total power per unit land area, because bigger windmills have to be spaced further apart. A wind-farm that's twice as tall will deliver roughly 30% more power.

Wind power fluctuates all the time. Surely that makes wind less useful? Maybe. We'll come back to this issue in Chapter 26, where we'll look at wind's intermittency and discuss two possible solutions to this problem: energy storage, and demand management.

Notes and further reading

page no.

- 34 Figure 4.1 and figure 4.6. Cambridge wind data are from the Digital Technology Group, Computer Laboratory, Cambridge [vxhhj]. The weather station is on the roof of the Gates building, roughly 10 m high. Wind speeds at a height of 50 m are usually about 25% bigger. Cairngorm data (figure 4.2) are from Heriot–Watt University Physics Department [tdvml].
- 35 The windmills required to provide the UK with 20 kWh/d per person are fifty times the entire wind power of Denmark. Assuming a load factor of 33%, an average power of 20 kWh/d per person requires an installed capacity of 150 GW. At the end of 2006, Denmark had an installed capacity of 3.1 GW; Germany had 20.6 GW. The world total was 74 GW (wwindea.org). Incidentally, the load factor of the Danish wind fleet was 22% in 2006, and the average power they delivered was 3 kWh/d per person.

5 Planes

Imagine that you make one intercontinental trip per year by plane. How much energy does that cost?

A Boeing 747-400 with 240 000 litres of fuel carries 416 passengers about 8 800 miles (14 200 km). And fuel's calorific value is 10 kWh per litre. (We learned that in Chapter 3.) So the energy cost of one full-distance round-trip on such a plane, if divided equally among the passengers, is

$$\frac{2\times240\,000\,litre}{416\,passengers}\times10\,kWh/litre\simeq12\,000\,kWh$$
 per passenger.

If you make one such trip per year, then your average energy consumption per day is

$$\frac{12000 \,\text{kWh}}{365 \,\text{days}} = 33 \,\text{kWh/day}.$$

14200 km is a little further than London to Cape Town ($10\,000\,\mathrm{km}$) and London to Los Angeles ($9000\,\mathrm{km}$), so I think we've slightly overestimated the distance of a typical long-range intercontinental trip; but we've also overestimated the fullness of the plane, and the energy cost per person is more if the plane's not full. Scaling down by $10\,000\,\mathrm{km}/14\,200\,\mathrm{km}$ to get an estimate for Cape Town, then up again by 100/80 to allow for the plane's being 80% full, we arrive at $29\,\mathrm{kWh}$ per day. For ease of memorization, I'll round this up to $30\,\mathrm{kWh}$ per day.

Let's make clear what this means. Flying once per year has an energy cost slightly bigger than leaving a 1 kW electric fire on, non-stop, 24 hours a day, all year.

Just as Chapter 3, in which we estimated consumption by cars, was accompanied by Chapter A, offering a model of where the energy goes in cars, this chapter's technical partner, Chapter C (p289), discusses where the energy goes in planes. Chapter C allows us to answer questions such as "would air travel consume significantly less energy if we travelled in slower planes?" (The answer is **no**: in contrast to wheeled vehicles, which can get more efficient the slower they go, planes are already almost as energy-efficient as they could possibly be. Planes unavoidably have to use energy for two reasons: they have to throw air down in order to stay up, and they need energy to overcome air resistance. No redesign of a plane is going to radically improve its efficiency. A 10% improvement? Yes, possible. A doubling of efficiency? I'd eat my complimentary socks.)

Queries

Aren't turboprop aircraft far more energy-efficient?

No. The "comfortably greener" Bombardier Q400 NextGen, "the most technologically advanced turboprop in the world", according to its manu-



Jet flights: 30 kWh/d

Car: **40 kWh/d**

Wind: **20 kWh/d**

Figure 5.1. Taking one intercontinental trip per year uses about 30 kWh per day.



Figure 5.2. Bombardier Q400 NextGen. www.q400.com.

facturers [www.q400.com], uses 3.81 litres per 100 passenger-km (at a cruise speed of 667 km/h), which is an energy cost of 38 kWh per 100 p-km. The full 747 has an energy cost of 42 kWh per 100 p-km. So both planes are twice as fuel-efficient as a single-occupancy car.

Is flying extra-bad for climate change in some way?

Yes, that's the experts' view, though uncertainty remains about this topic. (See [3fbufz].) Flying creates other greenhouse gases in addition to CO₂, such as ozone, and indirect greenhouse gases, such as nitrous oxides. If you want to estimate your carbon footprint in tons of CO₂-equivalent, then you should take the actual CO₂ emissions of your flights and bump them up two- or three-fold. This book's diagrams don't include that multiplier because here we are focusing on our *energy* balance sheet.

The best thing we can do with environmentalists is shoot them.

Michael O'Leary, CEO of Ryanair [3asmgy]

Notes and further reading

page no.

37 Boeing 747-400 facts are from [9ehws].

Planes today are not completely full. Airlines are proud if their average fullness is 80%. Easyjet planes are 85% full on average. (Source: thelondonpaper Tuesday 16th January 2007.) An 80%-full 747 uses about 53 kWh per 100 passenger-km.

What about short-haul flights? In 2007, Ryanair, "Europe's greenest airline," delivered transportation at a cost of 37 kWh per 100 p-km [3exmgv]. This means that flying across Europe with Ryanair has much the same energy cost as having all the passengers drive to their destination in cars, two to a car. For an indication of what other airlines might be delivering, Ryanair's fuel burn rate in 2000, before their environment-friendly investments, was above 73 kWh per 100 p-km. London to Rome is 1430 km; London to Malaga is 1735 km. So a round-trip to Rome with the greenest airline has an energy cost of 1050 kWh, and a round-trip to Malaga costs 1270 kWh. If you pop over to Rome and to Malaga once per year, your average power consumption is 6.3 kWh/d with the greenest airline, and perhaps 12 kWh/d with a less green.

What about frequent flyers? To get a silver frequent flyer card from an intercontinental airline, it seems one must fly around 25 000 miles per year in economy class. That's about 60 kWh per day, if we scale up the opening numbers from this chapter and assume planes are 80% full.

Some additional figures from the International Panel on Climate Change [yrnmum]: A full 747-400 travelling 10 000 km with low-density seating (262 seats) has an energy consumption of 50 kWh per 100 p-km. In a high-density seating configuration (568 seats) and travelling 4000 km, the same plane has an energy consumption of 22 kWh per 100 p-km. A shorthaul Tupolev-154 travelling 2235 km with 70% of its 164 seats occupied consumes 80 kWh per 100 p-km.

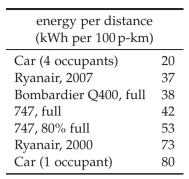


Table 5.3. Passenger transport efficiencies, expressed as energy required per 100 passenger-km.



Figure 5.4. Ryanair Boeing 737-800. Photograph by Adrian Pingstone.

5 — *Planes* 39

No redesign of a plane is going to radically improve its efficiency. Actually, the Advisory Council for Aerospace Research in Europe (ACARE) target is for an overall 50% reduction in fuel burned per passenger-km by 2020 (relative to a 2000 baseline), with 15–20% improvement expected in engine efficiency. As of 2006, Rolls Royce are half way to this engine target [36w5gz].

Dennis Bushnell, chief scientist at NASA's Langley Research Centre, seems to agree with my overall assessment of prospects for efficiency improvements in aviation. The aviation industry is mature. "There is not much left to gain except by the glacial accretion of a per cent here and there over long time periods." (New Scientist, 24 February 2007, page 33.) The radically reshaped "silent aircraft" SAX-40 [silentaircraft.org/sax40], if it were built, is predicted to be 16% more efficient than a conventional-shaped plane [Nickol, 2008].

Frequent
flyer:
60 kWh/d

Short hauls: 6 kWh/d

Figure 5.5. Two short-haul trips on the greenest short-haul airline: 6.3 kWh/d. Flying enough to qualify for silver frequent flyer status: 60 kWh/d.

6 Solar

We are estimating how our consumption stacks up against conceivable sustainable production. In the last three chapters we found car-driving and plane-flying to be bigger than the plausible on-shore wind-power potential of the United Kingdom. Could solar power put production back in the lead?

The power of raw sunshine at midday on a cloudless day is 1000 W per square metre. That's 1000 W per m² of area oriented towards the sun, not per m² of land area. To get the power per m² of land area in Britain, we must make several corrections. We need to compensate for the tilt between the sun and the land, which reduces the intensity of midday sun to about 60% of its value at the equator (figure 6.1). We also lose out because it is not midday all the time. On a cloud-free day in March or September, the ratio of the *average* intensity to the midday intensity is about 32%. Finally, we lose power because of cloud cover. In a typical UK location the sun shines during just 34% of daylight hours.

The combined effect of these three factors and the additional complication of the wobble of the seasons is that the average raw power of sunshine per square metre of south-facing roof in Britain is roughly $110\,\mathrm{W/m^2}$, and the average raw power of sunshine per square metre of flat ground is roughly $100\,\mathrm{W/m^2}$.

We can turn this raw power into useful power in four ways:

- 1. Solar thermal: using the sunshine for direct heating of buildings or water.
- 2. Solar photovoltaic: generating electricity.
- 3. Solar biomass: using trees, bacteria, algae, corn, soy beans, or oilseed to make energy fuels, chemicals, or building materials.
- 4. Food: the same as solar biomass, except we shovel the plants into humans or other animals.

(In a later chapter we'll also visit a couple of other solar power techniques appropriate for use in deserts.)

Let's make quick rough estimates of the maximum plausible powers each of these routes could deliver. We'll neglect their economic costs, and the energy costs of manufacturing and maintaining the power facilities.

Solar thermal

The simplest solar power technology is a panel making hot water. Let's imagine we cover *all* south-facing roofs with solar thermal panels –that would be about 10 m² of panels per person – and let's assume these are

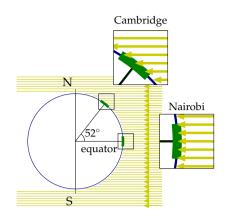


Figure 6.1. Sunlight hitting the earth at midday on a spring or autumn day. The density of sunlight per unit land area in Cambridge (latitude 52°) is about 60% of that at the equator.

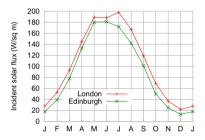


Figure 6.2. Average solar intensity in London and Edinburgh as a function of time of year. The average intensity, per unit land area, is 100 W/m².

6 — Solar 41



50%-efficient at turning the sunlight's $110\,\mathrm{W/m^2}$ into hot water (figure 6.3). Multiplying

 $50\% \times 10 \,\mathrm{m}^2 \times 110 \,\mathrm{W/m}^2$

we find solar heating could deliver

13 kWh per day per person.

I colour this production box white to indicate that it describes production of low-grade energy – hot water is not as valuable as the high-grade electrical energy that wind turbines produce. Heat can't be exported to the electricity grid. If you don't need it, if it's too much, it's wasted. We should bear in mind that much of this captured heat would not be in the right place. In cities, where many people live, residential accommodation has less roof area per person than the national average. Furthermore, this power would be delivered non-uniformly through the year.

Solar photovoltaic

Photovoltaic (PV) panels convert sunlight into electricity. Typical solar panels have an efficiency of about 10%; expensive ones perform at 20%. (Fundamental physical laws limit the efficiency of photovoltaic systems to at best 60% with perfect concentrating mirrors or lenses, and 45% without concentration. A mass-produced device with efficiency greater than 30% would be quite remarkable.) The average power delivered by south-facing 20%-efficient photovoltaic panels in Britain would be

$$20\% \times 110 \,\text{W/m}^2 = 22 \,\text{W/m}^2$$
.

Let's give every person $10\,\mathrm{m}^2$ of expensive (20%-efficient) solar panels and cover all south-facing roofs. These will deliver

5 kWh per day per person.

Since the area of all south-facing roofs is $10\,\mathrm{m}^2$ per person, there's certainly not space on our roofs for these photovoltaic panels as well as the

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

Figure 6.3. Solar power generated by a 3 m² panel (green), and supplementary heat required (blue) to make hot water in the test house of Viridian Solar. (The photograph shows a house with the same model of panel on its roof.) The average solar power from 3 m² was 3.8 kWh/d. The experiment simulated the hot-water consumption of an average European household – 100 litres of hot (60 °C) water per day. The 1.5-2 kWh/d gap between the total heat generated (black line, top) and the hot water used (blue line) is caused by heat-loss. The magenta line shows the electrical power required to run the solar system. The average power density of these solar panels is 53 W/m^2 .

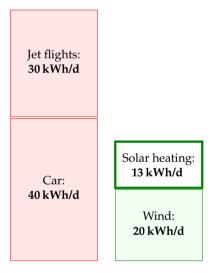


Figure 6.4. Solar thermal: a 10 m² array of thermal panels can deliver (on average) about 13 kWh per day of thermal energy.

solar thermal panels of the last section. So we have to choose whether to have the photovoltaic contribution or the solar hot water contribution. But I'll just plop both these on the production stack anyway. Incidentally, the present cost of installing such photovoltaic panels is about four times the cost of installing solar thermal panels, but they deliver only half as much energy, albeit high-grade energy (electricity). So I'd advise a family thinking of going solar to investigate the solar thermal option first. The smartest solution, at least in sunny countries, is to make combined systems that deliver both electricity and hot water from a single installation. This is the approach pioneered by Heliodynamics, who reduce the overall cost of their systems by surrounding small high-grade gallium arsenide photovoltaic units with arrays of slowly-moving flat mirrors; the mirrors focus the sunlight onto the photovoltaic units, which deliver electricity and hot water.

The conclusion so far: covering your south-facing roof at home with photovoltaics may provide enough juice to cover quite a big chunk of your personal average electricity consumption; but it doesn't look like roofs are big enough to really make a huge dent in our total *energy* consumption. To do more with PV, we need to step down to terra firma. The solar warriors in figure 6.6 show the way.



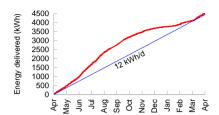




Figure 6.5. Solar photovoltaics: data from a 25-m² array in Cambridgeshire in 2006. The peak power delivered by this array is about 4 kW. The average, year-round, is 12 kWh per day. That's 20 W per square metre of panel.

Figure 6.6. Two solar warriors enjoying their photovoltaic system, which powers their electric cars and home. The array of 120 panels (300 W each, $2.2 \,\mathrm{m}^2$ each) has an area of $268 \,\mathrm{m}^2$, a peak output (allowing for losses in DC–to–AC conversion) of $30.5 \,\mathrm{kW}$, and an average output – in California, near Santa Cruz – of $5 \,\mathrm{kW}$ (19 W/m²). Photo kindly provided by Kenneth Adelman.

www.solarwarrior.com

Fantasy time: solar farming

If a miracle of solar technology occurs and the cost of photovoltaics came down enough that we could deploy panels all over the countryside, what is the maximum conceivable production? Well, if we covered 5% of the UK with 10%-efficient panels, we'd have

$$10\% \times 100 \,\text{W/m}^2 \times 200 \,\text{m}^2 \,\text{per person}$$

 $\simeq 50 \,\text{kWh/day/person}.$

I assumed only 10%-efficient panels, by the way, because I imagine that solar panels would be mass-produced on such a scale only if they were very cheap, and it's the lower-efficiency panels that will get cheap first. The power density of such a solar farm would be

$$10\% \times 100 \,\text{W/m}^2 = 10 \,\text{W/m}^2$$
.

This power density is twice that of the Bavaria Solarpark (figure 6.7).

Could this flood of solar panels co-exist with the army of windmills we imagined in chapter 4? Yes, no problem: windmills cast little shadow, and ground-level solar panels have negligible effect on the wind. How audacious is this plan? Well, the solar power capacity required to deliver this 50 kWh/d per person in the UK is more than one hundred times all the photovoltaics in the whole world. So should I include the PV farm in my sustainable production stack? I'm in two minds. At the start of the book I said I wanted to explore what the laws of physics say about the limits of sustainable energy, assuming money is no object. On those grounds, I should certainly go ahead, industrialize the countryside, and push the PV farm onto the stack. At the same time, I want to make helpful comments for today's society, to help people figure out what we should be doing between now and 2050. And today, electricity from solar farms would be four times as expensive as the market rate. So it feels a bit irresponsible to include this estimate in our total conceivable sustainable production – paving 5% of this country with solar panels seems beyond the bounds of plausibility in so many ways. If we seriously contemplated doing such a thing, it would quite likely be better to put the panels in a two-fold sunnier country and send some of the energy home by power lines. We'll return to this idea in chapter 25.

Mythconceptions

"The energy required to make a solar panel is much bigger than the energy it'll deliver."

False. The energy yield ratio (the ratio of energy delivered by a system over its lifetime, to the energy required to make it) of a roof-mounted, grid-connected solar system in Central Northern Europe is 4, for a system



Figure 6.7. Solar photovoltaic farms: The 6.3 MW (peak) Solarpark in Mühlhausen, Bavaria. Its average power per unit land area is expected to be about $5 \, \text{W/m}^2$. Photo by SunPower.

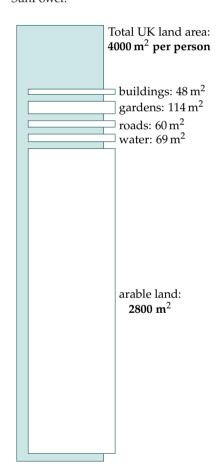


Figure 6.8. Land areas per person in Britain.

with a lifetime of 20 years [Richards and Watt, 2007]; and more than 7 in a sunnier spot such as Australia. (An energy yield ratio bigger than one means that a system was A Good Thing, energy-wise.) Wind turbines with a lifetime of 20 years have an energy yield ratio of 80.

Aren't photovoltaic panels going to get more and more efficient as technology improves?

I am sure that photovoltaic panels will become *cheaper*; I'm also sure that solar panels will become less energy-intensive to *manufacture*, so their energy yield ratio will improve. But this chapter's photovoltaic estimates didn't involve the economic cost of the panels, nor the energy cost of their manufacture. This chapter was concerned with the maximum conceivable power delivered. Photovoltaic panels with 20% efficiency are already close to the theoretical limit (see this chapter's endnotes). I'll be surprised if this chapter's estimate for roof-based photovoltaics ever needs a significant upward revision.

Solar biomass

All of a sudden, you know, we may be in the energy business by being able to grow grass on the ranch! And have it harvested and converted into energy. That's what's close to happening.

George W. Bush, February 2006

All available bioenergy solutions involve first growing green stuff, and then doing something with the green stuff. How big could the energy collected by the green stuff possibly be? There are four main routes to get energy from solar-powered biological systems:

- 1. We can grow specially-chosen plants and burn them in a power station which produces electricity or heat or both. We'll call this "coal substitution."
- 2. We can grow specially-chosen plants (oil-seed rape, sugar cane, or corn, say), turn them into ethanol or biodiesel, and shove that into cars, trains, planes or other places where such chemicals are useful. Or we might cultivate genetically-engineered bacteria, cyanobacteria, or algae that directly produce hydrogen, ethanol, or butanol, or even electricity. We'll call all such approaches "petroleum substitution."
- 3. We can take by-products from other agricultural activities and burn them in a power station. The by-products might range from straw (a by-product of Weetabix) to chicken poo (a by-product of McNuggets). Burning by-products is coal substitution again, but using ordinary plants, not the best high-energy plants. A power station that burns agricultural by-products won't deliver as much power per unit area

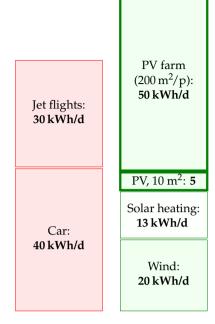


Figure 6.9. Solar photovoltaic: a 10 m² array of building-mounted south-facing panels with 20% efficiency can deliver about 5 kWh per day of electrical energy. If 5% of the country were coated with 10%-efficient solar panels (200 m² of panels per person) they would deliver 50 kWh/day/person.

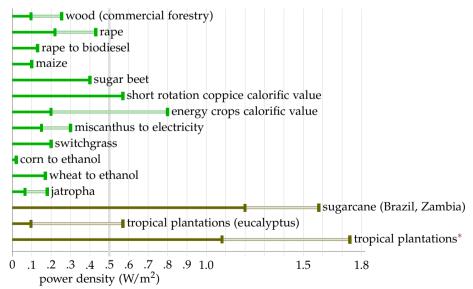
[©] David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

of farmland as an optimized biomass-growing facility, but it has the advantage that it doesn't monopolize the land. Burning methane gas from landfill sites is a similar way of getting energy, but it's sustainable only as long as we have a sustainable source of junk to keep putting into the landfill sites. (Most of the landfill methane comes from wasted food, I'm told.) Incinerating household waste is another slightly less roundabout way of getting power from solar biomass.

4. We can grow plants and feed them directly to energy-requiring humans or other animals.

For all of these processes, the first staging post for the energy is in a chemical molecule such as a carbohydrate in a green plant. We can therefore estimate the power obtainable from any and all of these processes by estimating how much power could pass through that first staging post. All the subsequent steps involving tractors, animals, chemical facilities, land-fill sites, or power stations can only lose energy. So the power at the first staging post is an upper bound on the power available from all plant-based power solutions.

So, let's simply estimate the power at the first staging post. In chapter D, we'll go into more detail, estimating the maximum contribution of each process. The average harvestable power of sunlight in Britain is $100\,\mathrm{W/m^2}$. The most efficient plants in Europe are about 2% efficient at turning solar energy into carbohydrates, which would suggest that plants might deliver $2\,\mathrm{W/m^2}$; however, efficiency drops at higher light levels, and the best performance of any energy crops in Europe is closer to $0.5\,\mathrm{W/m^2}$. Let's cover 75% of the country with quality green stuff. That's $3000\,\mathrm{m^2}$ per person devoted to bio-energy. This is the same as the British land area currently



45

Figure 6.10. Some *Miscanthus* grass enjoying the company of Dr. Emily Heaton, who is 5'4" tall (163 cm). In the USA, *Miscanthus* grown without nitrogen fertilizer yields about 24t/ha/y of dry matter. In Britain, yields of 12–16t/ha/y are reported. Dry *Miscanthus* has a net calorific value of 17 MJ/kg, so the British yield corresponds to a power density of 0.75 W/m². Photo provided by the University of Illinois.

Figure 6.11. Power densities achieved by various plants. For sources, see the end-notes. These power densities vary depending on irrigation and fertilization; ranges are indicated for some crops, for example wood has a range from 0.095–0.254 W/m². The bottom three power densities are for crops grown in tropical locations. The last power density (tropical plantations*) assumes genetic modification, fertilizer application, and irrigation. In the text, I use 0.5 W/m² as a summary figure for the best energy crops in NW Europe.

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

Biomass: food.

biofuel, wood,

devoted to agriculture. So the maximum energy available, ignoring all the additional costs of growing, harvesting, and processing the greenery, is

 $0.5\,\text{W/m}^2\,\times\,3000\,\text{m}^2\;\text{per person}$

- = 1500 W per person
- = 36 kWh/d per person.

Wow. That's not very much, considering the outrageously generous assumptions we just made, to try to get a big number. If you wanted to get biofuels for cars or planes from the greenery, all the other steps in the chain from farm to sparkplug would inevitably be inefficient. I think it'd be optimistic to hope that the overall losses along the processing chain would be as small as 33%. Even burning dried wood in a good wood boiler loses 20% of the heat up the chimney. So surely the true potential power from biomass and biofuels cannot be any bigger than $24 \, \text{kWh/d}$ per person. And don't forget, we want to use some of the greenery to make food for us and for our animal companions.

Could genetic engineering produce plants that convert sunlight to chemicals more efficiently? It's conceivable; but I haven't found any scientific publication predicting that plants in Europe could achieve net power production beyond 1 W/m².

I'll pop 24 kWh/d per person onto the green stack, emphasizing that I think this number is an over-estimate – I think the true maximum power that we could get from biomass will be smaller because of the losses in farming and processing.

I think one conclusion is clear: *biofuels can't add up* – at least, not in countries like Britain, and not as a replacement for all transport fuels. Even leaving aside biofuels' main defects – that their production competes with food, and that the additional inputs required for farming and processing often cancel out most of the delivered energy (figure 6.13) – biofuels made from plants, in a European country like Britain, can deliver so little power, I think they are scarcely worth talking about.

What about algae?

Algae are just plants, so everything I've said so far applies to algae. Slimy underwater plants are no more efficient at photosynthesis than their terrestrial cousins. But there is one trick that I haven't discussed, which is standard practice in the algae-to-biodiesel community: they grow their algae in water heavily enriched with carbon dioxide, which might be collected at power stations or other industrial facilities. It takes much less effort for plants to photosynthesize if the carbon dioxide has already been concentrated. In a sunny spot in America, in ponds fed with concentrated $\rm CO_2$ (concentrated to 10%), algae can grow at 30 grams per square metre per day producing 0.01 litres of biodiesel per square metre per day. This corresponds to a power per unit pond area of $4 \, \rm W/m^2$ – similar to the Bavaria

Waste incin'n, landfill gas: 24 kWh/d

PV farm (200 m²/p): 50 kWh/d

PV, 10 m²: 5

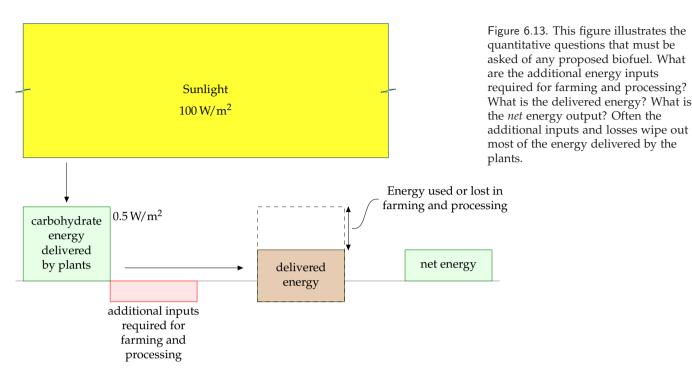
Solar heating: 13 kWh/d

Wind: 20 kWh/d

Figure 6.12. Solar biomass, including all forms of biofuel, waste incineration, and food: 24 kWh/d per person.

[©] David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

6 — Solar 47



photovoltaic farm. If you wanted to drive a typical car (doing 12 km per litre) a distance of 50 km per day, then you'd need 420 square metres of algae-ponds just to power your car; for comparison, the area of the UK per person is 4000 square metres, of which 69 m² is water. Please don't forget that it's essential to feed these ponds with concentrated carbon dioxide. So this technology would be limited both by land area – how much of the UK could we turn into algal ponds? - and by the availability of concentrated CO₂, the capture of which would have an energy cost (a topic we'll come back to later). Let's check the limit imposed by the concentrated CO₂. To grow 30 grams of algae per square metre per day would require at least 60 grams of CO₂ per square metre per day. If all the CO₂ from all UK power stations were captured (roughly $2^{1/2}$ tons per year per person), it could service 230 square metres per person of the algal ponds described above – roughly 6% of the country. This area would deliver biodiesel with a power of 24kWh per day per person, assuming that the numbers for sunny America apply here. A plausible vision? Perhaps on one tenth of that scale? I'll leave it to you to decide.

What about algae in the sea?

Remember what I just said: the algae-to-biodiesel posse always feed their algae concentrated CO_2 . If you're going out to sea, presumably pumping CO_2 into it won't be an option. And without the concentrated CO_2 , the

Land use	area per person (m ²)	percentage
 domestic buildings 	30	1.1
 domestic gardens 	114	4.3
 non-domestic buildings 	18	0.66
– roads	60	2.2
– railways	3.6	0.13
– paths	2.9	0.11
greenspace	2335	87.5
– water	69	2.6
- other land uses	37	1.4
Total	2670	100

Table 6.14. Land areas, in England, devoted to different uses. Source: Generalized Land Use Database Statistics for England 2005. [3b7zdf]

productivity of algae drops one hundred fold. For algae in the sea to make a difference, a country-sized harvesting area in the sea would be required.

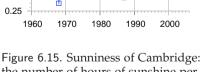
What about algae that produce hydrogen?

Trying to get slime to produce hydrogen in sunlight is a smart idea because it cuts out a load of chemical steps normally performed by carbohydrate-producing plants. Every chemical step reduces efficiency a little. Hydrogen can be produced directly by the photosynthetic system, right at step one. A research study from the National Renewable Energy Laboratory in Colorado predicted that a reactor filled with genetically modified green algae, covering an area of 11 hectares in the Arizona desert, could produce 300 kg per day of hydrogen. Hydrogen contains 39 kWh per kg, so this algae-to-hydrogen facility would deliver a power per unit area of $4.4\,\mathrm{W/m^2}$. Taking into account the estimated electricity required to run the facility, the net power delivered would be reduced to $3.6\,\mathrm{W/m^2}$. That strikes me as still quite a promising number.

Notes and further reading

page no.

- 40 compensate for the tilt between the sun and the land. The latitude of Cambridge is $\theta = 52^{\circ}$; the intensity of midday sunlight is multiplied by $\cos \theta \simeq 0.6$. The precise factor depends on the time of year, and varies between $\cos(\theta + 23) = 0.26$ and $\cos(\theta 23) = 0.87$.
- In a typical UK location the sun shines during one third of daylight hours. The Highlands get 1100 h sunshine per year a sunniness of 25%. The best spots in Scotland get 1400 h per year 32%. Cambridge: 1500 ± 130 h per year 34%. South coast of England (the sunniest part of the UK):



0.45

0.35

0.3

Figure 6.15. Sunniness of Cambridge: the number of hours of sunshine per year, expressed as a fraction of the total number of daylight hours.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

1700 h per year – 39%. [2rqloc] Cambridge data from [2szckw]. See also table 30.1.

- 40 The average raw power of sunshine per square metre of south-facing roof in Britain is roughly 110 W/m², and of flat ground, roughly 100 W/m². Source: NASA "Surface meteorology and Solar Energy" http://eosweb.larc.nasa.gov/, [5hrxls]. Surprised that there's so little difference between a tilted roof facing south and a horizontal roof? I was. The difference really is just 10% [6z9epq].
- that would be about 10 m² of panels per person. I estimated the area of south-facing roof per person by taking the area of land covered by buildings per person (48 m² in England table 6.14), multiplying by 1/4 to get the south-facing fraction, and bumping the area up by 40% to allow for roof tilt. This gives 16 m² per person. Panels usually come in inconvenient rectangles so some fraction of roof will be left showing; hence 10 m² of panels.

41 The average power delivered by photovoltaic panels...

There's a myth going around that states that solar panels produce almost as much power in cloudy conditions as in sunshine. This is simply not true. On a bright but cloudy day, solar photovoltaic panels and plants do continue to convert some energy, but much less: photovoltaic production falls roughly ten-fold when the sun goes behind clouds. As figure 6.17 shows, the power delivered by photovoltaic panels is almost exactly proportional to the intensity of the sunlight – at least, if the panels are at 25 °C. To complicate things, the power delivered depends on temperature too - hotter panels have reduced power (typically 0.38% loss in power per °C) - but if you check data from real panels, e.g. at www.solarwarrior.com, you can confirm the main point: output on a cloudy day is far less than on a sunny day. This issue is obfuscated by some solar-panel promoters who discuss how the "efficiency" varies with sunlight. "The panels are more efficient in cloudy conditions," they say; this may be true, but efficiency should not be confused with delivered power.

- 43 solar farming numbers from Serpa Solar Power Plant, Portugal (PV): "The world's most powerful solar power plant." [39z5m5] [2uk8q8] Its sun-tracking panels occupy 60 hectares, i.e. 600 000 m² or 0.6 km², and are expected to generate 20 GWh per year, i.e., 2.3 MW on average. That's a power density of 3.8 W/m².
- 41 Typical solar panels have an efficiency of about 10%; expensive ones perform at 20%. See figure 6.18. Sources: Turkenburg [2000], Sunpower www.sunpowercorp.com, Sanyo http://www.sanyo-solar.eu/, Suntech.
- A device with efficiency greater than 30% would be quite remarkable. This is a quote from Hopfield and Gollub [1978], who were writing about panels without concentrating mirrors or lenses. The theoretical limit for a standard "single-junction" solar panel without concentrators, the Shockley-Queisser limit, says that at most 31% of the energy in sunlight can be converted to electricity [Shockley and Queisser, 1961]. (The main

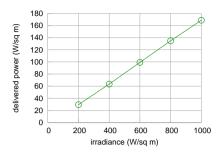


Figure 6.17. Power produced by the Sanyo HIP-210NKHE1 module as a function of light intensity (at 25 °C, assuming an output voltage of 40 V). Source: datasheet, http://www.sanyo-solar.eu/.

amorphous silicon

multi-crystalline silicon
single crystal silicon
Sunpower WHT
Sanyo HIP
Suntech poly-crystalline
thin-film triple junction

10% 20% 30% 40% 50%
efficiency

Figure 6.18. Efficiencies of solar photovoltaic modules available for sale today. In the text I assume that roof-top photovoltaics are 20% efficient, and that country-covering photovoltaics would be 10% efficient. In a location where the average power density of incoming sunlight is 100 W/m², 20%-efficient panels deliver 20 W/m².

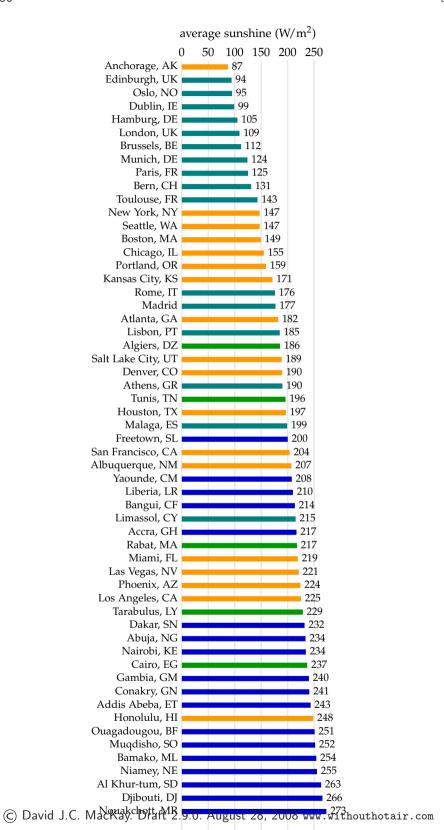
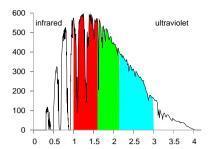
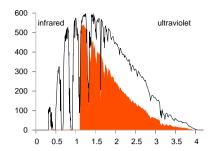


Figure 6.16. Average power of sunshine falling on a horizontal surface in selected locations in Europe, North America, and Africa.



6 — Solar 51





reason for this limit is that a standard solar material has a property called its band-gap, which defines a particular energy of photon that that material converts most efficiently. Sunlight contains photons with many energies; photons with energy *below* the band-gap are not used at all; photons with energy *greater* than the band-gap may be captured, but all their energy in excess of the band-gap is lost.

Concentrators (lenses or mirrors) can both reduce the cost (per watt) of photovoltaic systems, and increase their efficiency. The Shockley–Queisser limit for solar panels with concentrators is 41% efficiency.

The only way to beat the Shockley–Queisser limit is to make fancy photo-voltaic devices that split the light into different wavelengths, processing each wavelength-range with its own personalized band-gap. These are called multiple-junction photo-voltaics. Recently multiple-junction photo-voltaics with optical concentrators have been reported to be about 40% efficient. [2t17t6] http://www.spectrolab.com/. In July 2007, the University of Delaware reported 42.8% efficiency with 20-times concentration [6hobq2], [21sx6t]. In August 2008, NREL reported 40.8% efficiency with 326-times concentration [62ccou]. Strangely, both these results were called world efficiency records. What multiple-junction devices are available on the market? Uni-solar sell a thin-film triple-junction 58 W(peak) panel with an area of 1 m². That implies an efficiency, in full sunlight, of only 5.8%.

- 42 Figure 6.5: Solar PV data. Data and photograph kindly provided by Jonathan Kimmitt.
- Heliodynamics http://www.hdsolar.com/. See figure 6.20.
 A similar system is made by Arontis http://www.arontis.se/.
- **The Solarpark in Muhlhausen, Bavaria.** On average this 25-hectare farm is expected to deliver 0.7 MW (17 000 kWh per day).

New York's Stillwell Avenue subway station has integrated amorphous silicon thin-film photovoltaics in its roof canopy, delivering 4 W/m² [Fies et al., 2007].

The Nellis solar power plant in Nevada was completed in December, 2007, on 140 acres, and is expected to generate 30 GWh per year. That's 6 W/m^2 [5hzs5y].

 The solar power capacity required to deliver 50 kWh/d per person in the UK is more than one hundred times all the photovoltaics in the whole Figure 6.19. Part of Shockley and Queisser's explanation for the 31% limit of the efficiency of simple photovoltaics.

Left: the spectrum of midday sunlight. The horizontal axis shows photon energy in eV. The vertical axis shows the power density in watts per square metre per eV of spectral interval. The visible part of the spectrum is indicated by the coloured section.

Right: the energy captured by a photovoltaic device with a single band-gap at 1.1 eV is shown by the tomato-shaded area. Photons with energy less than the band-gap are lost. Some of the energy of photons above the band-gap is lost; for example half of the energy of every 2.2 eV photon is lost.

Further losses are incurred because of inevitable radiation from recombining charges in the photovoltaic material.

world. To deliver 50 kWh/d/p in the UK would require 125 GW average power, which requires 1250 GW of capacity. At the end of 2007, world installed photovoltaics amounted to 10 GW peak; the build rate is roughly 2 GW per year.

- 43 paving 5% of this country with solar panels seems beyond the bounds of plausibility. My main reason for feeling such a panelling of the country would be implausible is that Brits like using their countryside for farming and recreation rather than solar-panel-husbandry. Another concern might be price. This isn't a book about economics, but here are a few figures. Going by the price-tag of the Bavarian solar farm, to deliver 50 kWh/d per person would cost €91 000 per person; if that power station lasted 20 years without further expenditure, the wholesale cost of the electricity would be €0.25 per kWh. Further reading: David Carlson, BP solar [2ahecp].
- 45 *Figure 6.10. Miscanthus* data are from Heaton et al. [2004] and [6kqq77]. The estimated yield is obtained only after three years of undisturbed growing.
 - The most efficient plants are about 2% efficient; but the delivered power per unit area is about 0.5 W/m². Actually, at low light intensities, the best British plants are 2.4% efficient in well-fertilized fields [Monteith, 1977] but at higher light intensities, their conversion efficiency drops. According to Turkenburg [2000] and Schiermeier et al. [2008], the conversion efficiency of solar to biomass energy is less than 1%.

Here are a few sources to back up my estimate of $0.5 \, \text{W/m}^2$ for vegetable power in the UK. First, the Royal Commission on Environmental Pollution's estimate of the potential delivered power density from energy crops in Britain is $0.2 \, \text{W/m}^2$ [Royal Commission on Environmental Pollution, 2004]. Second, on page 43 of the Royal Society's biofuels document [Royal Society working group on biofuels, 2008], Miscanthus tops the list, delivering about $0.8 \, \text{W/m}^2$ of chemical energy. My figure of $0.5 \, \text{W/m}^2$ is the average of these two.

In the World Energy Assessment published by the UNDP, Rogner [2000] writes: "Assuming a 45% conversion efficiency to electricity and yields of 15 oven dry tons a hectare per year, $2\,\mathrm{km}^2$ of plantation would be needed per megawatt of electricity of installed capacity running 4,000 hours a year." That is a power density of $0.23\,\mathrm{W(e)/m^2}$. (1 W(e) means 1 watt of electrical power.)

Energy for Sustainable Development Ltd [2003] say that short-rotation coppices can deliver over 10 tons of dry wood per hectare per year, which corresponds to a power density of $0.57 \, \text{W/m}^2$. (Dry wood has a calorific value of $5 \, \text{kWh}$ per kg.)

According to Archer and Barber [2004] the instantaneous efficiency of a healthy leaf in optimal conditions can approach 5%, but the long-term energy-storage efficiency of modern crops is 0.5–1%. Archer and Barber [2004] suggest that by genetic modification, it might be possible to improve the storage efficiency of plants, especially C4 plants, which have already naturally evolved a more efficient photosynthetic pathway. C4 plants are mainly found in the tropics and thrive in high temperatures;



Figure 6.20. A combined-heat-and-power photovoltaic unit from Heliodynamics. A reflector area of 32 m² (a bit larger than the side of a double-decker bus) delivers up to 10 kW of heat and 1.5 kW of electrical power. In a sun-belt country, one of these one-ton devices could deliver about 60 kWh/d of heat and 9 kWh/d of electricity. These powers correspond to average fluxes of $80 \,\mathrm{W/m^2}$ of heat and $12 \,\mathrm{W/m^2}$ of electricity (that's per square metre of device surface); these fluxes are similar to the fluxes delivered by standard solar heating panels and solar photovoltaic panels, but Heliodynamics's concentrating design delivers power at a lower cost, because most of the material is simple flat glass.

they don't grow at temperatures below 10 °C. Some examples of C4 plants are sugarcane, maize, sorghum, finger millet, and switchgrass. Zhu et al. [2008] calculate that the theoretical limit for the conversion efficiency of solar energy to biomass is 4.6% for C3 photosynthesis at 30 °C and today's 380 ppm atmospheric CO₂ concentration, and 6% for C4 photosynthesis. They say that the highest solar energy conversion efficiencies reported for C3 and C4 crops are 2.4% and 3.7% respectively; and, citing Boyer [1982], that the average conversion efficiencies of major crops in the US are 3 or 4 times lower than those record efficiencies (that is, about 1% efficient). One reason that plants don't achieve the theoretical limit is that they have insufficient capacity to use all the incoming radiation of bright sunlight. Both these papers [Zhu et al., 2008, Boyer, 1982] discuss prospects for genetic engineering of more-efficient plants.

- 45 Figure 6.11. The numbers in this figure are drawn from Rogner [2000] (net energy yields of wood, rape, sugarcane, and tropical plantations); Bayer Crop Science [2003] (rape to biodiesel); Francis et al. [2005] and Asselbergs et al. [2006] (jatropha); Mabee et al. [2006] (sugarcane, Brazil); Schmer et al. [2008] (switchgrass, marginal cropland in USA); Shapouri et al. [1995] (corn to ethanol); Royal Commission on Environmental Pollution [2004]; Royal Society working group on biofuels [2008]; Energy for Sustainable Development Ltd [2003]; Archer and Barber [2004]; Boyer [1982]; Monteith [1977].
- 46 Even just setting fire to dried wood in a good wood boiler loses 20% of the heat up the chimney. Sources: Royal Society working group on biofuels [2008], Royal Commission on Environmental Pollution [2004]
- In America, in ponds fed with concentrated CO₂, algae can grow at 30 grams per square metre per day, producing 0.01 litres of biodiesel per square metre per day. Source: Putt [2007]. This calculation has ignored the energy cost of running the algae ponds and processing the algae into biodiesel. Putt [2007] describes the energy balance of a proposed design for a 100-acre algae farm, powered by methane from an animal litter digester. The farm described would in fact produce less power than the methane power input. The 100-acre farm would use 2600 kW of methane, which corresponds to an input power density of 6.4 W/m². To recap, the power density of the output, in the form of biodiesel, would be just 4.2 W/m². All proposals to make biofuels should be approached with a critical eye!
- 48 A research study from the National Renewable Energy Laboratory predicted that genetically modified green algae, covering an area of 11 hectares, could produce 300 kg per day of hydrogen. Source: Amos [2004].



7 Heating and cooling

We spend about one third of our energy on controlling the temperature of our surroundings – at home and at work – and on warming or cooling our food, drink, laundry, and dirty dishes.

Domestic water heating

The biggest use of hot water in a house might be baths, showers, dishwashing, or clothes-washing – it depends on your lifestyle. Let's estimate the energy used by taking a hot bath.

The volume of bathwater is $50\,\mathrm{cm} \times 15\,\mathrm{cm} \times 150\,\mathrm{cm} \simeq 110\,\mathrm{litre}$. Say the temperature of the bath is $50\,^\circ\mathrm{C}$ (120 F) and the water coming into the house is at $10\,^\circ\mathrm{C}$. The heat capacity of water, which measures how much energy is required to heat it up, is $4200\,\mathrm{J}$ per litre per $^\circ\mathrm{C}$. So the energy required to heat up the water by $40\,^\circ\mathrm{C}$ is

 $4200 \text{ J/litre/}^{\circ}\text{C} \times 110 \text{ litre} \times 40 \,^{\circ}\text{C} \simeq 18 \text{ MJ} \simeq 5 \text{ kWh}.$

So taking a bath uses about 5kWh. For comparison, taking a shower (25 litres) uses about 1kWh.

Kettles and cookers

Britain, being a civilized country, has a 230 volt domestic electricity supply. With this supply, we can use an electric kettle to boil several litres of water in a couple of minutes. Such kettles have a power of 3 kW. Why 3 kW? Because this is the biggest power that a 230 volt outlet can deliver without the current exceeding 13 amps. In countries where the voltage is 110 volts, it takes twice as long to make a pot of tea.

If a household has the kettle on for 20 minutes per day, that's an average power consumption of 1 kWh per day. (I'll work out the next few items "per household," with 2 people per household.)

One small ring on an electric cooker has the same power as a toaster: 1kW. The higher-power hot plates deliver 2.3kW. If you use two rings of the cooker on full power for half an hour per day, that corresponds to 1.6kWh per day.

A microwave oven usually has its cooking power marked on the front: mine says 900 W, but it actually *consumes* about 1.4 kW. If you use the microwave for 20 minutes per day, that's 0.5 kWh per day.

A regular oven guzzles more: about 3 kW when on full. If you use the oven for one hour per day, and the oven's on full power for half of that time, that's 1.5 kWh per day.



Figure 7.1. A flock of new houses, yesterday.

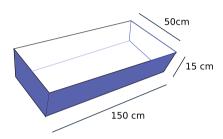


Figure 7.2. The water in a bath.

 $230 \text{ V} \times 13 \text{ A} = 3000 \text{ W}$

Microwave: 1400 W peak

Fridgefreezer: 100 W peak, 18 W average



Figure 7.3. Power consumption by a heating and a cooling device.

Device power time energy per day per day Cooking $\frac{1}{3}h$ 3kW - kettle 1kWh/d 1.4 kW $^{1/3}h$ $0.5 \, \text{kWh/d}$ - microwave $^{1/2}h$ 3.3 kW electric cooker (rings) $1.6 \, \text{kWh/d}$ $1/_{2} h$ - electric oven 3kW $1.5 \, \text{kWh/d}$ Cleaning - washing machine 2.5 kW 1 h $2.5 \, \text{kWh/d}$ - tumble dryer $2.5 \, kW$ 0.8 h2kWh/d - airing-cupboard drying $0.5 \, \text{kWh/d}$ - washing-line drying 0kWh/d - dishwasher $1.5 \, \text{kWh/d}$ 2.5 kW Cooling $0.5 \, \text{kWh/d}$ - refrigerator 0.02 kW 24 h freezer $0.09\,\mathrm{kW}$ 24 h $2.3 \, \text{kWh/d}$ 0.6 kW $0.6 \, \text{kWh/d}$ - air-conditioning 1 h

Table 7.4. Electrical consumption figures for heating and cooling devices, per household.

Hot clothes and hot dishes

A clothes washer, dishwasher, and tumble dryer all use a power of about 2.5 kW when running.

A clothes washer uses about 80 litres of water per load, with an energy cost of about 4 kWh. If we use an indoor airing-cupboard instead of a tumble dryer to dry clothes, heat is still required to evaporate the water – roughly 1.5 kWh to dry one load of clothes, instead of 3 kWh.

Totting up the estimates relating to hot water, I think it's easy to use about 12 kWh per day per person.

Hot air - at home and work

Now, does more power go into making hot water and hot food, or into making hot air via our buildings' radiators?

One way to estimate the energy used per day for hot air is to imagine a building heated instead by electric fires, whose powers are more familiar. The power of a small electric bar fire or electric fan heater is 1 kW (24 kWh per day). In winter, you might need one of these per person to keep toasty. In summer, none. So we estimate that on average one modern person *needs* to use 12 kWh per day on hot air. But most people use more than they need, keeping several rooms warm simultaneously (kitchen, living room, corridor, and bathroom, say). So a plausible consumption figure for hot air is about double that: 24 kWh per day per person.

This chapter's companion Chapter E contains a more detailed account of where the heat is going in a building; this model makes it possible to Hot water: 12 kWh/d

Figure 7.5. Hot water total – including bathing, showering, clothes washing, cookers, kettles, microwave oven, dishwashing – about 12 kWh per day per person. I've given this box a light colour to indicate that this power could be delivered by low-grade thermal energy.



Figure 7.6. A big electric heater: 2 kW.

predict the heat savings from turning the thermostat down, double-glazing the windows, and so forth.

Warming outdoors, and other luxuries

There's a growing trend of warming the outdoors with patio heaters. Typical patio heaters have a power of 15 kW. So if you use one of these for a couple of hours every evening, you are using an extra 30 kWh per day.

A more modest luxury is an electric blanket. An electric blanket for a double bed uses 140 W; switching it on for one hour uses 0.14 kWh.

Hot air: 24 kWh/d

Figure 7.7. Hot air total – including domestic and workplace heating – about 24 kWh per day per person.

Cooling

Fridge and freezer

We control the temperatures not only of the hot water and hot air with which we surround ourselves, but also of the cold cupboards we squeeze into our hothouses. My fridge-freezer, pictured in figure 7.3, consumes 18 W on average – that's roughly 0.5 kWh/d.

Air-conditioning

In countries where the temperature gets above 30 °C, air-conditioning is viewed as a necessity, and the energy cost of delivering that temperature control can be large. However, this part of the book is about British energy consumption, and Britain's temperatures provide little need for air-conditioning (figure 7.8).

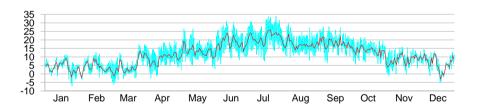


Figure 7.8. Cambridge temperature in degrees Celsius, daily (red line), and half-hourly (blue line) during 2006.

An economical way to get air-conditioning is an air-source heat pump. A window-mounted electric air-conditioning unit for a single room uses 0.6 kW of electricity and (by heat-exchanger) delivers 2.6 kW of cooling. To estimate how much energy someone might use in the UK, I assumed they might switch such an air-conditioning unit on for about 12 hours per day on 30 days of the year. On the days when it's on, the air-conditioner uses 7.2 kWh. The average consumption over the whole year is 0.6 kWh/d.

This chapter's estimate of the energy cost of cooling – 1kWh/d per person – includes this air-conditioning and a domestic refrigerator. Society

igure 7.9. Cooling total – inch

Figure 7.9. Cooling total – including a refrigerator (fridge/freezer) and a little summer air-conditioning – 1 kWh/d.

Cooling: 1kWh/d

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

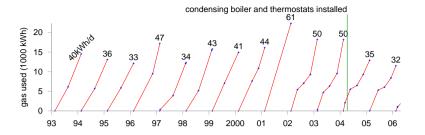


Figure 7.10. My domestic cumulative gas consumption, in kWh, each year from 1993 to 2005. The number at the top of each year's line is the average rate of energy consumption, in kWh per day. To find out what happened in 2007, keep reading!

also refrigerates food on its way from field to shopping basket. I'll estimate the power cost of the foodchain later in Chapter 15.

Total heating and cooling

Our rough estimate of the total energy that one person might spend on heating and cooling, including home, workplace, and cooking, is 37 kWh/d per person (12 for hot water, 24 for hot air, and 1 for cooling).

Evidence that this estimate is in the right ballpark, or perhaps a little on the low side, comes from my own domestic gas consumption, which for twelve years averaged 40 kWh per day (figure 7.10). At the time I thought I was a fairly frugal user of heating, but I wasn't being attentive to my actual power consumption. Chapter 21 will reveal how much power I saved once I started paying attention.

Since heating is a big item in our consumption stack, let's check my estimates against some national statistics. Nationally, the average *domestic* consumption for space heating, water, and cooking in the year 2000 was 21 kWh per day per person, and consumption in the *service sector* for heating, cooling, catering, and hot water was 8.5 kWh/d/p. For an estimate of workplace heating, let's take the gas consumption of the University of Cambridge, which was 16 kWh/d per employee in 2006–7.

Totting up these three numbers, a second guess for the national spend on heating is $21+8.5+16 \simeq 45\,\text{kWh/d}$ per person, if Cambridge University is a normal workplace. Good, that's reassuringly close to our first guess of $37\,\text{kWh/d}$.

Notes and further reading

page no.

54 An oven uses 3kW. Obviously there's a range of powers. http://www. 1stforkitchens.co.uk/kitchenovens.html Many have a maximum power of 1.8 kW or 2.2 kW. Top-of-the-line ovens use as much as 6 kW. For example, the Whirlpool AGB 487/WP 4 Hotplate Electric Oven Range has a 5.9 kW oven, and four 2.3 kW hotplates. http://www.kcmltd.com/electric_oven_ranges.shtml

Biomass: food, biofuel, wood, waste incin'n, landfill gas: Heating, 24 kWh/d cooling: 37 kWh/d PV farm $(200 \,\mathrm{m}^2/\mathrm{p})$: 50 kWh/d Jet flights: 30 kWh/d PV, 10 m²: 5 Solar heating: 13 kWh/d Car: 40 kWh/d Wind: 20 kWh/d

Figure 7.11. Heating and cooling – about 37 units per day per person. I've removed the shading from this box to indicate that it represents power that could be delivered by low-grade thermal energy.

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

- 55 An airing cupboard requires roughly 1.5 kWh to dry one load of clothes. I worked this out by weighing my laundry: a load of clothes, 4 kg when dry, emerged from my Bosch washing machine weighing 2.2 kg more (even after a good German spinning). The latent heat of vaporization of water at 15 °C is roughly 2500 kJ/kg. To obtain the daily figure in the table I assumed that one person has a load of laundry every three days, and that this sucks valuable heat from the house during the cold half of the year. (In summer, using the airing cupboard delivers a little bit of air-conditioning.)
- 57 Nationally, the average domestic consumption was 21 kWh/d/p; consumption in the service sector was 8.5 kWh/d/p. Source: Department of Trade and Industry [2002a].
- In 2006–7, Cambridge University's gas consumption was 16 kWh/d per employee. The gas and oil consumption of the University of Cambridge (not including the Colleges) was 76 GWh in 2006–7. I declared the University to be the place of work of 13 300 people (8602 staff and 4667 postgraduate researchers). Its electricity consumption, incidentally, was 99.5 GWh. Source: University utilities report.

8 Hydroelectricity

To make hydroelectric power, you need altitude, and you need rainfall. Let's estimate the total energy of all the rain as it runs down to sea-level.

For this hydroelectric forecast, I'll divide Britain into two: the lower, dryer bits, which I'll call "the lowlands"; and the higher, wetter bits, which I'll call "the highlands." I'll choose Bedford and Kinlochewe as my representatives of these two regions.

Let's do the lowlands first. To estimate the gravitational power of lowland rain, we multiply the rainfall in Bedford ($584\,\mathrm{mm}$ per year) by the density of water ($1000\,\mathrm{kg/m^3}$), the strength of gravity ($10\,\mathrm{m/s^2}$) and the typical lowland altitude above the sea (say $100\,\mathrm{m}$). The power density works out to $0.02\,\mathrm{W/m^2}$. That's the power per unit area of land on which rain falls

When we multiply this by the area per person (2700 m², if the lowlands are equally shared between all 60 million Brits), we find an average raw power of about 1 kWh per day per person. This is the absolute upper limit for lowland hydroelectric power, if every river were dammed and every drop perfectly exploited. Realistically, we will only ever dam rivers with substantial height drops, with catchment areas much smaller than the whole country. Much of the water evaporates before it gets anywhere near a turbine, and no hydroelectric system exploits the full potential energy of the water. We thus arrive at a firm conclusion about lowland water power. People may enjoy making "run-of-the-river" hydro and other small-scale hydroelectric schemes, but such lowland facilities can never deliver more than 1 kWh per day per person.

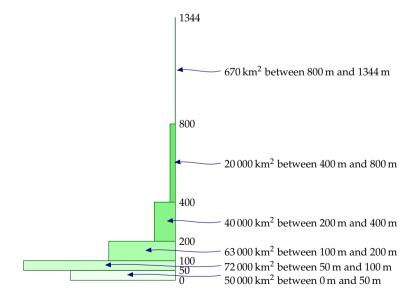




Figure 8.1. Nant-y-Moch dam, part of a 55 MW hydroelectric scheme in Wales. Photo by Dave Newbould, www.origins-photography.co.uk.



Figure 8.2. Altitudes of land in Britain. The rectangles show how much land area there is at each height.

Heating,

cooling: 37 kWh/d

Jet flights:

30 kWh/d

Let's turn to the highlands. Kinlochewe is a rainier spot: it gets $2278 \,\mathrm{mm}$ per year, four times more than Bedford. The height drops there are bigger too – large areas of land are above $300 \,\mathrm{m}$. So overall a twelve-fold increase in power per square metre is plausible for mountainous regions. The raw power density is roughly $0.24 \,\mathrm{W/m^2}$. If the highlands generously share their hydro-power with the rest of the UK (at $1300 \,\mathrm{m^2}$ area per person), we find an upper limit of about $7 \,\mathrm{kWh}$ per day per person. As in the low-lands, this is the upper limit on raw power if evaporation were outlawed and every drop were perfectly exploited.

What should we estimate is the plausible practical limit? Let's guess 20% of this $-1.4\,\mathrm{kWh}$ per day, and round it up a little to allow for production in the lowlands: $1.5\,\mathrm{kWh}$ per day.

The actual power from hydroelectricity in the UK today is 0.2 kWh per day per person, so this 1.5 kWh/d/p would require a seven-fold increase in hydroelectric power.

Notes and further reading

page no.

- 60 The actual power from hydroelectricity in the UK today is 0.2 kWh per day per person. Source: MacLeay et al. [2007]. In 2006, large-scale hydro produced 3515 GWh (from plant with a capacity of 1.37 GW); small-scale hydro, 212 GWh (0.01 kWh/d/p) (from a capacity of 153 MW). Glendoe, the first new large-scale hydroelectric project in the UK since 1957, will add capacity of 100 MW and is expected to deliver 180 GWh per year. Glendoe is billed in the news as "big enough to power every home in a city the size of Glasgow." I bet that people get the impression from this that Glendoe will provide enough electricity "to power Glasgow." But this is a long way from the truth. If we take 180 GWh per year and share it between Glasgow (616 000 people), we get 0.8 kWh/d per person. That is just 5% of the average electricity consumption of 17 kWh/d per person.
- Figure 8.4. A 60 kW waterwheel in Dinorwig, North Wales. With a diameter of 50 feet, it's the largest working waterwheel in Britain. From 1870 to 1925 this waterwheel powered virtually all the machinery of the Dinorwig slateworks.

Hydro: 1.5 kWh/d

Biomass: food, biofuel, wood, waste incin'n, landfill gas: 24 kWh/d

PV farm (200 m²/p): **50 kWh/d**

PV, 10 m²: 5

Solar heating: 13 kWh/d

Wind: 20 kWh/d

Figure 8.3. Hydro.

Car: **40 kWh/d**



Figure 8.4. A 60 kW waterwheel.

Hydro: 1.5 kWh/d

Lighting home and work

The brightest domestic lightbulbs use 250 W, and bedside lamps use 40 W. In an old-fashioned incandescent bulb, most of this power gets turned into heat, rather than light. A fluorescent tube can produce an equal amount of light using one quarter of the power of an incandescent bulb.

How much power does a moderately affluent person use on lighting? My rough estimate, based on table 9.2, is that a typical two-person home with a mix of low-energy and high-energy bulbs uses about 5.5 kWh per day, or 2.7 kWh per day per person. I assume that each person also has a workplace where they share similar illumination with their colleagues; guessing that the workplace uses 1.3 kWh/d per person, we get a round figure of 4 kWh/d per person.

Street-lights and traffic lights

Do we need to include public lighting too, to get an accurate estimate, or do home and work dominate the lighting budget? Street-lights in fact use about $0.1\,\mathrm{kWh}$ per day per person, and traffic lights only $0.005\,\mathrm{kWh/d}$ per person – both negligible, compared with our home and workplace lighting. What about other forms of public lighting – illuminated signs, bollards, for example? There are fewer of them than street lights; and street lights already came in well under our radar, so we don't need to modify our overall estimate of $4\,\mathrm{kWh/d}$ per person.

Lights on the traffic

In some countries, drivers must switch their lights on whenever their car is moving. How does the extra power required by that policy compare with the power already being used to trundle the car around? Let's say the car has four incandescent lights totalling 100 W. The electricity for those bulbs is supplied by a 25%-efficient engine powering a 55%-efficient generator, so the power required is 730 W. For comparison, a typical car going at an average speed of 50 km/h and consuming one litre per 12 km has an

Device	Power	Time per day	Energy per day per home
10 incandescent lights	1 kW	5 h	5 kWh
10 low-energy lights	0.1 kW	5 h	0.5 kWh

Light: 4 kWh/d Heating, cooling:	Biomass: food, biofuel, wood, waste incin'n, landfill gas: 24 kWh/d
37 kWh/d	DV
Jet flights: 30 kWh/d	PV farm (200 m ² /p): 50 kWh/d
	PV, 10 m ² : 5
Car: 40 kWh/d	Solar heating: 13 kWh/d
	Wind: 20 kWh/d

Figure 9.1. Lighting – 4 kWh per day per person.

Table 9.2. Electric consumption for domestic lighting. A plausible total is 5.5 kWh per home per day; and a similar figure at work; perhaps 4 kWh per day per person.

average power consumption of 42 000 W. So the extra power consumed by having the lights on while driving is 2%.

What about the future's electric cars? The power consumption of a typical electric car is about 5000 W. So popping on an extra 100 W would increase its consumption by 2%. Power consumption would be smaller if we switched all car lights to light-emitting diodes, but if we pay any more attention to this topic, we will be coming down with a severe case of every-little-helps-ism.

The economics of low-energy bulbs

Generally I avoid discussion of economics, but I'd like to make an exception for lightbulbs. Osram's 20 W low-energy bulb claims the same light output as a 100 W incandescent bulb. Moreover, its lifetime is said to be 15 000 hours (or "12 years," at 3 hours per day). In contrast a typical incandescent bulb might last 1000 hours. So during a 12 year period, you have this choice (figure 9.3): buy 15 incandescent bulbs and 1500 kWh of electricity (which costs roughly £150); or buy one low-energy bulb and $300 \, \text{kWh}$ of electricity (which costs roughly £30).

Should I wait until the old bulb dies before replacing it?

It feels like a waste, doesn't it? Someone put resources into making the old incandescent lightbulb; shouldn't we cash in that original investment by using the bulb until it's worn out? But the economic answer is clear: continuing to use an old lightbulb is throwing good money after bad. If you can find a satisfactory low-energy replacement, replace the old bulb now.

What about the mercury in compact fluorescent lights? Are LED bulbs better than fluorescents?

Researchers say that LED (light-emitting diode) bulbs will soon be even more energy efficient than compact fluorescent lights. I checked the numbers on my latest purchases: the Philips Genie 11 W compact fluorescent bulb (figure 9.4) has a brightness of 600 lumens, which is an efficiency of 55 lumens per watt; regular incandescent bulbs deliver 10 lumens per watt; the Omicron 1.3 W lamp, which has 20 white LEDs hiding inside it, has a brightness of 46 lumens, which is an efficiency of 35 lumens per watt. So this LED bulb is almost as efficient as the fluorescent bulb. The LED industry still has a little catching up to do. In its favour, the LED bulb has a life of 50 000 hours, eight times the life of the fluorescent bulb. As I write, I see that www.cree.com are selling LEDs with a power of 100 lumens per watt. It's projected that in the future, white LEDs will have an efficiency of over 150 lumens per watt [ynjzej]. I expect that within another couple of years, the best advice, from the point of view of both energy efficiency and avoiding mercury pollution, will be to use LED bulbs.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

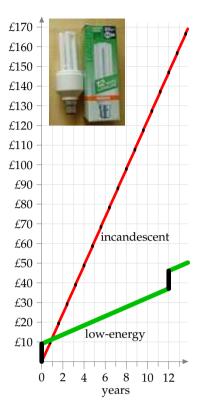


Figure 9.3. Total cumulative cost of using a traditional incandescent 100 W bulb for 3 hours per day, compared with replacing it *now* with an Osram Dulux Longlife Energy Saver (pictured). Assumptions: electricity costs 10p per kWh; traditional bulbs cost 45p each; energy-saving bulbs cost £9. (I know you can find them cheaper than this, but this graph shows that even at £9, they're much more economical.)



Figure 9.4. Philips 11 W alongside Omicron 1.3 W LED bulb.

9 — *Light* 63

Mythconceptions

"There is no point in my switching to energy-saving lights. The "wasted" energy they put out heats my home, so it's not wasted."

This myth is addressed in a couple of chapters on p75.

Notes and further reading

page no.

- 61 Street-lights use about 0.1 kWh per day per person... There's roughly one sodium streetlight per ten people, each with a power of 100 W, switched on for 10 hours per day. That's 0.1 kWh per day per person.
- ...and traffic lights only 0.005 kWh/d per person. Britain has 420 000 traffic and pedestrian signal light bulbs, consuming 100 million kWh of electricity per year. Shared between 60 million people, 100 million kWh per year is 0.005 kWh/d per person.
- There are fewer signs and illuminated bollards than street lights. http://www.highwayelectrical.org.uk/ There are 7.7 million lighting units (street lighting, illuminated signs and bollards) in the UK. Of these, roughly 7 million are street lights and 1 million are illuminated road signs. There are 210 000 traffic signals.
 - According to DUKES 2005, the total power going to public lighting is 2095 GWh/y, which is 0.1 kWh/d per person.
- 55%-efficient generator source: http://en.wikipedia.org/wiki/Alternator

, I	Efficiency mens/W)
incandescent	10
halogen	16-24
white LED	35
compact fluorescer	nt 55
large fluorescent	94
sodium streetlight	150

Table 9.5. Lighting efficiencies of commercially-available bulbs. In the future, white LEDs are expected to deliver 150 lumens per watt.

10 Offshore wind

The London Array offshore wind farm will make a crucial contribution to the UK's renewable energy targets.

James Smith, chairman of Shell UK

Electric power is too vital a commodity to be used as a job-creation programme for the wind turbine industry.

David J. White

At sea, winds are stronger and steadier than on land, so offshore windfarms deliver a higher power per unit area than onshore windfarms. The Kentish Flats windfarm in the Thames Estuary, about $8.5\,\mathrm{km}$ offshore from Whitstable and Herne Bay, which started operation at the end of 2005, was predicted to have an average power density of $3.2\,\mathrm{W/m^2}$. In 2006, its average power density was $2.6\,\mathrm{W/m^2}$.

I'll assume that a power density of $3\,\mathrm{W/m^2}$ (50% larger than our onshore estimate of $2\,\mathrm{W/m^2}$) is an appropriate figure for offshore windfarms around the UK.

We now need an estimate of the area of sea that could plausibly be covered with wind turbines. It is conventional to distinguish between *shallow* offshore wind and *deep* offshore wind, as illustrated in figure 10.2. Conventional wisdom seems to be that *shallow* offshore wind (depth less than 25–30 m), while roughly twice as costly as onshore wind, is economically feasible, given modest subsidy; and *deep* offshore wind is at present not economically feasible. As of 2007, there's just one deep offshore windfarm, an experimental prototype sending all its electricity to a nearby oilrig.

Shallow offshore

Within British territorial waters, the shallow area is about $40\,000\,\mathrm{km^2}$ – most of it off the coast of England and Wales. This area is about two Waleses.

The average power available from shallow offshore windfarms occupying the whole of this area would be 120 GW, or 48 kWh/d per person. But it's hard to imagine this arrangement being satisfactory for shipping. Substantial chunks of this shallow water would, I'm sure, remain off-limits for windfarms. The requirement for shipping corridors and fishing areas must reduce the plausibly-available area; I propose that we assume the available fraction is one third (but please see this chapter's end-notes for a more pessimistic view!). So we estimate the maximum plausible power from shallow offshore wind to be 16 kWh/d per person.

Before moving on, I want to emphasize the audaciously large area – two thirds of a Wales – that would be required to deliver this $16\,\mathrm{kWh/d}$





Figure 10.1. Kentish Flats – a shallow offshore windfarm. Each rotor has a diameter of 90 m centred on a hub height of 70 m. Each "3 MW" turbine weighs 500 tons, half of which is its foundation.

Photos © by Elsam (elsam.com). Used with permission.

10 — Offshore wind 65

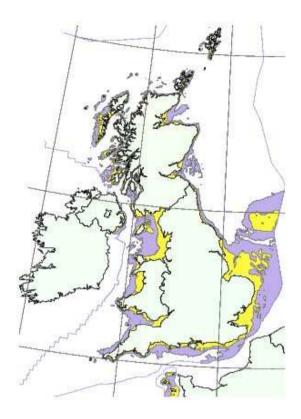


Figure 10.2. UK territorial waters with depth less than 25 m (yellow) and depth between 25 m and 50 m (purple). Data from DTI Atlas of Renewable Marine Resources. © Crown copyright.



per person. If we take the total coastline of Britain (length: $3000 \, \mathrm{km}$), and put a strip of turbines $4 \, \mathrm{km}$ wide all the way round, that strip would have an area of $13000 \, \mathrm{km}^2$. That is the area we must fill with turbines to deliver $16 \, \mathrm{kWh/d}$ per person. To put it another way, consider the number of turbines required. $16 \, \mathrm{kWh/d}$ per person would be delivered by $44\,000$ "3 MW" turbines, which works out to fifteen per kilometre of coastline, if they were evenly spaced around $3000 \, \mathrm{km}$ of coast.

Offshore wind is tough to pull off because of the corrosive effects of sea water. At the big Danish windfarm, Horns Reef, all 80 turbines had to be dismantled and repaired after only 18 months' exposure to the sea air. The Kentish Flats turbines seem to be having similar problems with their gearboxes, one third needing replacement during the first 18 months.

Deep offshore

The area with depths between $25\,\mathrm{m}$ and $50\,\mathrm{m}$ is about $80\,000\,\mathrm{km^2}$ – the size of Scotland. "Deep" offshore windfarms could deliver another $240\,\mathrm{GW}$, or $96\,\mathrm{kWh/d}$ per person, if turbines completely filled this area. Again, we must make corridors for shipping. I suggest as before that we assume we can use one third of the area for wind farms; this area would then be about 30% bigger than Wales, and much of it would be further than $50\,\mathrm{km}$

Deep

offshore. The outcome: if an area equal to a 9 km-wide strip all round the coast were filled with turbines, deep offshore wind could deliver a power of 32 kWh/d per person. A huge amount of power, yes; but still no match for our huge consumption. And we haven't spoken about the issue of wind's intermittency. We'll come back to that in chapter 26.

I'll include this potential deep offshore contribution in the production stack, with the proviso, as I said before, that wind experts reckon deep offshore wind is not economically feasible.

Some comparisons and costs

So, how's our race between consumption and production coming along? Adding both shallow and deep offshore wind to the production stack, the green stack has a lead. Something I'd like you to notice about this race, though, is this contrast: how *easy* it is to toss a bigger log on the consumption fire, and how *difficult* it is to grow the production stack. As I write this paragraph, I'm feeling a little cold, so I step over to my thermostat and turn it up. It's so simple for me to consume an extra 30 kWh per day. But squeezing an extra 30 kWh per day per person from renewables requires an industrialization of the environment so large it is hard to imagine.

To create 48 kWh per day of offshore wind per person in the UK would require 60 million tons of concrete and steel – one ton per person. Annual world steel production is about 1200 million tons, which is 0.2 tons per person. During world war II, American shipyards built 2751 Liberty ships, each containing 7000 tons of steel – that's a total of 19 million tons of steel, or 0.1 tons per American. So the building of 60 million tons of wind turbines is not off the scale of achievability; but don't kid yourself into thinking that it's easy. Making this many windmills is as big a feat as building the Liberty ships.

For comparison, to make $48\,\mathrm{kWh}$ per day of nuclear power per person in the UK would require 8 million tons of steel and $0.14\,\mathrm{million}$ tons of concrete. We can also compare the 60 million tons of offshore wind hardware that we're trying to imagine with the existing fossil-fuel hardware already sitting in and around the North Sea (figure 10.4). In 1997, 200 installations and $7000\,\mathrm{km}$ of pipelines in the UK waters of the North Sea contained 8 million tons of steel and concrete. The newly built Langeled gas pipeline from Norway to Britain, which will convey gas with a power of $25\,\mathrm{GW}$ ($10\,\mathrm{kWh/d/p}$), used another 1 million tons of steel and 1 million tons of concrete (figure 10.5).

The UK government announced on 10th December 2007 that it would permit the creation of 33 GW of offshore capacity (which would deliver on average 10 GW per UK, or 4.4 kWh/d per person), a plan branded "pie in the sky" by some in the wind industry. Let's run with a round figure of 4 kWh per day per person. This is one quarter of my shallow 16 kWh per day per person. To obtain this average power requires roughly 10 000

offshore wind: 32 kWh/d Shallow offshore wind: 16 kWh/d Light: 4 kWh/d Biomass: food, biofuel, wood, waste incin'n, landfill gas: Heating, 24 kWh/d cooling: 37 kWh/d PV farm $(200 \,\mathrm{m}^2/\mathrm{p})$: 50 kWh/d Jet flights: 30 kWh/d PV, 10 m²: 5 Solar heating: 13 kWh/d Car: 40 kWh/d Wind: 20 kWh/d

Figure 10.3. Offshore wind.

[©] David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

10 — Offshore wind 67

"3 MW" wind turbines like those in figure 10.1. (They have a capacity of "3 MW" but on average they deliver 1 MW. I'll pop quotes round "3 MW" to indicate that this is a capacity, a peak power.)

What would this "33 GW" of power cost to erect? Well, the "90 MW" Kentish Flats farm cost £105 million, so "33 GW" would cost about £33 billion. One way to clarify this £33 billion cost of offshore wind delivering 4kWh/d per person is to share it among the UK population; that comes out to £550 per person. This is a much better deal, incidentally, than microturbines. A roof-mounted microturbine currently costs about £1500 and, even at a very optimistic windspeed of 6 m/s, delivers only 1.6 kWh/d. In reality, in a typical urban location in England, such microturbines deliver 0.2 kWh per day.

Another bottleneck constraining the planting of wind turbines is the special ships required. To erect 10 000 wind turbines ("33 GW") over a period of 10 years would require roughly 50 jack-up barges. These cost £60 million each, so an extra capital investment of £3 billion would be required. Not a show-stopper compared with the £33b price tag already quoted, but the need for jack-up barges is certainly a detail that requires some forward planning.

Costs to birds

Do windmills kill "huge numbers of birds"? Wind farms recently got adverse publicity from Norway, where the wind turbines on Smola, a set of islands off the north-west coast, killed nine white-tailed eagles in ten months. I share the concern of BirdLife International for the welfare of rare birds. But I think, as always, it's important to do the numbers. It's been estimated that 30 000 birds per year are killed by wind turbines in Denmark, where windmills generate 9% of the electricity. Horror! Ban windmills! We also learn, moreover, that *traffic* kills *one million* birds per year in Denmark. Thirty-times-greater horror! Thirty-times-greater incentive to ban cars! And in Britain, 55 million birds per year are killed by *cats* (figure 10.6).

Going on emotions alone, I would like to live in a country with virtually no cars, virtually no windmills, and with plenty of cats and birds (with the cats that prey on birds perhaps being preyed upon by Norwegian white-tailed eagles, to even things up). But what I really hope is that decisions about cars and windmills are made by careful rational thought, not by emotions alone. Maybe we do need the windmills!



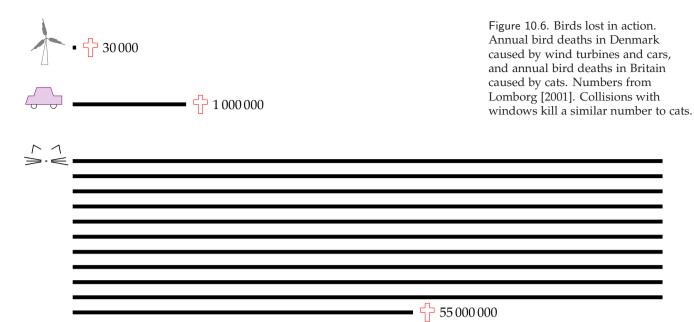


Figure 10.4. The Magnus platform in the northern UK sector of the North Sea contains 71 000 tons of steel. In the year 2000 this platform delivered 3.8 million tons of oil and gas – a power of 5 GW. The platform cost £1.1 billion.

Photos by Terry Cavner.



Figure 10.5. Pipes for Langeled. From Bredero-Shaw [brederoshaw.com].



Notes and further reading

page no.

64 The Kentish Flats windfarm in the Thames Estuary...

See www.kentishflats.co.uk. Its 30 Vestas V90 wind turbines have a total peak output of 90 MW, and the predicted average output was 32 MW (assuming a load factor of 36%). The mean wind speed at the hub height is $8.7\,\mathrm{m/s}$. The turbines stand in 5 m-deep water, are spaced 700 m apart, and occupy an area of $10\,\mathrm{km^2}$. The power density of this offshore windfarm was thus predicted to be $3.2\,\mathrm{W/m^2}$. In fact, the average load factor in 2006 was 29% (227 279 MWh delivered, compared with a capacity of 8760 \times 90 MWh) [wbd8o]. This is a power density of $2.6\,\mathrm{W/m^2}$. The North Hoyle wind farm off Prestatyn, North Wales, had a higher load factor of 36% in 2006. Its thirty 2 MW turbines occupy $8.4\,\mathrm{km^2}$. They thus had an average power density of $2.6\,\mathrm{W/m^2}$.

- shallow offshore wind, while roughly twice as costly as onshore wind, is economically feasible, given modest subsidy. Source: Danish wind association windpower.org.
- deep offshore wind is not at present at all economically feasible. Source: British Wind Energy Association briefing document, September 2005, www.bwea.com. Nevertheless, a deep offshore demonstration project in 2007 put two turbines adjacent to the Beatrice oil field, 22 km off the east coast of Scotland (figure 10.8). Each turbine has a "capacity" of 5 MW and sits in a water depth of 45 m. Hub height: 107 m; diameter 126 m. All the electricity generated will be used by the oil platforms. Isn't that special! The 10 MW project cost £30 million this pricetag of £3 per watt
- (c) David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

10 — Offshore wind 69

	Depth 5 to 30 metres		Depth 30 to 50 metres	
Region	area	potential resource	area	potential resource
	(km^2)	(kWh/d/p)	(km^2)	(kWh/d/p)
North West	3300	6	2000	4
Greater Wash	7400	14	950	2
Thames Estuary	2100	4	850	2
Other	14000	28	45000	87
TOTAL	27 000	52	49 000	94

Table 10.7. Potential offshore wind generation resource in proposed strategic regions, if these regions were *entirely filled* with wind turbines. From Department of Trade and Industry [2002b].

(peak) can be compared with that of Kentish Flats, £1.2 per watt (£105 million for $90\,\mathrm{MW}$). http://www.beatricewind.co.uk/

64 The area available for offshore wind.

The Department of Trade and Industry's [2002] document "Future Offshore" gives a detailed breakdown of areas that are useful for offshore wind power. Table ?? shows the estimated resource in 76 000 km² of shallow and deep water. Their estimated power contribution, if these areas were entirely filled with windmills, is 146 kWh/d per person (consisting of 52 kWh/d/p from the shallow and 94 kWh/d/p from the deep). But the DTI's estimate of the potential offshore wind generation resource is just 4.6 kWh per day per person. It might be interesting to describe how they get down from this potential resource of 146 kWh/d per person to 4.6 kWh/d per person. Why a final figure so much lower than ours? First, they imposed these limits: the water must be within 30 km of the shore and less than 40 m deep; the sea bed must not have gradient greater than 5 degrees; shipping lanes, military zones, pipelines, fishing grounds, and wildlife reserves are excluded. Second, they assumed that only 5% of potential sites will be developed (as a result of seabed composition or planning constraints); they reduced the capacity by 50% for all sites less than 10 miles from shore, for reasons of public acceptability; they further reduced the capacity of sites with wind speed over 9 m/s by 95% to account for "development barriers presented by the hostile environment;" and other sites with average wind speed 8-9 m/s had their capacities reduced by 5%.

- 65 ...if we take the total coastline of Britain (length: 3000 km), and put a strip of turbines 4 km wide all the way round... Pedants will say that "the coastline of Britain is not a well-defined length, because the coast is a fractal." Yes, yes, it's a fractal. But, dear pedant, please take a map and put a strip of turbines 4 km wide around mainland Britain, and see if it's not the case that your strip is indeed about 3000 km long.
- Horns Reef (Horns Rev). The difficulties with this "160 MW" Danish wind farm off Jutland [www.hornsrev.dk] are described in Halkema [2006]. When it is working, Horns Reef's load factor is 0.43 and its average power per unit area is 2.6 W/m².

Prepublication draft~2.9.0.~August 28, 2008 www.withouthotair.com

- 66 Liberty ships http://www.liberty-ship.com/html/yards/introduction.html
- 66 fossil fuel installations in the North Sea contained 8 million tons of steel and concrete Rice and Owen [1999].
- The UK government announced on 10th December 2007 that it would permit the creation of 33 GW of offshore capacity... [25e59w].
- ... "pie in the sky". Source: Guardian [2t2vjq].
- 67 What would "33 GW" of offshore wind cost? According to the DTI in November 2002, electricity from offshore windfarms costs about £50 per MWh (5p per kWh) [Department of Trade and Industry, 2002b, p.21]. Economic facts vary, however, and in April 2007 the estimated cost of offshore was up to £92 per MWh [Department of Trade and Industry, 2007, p. 7]. By April 2008, the price of offshore wind evidently went even higher: Shell pulled out of their commitment to build the London Array. It's because offshore wind is so expensive that the government is having to increase the number of ROCs (renewable obligation certificates) per unit of offshore wind energy. The ROC is the unit of subsidy given out to certain forms of renewable electricity generation. The standard value of a ROC is £45, with 1 ROC per MWh; so with a wholesale price of roughly £40/MWh, renewable generators are getting paid £85 per MWh. So 1 ROC per MWh is not enough subsidy to cover the cost of £92 per MWh. In the same document, estimates for other renewables (medium levelized costs in 2010) are as follows. Onshore wind: £65-89/MWh; cofiring of biomass: £53/MWh; large-scale hydro: £63/MWh; sewage gas: £38/MWh; solar PV: £571/MWh; wave: £196/MWh; tide: £177/MWh. "Dale Vince, chief executive of green energy provider Ecotricity, which is engaged in building onshore wind farms, said that he supported the government's [offshore wind] plans, but only if they are not to the detriment of onshore wind. 'It's dangerous to overlook the fantastic resource we have in this country ... By our estimates, it will cost somewhere in the region of £40bn to build the 33 GW of offshore power Hutton is proposing. We could do the same job onshore for £20bn'." [57984r]
- In a typical urban location in England, microturbines deliver 0.2 kWh per day. Source: Third Interim Report, http://www.warwickwindtrials.org.uk/2.html. Among the best results in the Warwick Wind Trials study is a Windsave WS1000 (a 1-kW machine) in Daventry mounted at a height of 15 m above the ground, generating 0.6 kWh/d on average. But some microturbines deliver only 0.05 kWh per day Source: Donnachadh McCarthy: "My carbon-free year", The Independent, December 2007 [6oc3ja]. The Windsave WS1000 wind turbine, sold across England in B&Q's shops, won an Eco-Bollocks award from Housebuilder's Bible author Mark Brinkley: "Come on, it's time to admit that the roof-mounted wind turbine industry is a complete fiasco. Good money is being thrown at an invention that doesn't work. This is the Sinclair C5 of the Noughties." [5soq12]. The Met Office and Carbon Trust published a report in July 2008 [6g2jm5], which estimates that, if small-scale turbines were installed









Figure 10.8. Construction of the Beatrice demonstrator deep offshore windfarm. Photos kindly provided by Talisman Energy (UK) Limited.

10 — Offshore wind 71





Figure 10.9. Kentish Flats. Photos © by Elsam (elsam.com). Used with permission.

at all houses where economical in the UK, they would generate in total roughly $0.7\,\mathrm{kWh/d/p}$. They advise that roof-mounted turbines in towns are usually worse than useless: "in many urban situations, roof-mounted turbines may not pay back the carbon emitted during their production, installation and operation."

67 Jack-up barges cost £60 million each. Source: http://news.bbc.co.uk/
1/hi/magazine/7206780.stm. I estimated that we'd need roughly 50 of
them by assuming that there would be 60 work-friendly days each year,
and that erecting a turbine would take 3 days.

Further reading: UK wind energy database [www.bwea.com/ukwed/].

11 Gadgets

One of the greatest dangers to society is the phone charger. The BBC News has been warning us of this since 2005:

"The nuclear power stations will all be switched off in a few years. How can we keep Britain's lights on? ... unplug your mobile-phone charger when it's not in use."

Sadly, a year later, Britain hadn't got the message, and the BBC were forced to report:

"Britain tops energy waste league."

And how did this come about? The BBC rams the message home:

"65% of UK consumers leave chargers on."

From the way reporters talk about these planet-destroying black objects, it's clear that they are roughly as evil as Darth Vader. But how evil, exactly?

In this chapter we'll find out the truth about chargers. We'll also investigate their cousins in the gadget parade: computers, phones, and TVs. Digital set-top boxes. Cable modems. In this chapter we'll estimate the power used in running them and charging them, but not in manufacturing the toys in the first place – we'll address that in the later chapter on "stuff."

The truth about chargers

Modern phone chargers, when left plugged in with no phone attached, use about half a watt. In our preferred units, this is a power consumption of about 0.01 kWh per day. For anyone whose consumption stack is over 100 kWh per day, the BBC's advice, *always unplug the phone charger*, could potentially reduce their energy consumption by one hundredth of one percent (if only they would do it).

Every little helps!

I don't think so. Obsessively switching off the phone-charger is like bailing the Titanic with a teaspoon. Do switch it off, but please be aware how tiny a gesture it is. Let me put it this way:

All the energy saved in switching off your charger for one day is used up in *one second* of car-driving.

The energy saved in switching off the charger for *one year* is equal to the energy in a single hot bath.





Vader

Charger

Figure 11.1. Planet destroyers. Spot the difference.



Figure 11.2. These five chargers – three for mobile phones, one for a pocket PC, and one for a laptop – registered less than one watt on my power meter.

11 — *Gadgets* 73

Admittedly, some older chargers use more than half a watt – if it's warm to the touch, it's probably using one watt or even two (figure 11.3). A two-watt-guzzling charger uses 0.05 kWh per day. I think that it's a good idea to switch off such a charger – it *will* save you two pounds per year. But don't kid yourself that you've "done your bit" by so doing. 2 W is only a small fraction of total energy consumption.

OK, that's enough bailing the Titanic with a teaspoon. Let's find out where the electricity is really being used.

Gadgets that really suck

Table 11.4 shows the power consumptions, in watts, of a houseful of gadgets. The first column shows the power consumption when the device is actually being used – for example, when a sound system is actually playing sound. The second column shows the consumption when the device is switched on, but sitting doing nothing. I was particularly shocked to find that a laser-printer sitting idle consumes 17 W – the same as the average consumption of a fridge-freezer! The third column shows the consumption when the gadget is explicitly asked to go to sleep or standby. The fourth shows the consumption when it is completely switched off – but still left plugged in to the mains. I'm showing all these powers in watts – to convert back to our standard units, remember that 40 W is 1 kWh/d. A nice rule of thumb, by the way, is that each watt costs about one pound per year (assuming electricity costs 10p per kWh).

The biggest guzzlers are the computer, its screen, and the television, whose consumption is in the hundreds of watts, when on. Entertainment systems such as stereos and DVD players swarm in the computer's wake, many of them consuming $10\,\mathrm{W}$ or so. A DVD player may cost just £20 in the shop, but if you leave it switched on all the time, it's costing you another £10 per year. Some stereos and computer peripherals consume several watts even when switched off, thanks to their mains-transformers. To be sure that a gadget is truly off, you need to switch it off at the wall.

Powering the hidden tendrils of the information age

According to Jonathan Koomey [2007], the computer-servers in US datacentres and their associated plumbing (air conditioners, backup power systems, and so forth) consumed 0.4kWh per day per person – just over 1% of US electricity consumption. That's the consumption figure for 2005, which, by the way, is twice as big as the consumption in 2000, because the number of servers grew from 5.6 million to ten million.

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

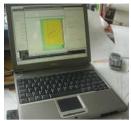


Figure 11.3. This lousy cordless phone and its charger use 2 W when left plugged in. That's **0.05 kWh/d**. If electricity costs 10p per kWh then a 2 W trickle costs £2 per year.



Gadget	Power consumption (W)			
-	on and	on but	standby	off
	active	inactive		
Computer and peripherals:				
computer box	80	55		2
cathode-ray display	110		3	0
LCD display	34		2	1
projector	150		5	
laser printer	500	17		
wireless & cable-modem	9			
Laptop computer	16	9		0.5
Portable CD player	2			
Bedside clock-radio	1			
Bedside clock-radio	1.6			
Digital radio	8		3	
Radio cassette-player	3	1		1
Stereo amplifier	6			6
Stereo amplifier	13			0
Home cinema sound	7	7	4	
DVD player	7	6		
DVD player	12	10	5	
TV	100		10	
Video recorder	13		1	
Digital TV set top box	6		5	
Clock on microwave oven	2			
Xbox	160		2.4	
Sony Playstation 3	190		2	
Nintendo Wii	18		2	
Answering machine		2		
Answering machine		3		
Cordless telephone		1.7		
Mobile phone charger		0.5		
Vacuum cleaner	1600			

Table 11.4. Power consumptions of various gadgets, in watts. $40\,\mathrm{W}$ is $1\,\mathrm{kWh/d}$.





Laptop: 16 W

Computer: 80 W





LCD CRT 31 W 108 W

Printer: 17 W (on, idle)





Projector: 150 W

Digital radio: 8 W

Other gadgets

A vacuum cleaner, used for a couple of hours per week, uses about 0.2 kWh/d. Mowing the lawn uses about 0.6 kWh. We could go on, but I suspect that computers and entertainment systems are the big suckers on most people's electrical balance-sheet.

This chapter's summary figure: it'll depend how many gadgets you have at home and work, but a healthy houseful or officeful of gadgets left on all the time could easily use 5 kWh/d.

Mythconceptions

"There is no point in my switching off lights, TVs, and phone chargers during the winter. The "wasted" energy they put out heats my home, so it's not wasted."

This myth is *True* for a few people, but only during the winter; but *False* for most.

If your house is being heated by electricity through ordinary bar fires or blower heaters then, yes, it's much the same as heating the house with any electricity-wasting appliances. But if you are in this situation, you should change the way you heat your house. Electricity is high-grade energy, and heat is low-grade energy. It's a waste to turn electricity into heat. To be precise, if you make only one unit of heat from a unit of electricity, that's a waste. Heaters called air-source heat pumps or ground-source heat pumps can do much better, delivering 3 or 4 units of heat for every unit of electricity consumed. They work like back-to-front refrigerators, pumping heat into your house from the outside air (see Chapter 21).

For the rest, whose homes are heated by fossil fuels or biofuels, it's a good idea to avoid using electrical gadgets as a heat source for your home – at least for as long as our increases in electricity-demand are served from fossil fuels. The point is, if you use electricity from an ordinary fossil power station, more than half of the energy from the fossil fuel goes sadly up the cooling tower. Of the energy that gets turned into electricity, about 8% is lost in the transmission system. If you burn the fossil fuel in your home, more of the energy goes directly into making hot air for you.

Notes and further reading

page no.

72 The BBC News has been warning us ... unplug your mobile-phone charger. The BBC News article from 2005 said: "the nuclear power stations will all be switched off in a few years. How can we keep Britain's lights on? Here's three ways you can save energy: switch off video recorders when they're not in use; don't leave televisions on standby; and unplug your mobile-phone charger when it's not in use."

Jet flights:
30 kWh/d

PV, 10 m²: 5

Solar heating:
13 kWh/d

Wind:
20 kWh/d

Figure 11.5. Information systems and

Gadgets: 5

Light: 4 kWh/d

Heating,

cooling:

37 kWh/d

Deep offshore

wind:

32 kWh/d

Shallow

offshore wind: 16 kWh/d

Biomass: food,

biofuel, wood,

waste incin'n, landfill gas:

24 kWh/d

Figure 11.5. Information systems and other gadgets.

Photo of air-source heat pump.

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

- Modern phone chargers, when left plugged in with no phone attached, use about half a watt. The Maplin power meter in figure 11.2 is not accurate enough to measure this sort of power. I am grateful to Sven Weier and Richard McMahon of Cambridge University Engineering Department who measured a standard Nokia charger in an accurate calorimeter; they found that, when not connected to the mobile, it wastes 472 mW. They made additional interesting measurements: the charger, when connected to a fully-charged mobile phone, wastes 845 mW; and when the charger is doing what it's meant to do, charging a partly-charged Nokia mobile, it wastes 4.146 W as heat. Pedants sometimes ask "what about the reactive power of the charger?" This is a technical niggle, not really worth our time. For the record, I measured the reactive power (with a crummy meter) and found it to be about 2 VA per charger. Given that the power loss in the national grid is 8% of the delivered power, I reckon that the power loss associated with the reactive power is at most 0.16 W. When actually making a phone-call, the mobile uses 1 W.

Further reading: Kuehr [2003]

Somewhere I need to include other household gadgets – vacuum cleaner (1.4 kWh/week), lawn mower (notes in electricity.tex).

12 Wave

If wave power offers hope to any country, then it must offer hope to the United Kingdom and Ireland – flanked on the one side by the Atlantic Ocean, and on the other by the North Sea.

First, let's clarify where waves come from: sun makes wind and wind makes waves.

Most of the sunlight that hits our planet warms the oceans. The warmed water warms the air above it, and releases water vapour. The warmed air rises; as it rises it cools, and the water eventually re-condenses, forming clouds and rain. At its highest point, the air is cooled down further by the freezing blackness of space. The cold air sinks again. This great solar-powered pump drives air round and round in great convection rolls. From our point of view on the surface, these convection rolls produce the winds. Wind is second-hand solar energy. As wind rushes across open water, it generates waves. Waves are thus third-hand solar energy. (The waves that crash on a beach are nothing to do with the tides.)

In open water, waves are generated whenever the wind speed is greater than about $0.5\,\mathrm{m/s}$. The wave crests move at about the speed of the wind that creates them, and in the same direction. The *wavelength* of the waves (the distance between crests) and the *period* (the time between crests) depend on the speed of the wind. The longer the wind blows for, and the greater the expanse of water over which the wind blows, the greater the *height* of the waves stroked up by the wind. Thus since the prevailing winds over the Atlantic go from west to east, the waves arriving on the Atlantic coast of Europe are often especially big. (The waves on the east coast of the British Isles are usually much smaller, so my estimates of potential wave power will focus on the resource in the Atlantic ocean.)

Waves have long memory and will keep going in the same direction for days after the wind stopped blowing, until they bump into something. In seas where the direction of the wind changes frequently, waves born on different days form a superposed jumble, travelling in different directions.

If waves travelling in a particular direction encounter objects that absorb energy from the waves – for example, a row of islands with sandy beaches – then the seas beyond the object are calmer. The objects cast a shadow, and there's less energy in the waves that get by. So, whereas sunlight delivers a power per unit *area*, waves deliver a power per unit *length* of coastline. You can't have your cake and eat it. You can't collect wave energy two miles off-shore *and* one mile off-shore. Or rather, you can try, but the two-mile facility will absorb energy that would have gone to the one-mile facility, and it won't be replaced. The fetch required for wind to stroke up big waves is thousands of miles.

We can find an upper bound on the maximum conceivable power that could be obtained from wave power by estimating the incoming power







Figure 12.1. A Pelamis wave energy collector is a sea snake made of four sections. It faces nose-on towards the incoming waves. The waves make the snake flex, and these motions are resisted by hydraulic generators. The peak power from one snake is 750 kW; in the best Atlantic location one snake would deliver 300 kW on average. From Pelamis wave power www.pelamiswave.com.

per unit length of exposed coastline, and multiplying by the length of coastline. We ignore the question of what mechanism could collect all this power, and start by working out how much power it is.

The power of Atlantic waves has been measured: it's about $40\,\mathrm{kW}$ per metre of exposed coastline.

That sounds like a lot of power! If everyone owned a metre of coastline and could harness their whole 40 kW, that would be plenty of power to cover modern consumption. However, *our population is too big*. There is not enough Atlantic-facing coastline for everyone to have their own metre.

As the map on p77 shows, Britannia rules about $1000\,\mathrm{km}$ of Atlantic (one million metres), which is $^{1}/_{60}\,\mathrm{m}$ per person. So the total raw incoming power is $16\,\mathrm{kWh}$ per day per person. If we extracted all this power, the Atlantic, at the seaside, would be as flat as a millpond. Practical systems won't manage to extract all the power, and some of the power will inevitably be lost during conversion from mechanical energy to electricity. Let's assume that brilliant wave-machines are 50%-efficient at turning the incident power into electricity, and that we are able to pack wave-machines along $500\,\mathrm{km}$ of Atlantic-facing coastline. That would mean we could deliver 25% of this theoretical bound. That's $4\,\mathrm{kWh}$ per day per person.

How do the numbers assumed in this calculation compare with today's technology? As I write, there are still no wave energy collectors working in deep water; some Pelamis wave energy collectors are sitting coyly on the shore in Portugal but there's no news of their having been deployed. The makers of the Pelamis ("designed with survival as the key objective before power capture efficiency") describe a two-kilometre-long wave-farm consisting of 40 of their sea-snakes, delivering 6 kW per metre. Using this figure in the previous calculation, the power delivered by 500 kilometres of wave-farm is reduced to 1.2 kWh/d per person. While wave power may be useful for small communities on remote islands, I suspect it can't play a significant role in the solution to Britain's sustainable energy problem.

What's the weight of a Pelamis, and how much steel does it contain? One snake with a maximum power of 750 kW weighs 700 tons, including 350 tons of ballast. So it has about 350 tons of steel. That's a weight-to-power ratio of roughly 500 kg per kW (peak). We can compare this with the steel requirements for offshore wind: an offshore wind-turbine with a maximum power of 3 MW weighs 500 tons, including its foundation. That's a weight-to-power ratio of about 170 kg per kW, one third of the wave machine's. The Pelamis is a first prototype; presumably with further investment and development in wave technology, the weight-to-power ratio would fall.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

Wave: 4 kWh/d Deep offshore wind: 32 kWh/d Shallow offshore wind: 16 kWh/d Gadgets: 5 Light: 4 kWh/d Biomass: food, biofuel, wood, waste incin'n, landfill gas: 24 kWh/d Heating, cooling: 37 kWh/d PV farm $(200 \,\mathrm{m}^2/\mathrm{p})$: 50 kWh/d Jet flights: 30 kWh/d PV, 10 m²: 5 Solar heating: 13 kWh/d Car: 40 kWh/d Wind: 20 kWh/d

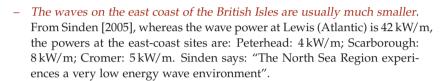
Figure 12.2. Wave.

12 — Wave 79

Notes and further reading

page no.

77 Waves are generated whenever the wind speed is greater than about 0.5 m/s. The wave crests move at about the speed of the wind that creates them. The simplest theory of wave-production [Faber, 1995, p. 337] suggests that (for small waves) the wave crests move at about half the speed of the wind that creates them. It's found empirically however that, the longer the wind blows for, the longer the wavelength of the dominant waves present, and the greater their velocity. The characteristic speed of fully-developed seas is almost exactly equal to the wind-speed 20 metres above the sea surface [Mollison, 1986].



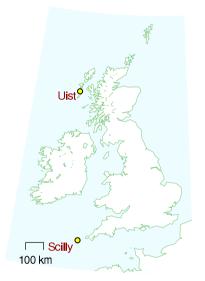


(Chapter F explains how we can estimate this power using a few facts about waves.) This number has a firm basis in the literature on Atlantic wave power [Mollison et al., 1976, Mollison, 1986, 1991]. From Mollison [1986], for example: "the large scale resource of the NE Atlantic, from Iceland to North Portugal, has a net resource of 40–50 MW/km, of which 20–30 MW/km is potentially economically extractable." At any point in the open ocean, three powers per unit length can be distinguished: the total power passing through that point in all directions (63 kW/m on average at the Isles of Scilly and 67 kW/m off Uist); the net power intercepted by a directional collecting device oriented in the optimal direction (47 kW/m and 45 kW/m respectively); and the power per unit coastline, which takes into account the misalignment between the optimal orientation of a directional collector and the coastline (for example in Portugal the optimal orientation faces northwest and the coastline faces west).

Practical systems won't manage to extract all the power, and some of the power will inevitably be lost during conversion from mechanical energy to electricity. The UK's first grid-connected wave machine, the Limpet on Islay, provides a striking example of these losses. When it was designed its conversion efficiency from wave power to grid power was estimated to be 0.48, and the average power output was predicted to be 200 kW. However losses in the capture system, flywheels and electrical components mean the actual average output is 21 kW – just 5% of the predicted output [Wavegen, 2002].



Photo by Terry Cavner.



13 Food and farming

Modern agriculture is the use of land to convert petroleum into food.

Albert Bartlett

We've already discussed in chapter 6 how much sustainable power could be produced through greenery; in this chapter we discuss how much power is currently *consumed* in giving us our daily bread.

A moderately active person with a weight of 65 kg consumes food with a chemical energy content of about 2600 "Calories" per day. A "Calorie," in food circles, is actually 1000 chemist's calories (1 kcal), or 4200 joules of energy. So 2600 "Calories" per day is about 3 kWh per day. One function of a typical person is thus to act as a space heater with an output of a little over 100 W, a medium-power lightbulb. Put ten people in a small cold room, and you can switch off the 1 kW convection heater.

How much energy do we actually consume in order to get our 3 kWh per day? If we enlarge our viewpoint to include the inevitable upstream costs of food production, then we may find that our energy footprint is substantially bigger. It depends if we are vegan, vegetarian or carnivore.

The vegan has the smallest inevitable footprint: 3 kWh/d of energy from the plants he eats.

The energy cost of drinking milk

I love milk. If I drinka-pinta-milka-day, what energy does that require? A typical dairy cow produces 16 litres of milk per day. So my one pint per day (half a litre per day) requires that I employ ¹/₃₂ of a cow. Oh, hang on - I love cheese too. And to make 1 kg of Irish Cheddar takes about 9 kg of milk. So consuming 50 g of cheese per day requires the production of an extra 450 g of milk. OK: my milk and cheese habit requires that I employ $\frac{1}{16}$ of a cow. And how much power does it take to run a cow? Well, if a cow weighing 450 kg has similar energy requirements per kilogram to a human (whose 65 kg burns 3 kWh per day) then the cow must be using about 21 kWh/d. Does this extrapolation from human to cow make you uneasy? Let's check these numbers: www.dairyaustralia.com.au says that a suckling cow of weight 450 kg needs 85 MJ/day, which is 24 kWh/d. Great, our guess wasn't far off! So my ¹/₁₆ share of a cow has an energy consumption of about 1.5 kWh/d. This figure ignores other energy costs involved in persuading the cow to make milk and the milk to turn to cheese, and of getting the milk and cheese to travel from her to me. We'll cover some of these costs when we discuss freight in Chapter 15.



Figure 13.1. A salad nicoise, yesterday.

Minimum: 3 kWh/d

Figure 13.2. Minimum energy requirement of one person.

Milk, cheese: 1.5 kWh/d

Figure 13.3. Milk and cheese.

Eggs

A "layer" (a chicken that lays eggs) eats about 110 g of chicken feed per day. Assuming chicken feed has a metabolizable energy content of 3.3 kWh per kg, that's a power consumption of 0.4 kWh per day per chicken. Layers yield on average 290 eggs per year. So eating two eggs a day requires a power of 1kWh/d. Each egg itself contains 80 kcal, which is about 0.1 kWh. So from an energy point of view, egg production is 20% efficient.

Eggs: 1kWh/d

Figure 13.4. Two eggs per day.

The energy cost of eating meat

Let's say an enthusiastic meat-eater eats about half a pound a day (227 g). To work out the power required to maintain the meat-eater's animals as they mature and wait for the chop, we need to know for how long the animals are around, consuming energy. Chicken, pork, or beef?

Chicken, sir? Every chicken you eat was clucking around being a chicken for roughly 50 days. So the steady consumption of half a pound a day of chicken requires about 25 pounds of chicken to be alive, preparing to be eaten. And those 25 pounds of chicken consume energy.

Pork, madam? Pigs are around for longer – maybe 400 days from birth to bacon – so the steady consumption of half a pound a day of pork requires about 200 pounds of pork to be alive, preparing to be eaten.

Cow? Beef production involves the longest lead times. It takes about 1000 days to create a steak. So the steady consumption of half a pound a day of beef requires about 500 pounds of beef to be alive, preparing to be eaten.

To condense all these ideas down to a single number, let's assume you eat half a pound (227 g) a day of meat, made up of equal quantities of chicken, pork, and beef. This meat habit requires the perpetual sustenance of 8 pounds of chicken meat, 70 pounds of pork meat, and 170 pounds of cow meat. That's a total of 110 kg of meat, or 170 kg of animal (since about two thirds of the animal gets turned into meat). And if the 170 kg of animal has similar power requirements to a human (whose 65 kg burns 3 kWh/d) then the power required to fuel the meat habit is

$$170 \,\mathrm{kg} \times \frac{3 \,\mathrm{kWh/d}}{65 \,\mathrm{kg}} \simeq 8 \,\mathrm{kWh/d}.$$

I've again taken the physiological liberty of assuming "animals are like humans"; a more accurate estimate of the energy to make chicken is in this chapter's endnotes. No matter, I only want a ballpark estimate, and here it is. The power required to make the food for a typical consumer of vegetables, dairy, eggs, and meat is 1.5 + 1.5 + 1 + 8 = 12 kWh per day. (The calorific balance of this rough diet is 1.5 kWh/d from vegetables; 0.7 kWh from dairy; 0.2 kWh from eggs; and 0.5 kWh from meat.)

Carnivory: 8 kWh/d

Figure 13.5. Eating meat requires extra power because we have to feed the queue of animals lining up to be eaten by the human.

This number does not include any of the power costs associated with fertilizing, processing, refrigerating, and transporting the food. We'll estimate some of those costs in Chapter 15.

Do these calculations give an argument in favour of vegetarianism, on the grounds of lower energy consumption? It depends on where the animals feed. Take the steep hills and mountains of Wales, for example. Could the land be used for anything other than grazing? Either these rocky pasturelands are used to sustain sheep, or they are not used to help feed humans. You can think of these natural green slopes as maintenance-free biofuel plantations, and the sheep as automated self-replicating biofuelharvesting machines. The energy losses between sunlight and mutton are substantial, but there is probably no better way of capturing solar power in such places. (I'm not sure whether this argument for sheep-farming in Wales actually adds up: during the worst weather, Welsh sheep are moved to lower fields where their diet is supplemented with soya feed and other food grown with the help of energy-intensive fertilizers; what's the true energy cost? I don't know.) Similar arguments can be made in favour of carnivory for places such as the scrublands of Africa and the grasslands of Australia; and in favour of dairy-consumption in India, where millions of cows are fed on byproducts of rice and maize farming.

On the other hand, where animals are reared in cages and fed grain that humans could have eaten, there's no question that it would be more energy-efficient to cut out the middlehen or middlesow, and feed the grain directly to humans.

Fertilizer costs

The embodied energy in Europe's fertilizers is about 2 kWh per day per person.

The energy cost of Tiddles, Fido, and Shadowfax

Animal companions! Are you the servant of a dog, a cat, or a horse?

There are perhaps eight million cats in Britain. Let's assume you look after one of them. The energy cost of Tiddles? If she eats 50 g of meat per day (chicken, pork, and beef), then the last section's calculation says that the power required to make Tiddles' food is just shy of 2 kWh/d. A vegetarian cat would require less.

Similarly if your dog Fido eats 200 g of meat per day, and carbohydrates amounting to 1 kWh per day, then the power required to make his food is about 9 kWh per day.

Shadowfax the horse weighs about 400 kg and consumes 17 kWh per day.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

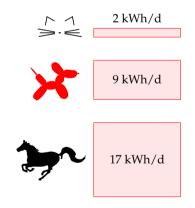


Figure 13.6. The power required for animal companions' food.

83

Wave: 4 kWh/d

Mythconceptions

I heard that the energy footprint of food is so big that "it's better to drive than to walk."

It's certainly possible to find food whose energy footprint is bigger than the energy delivered to the human. A bag of crisps, for example, has an embodied energy of 1.4 kWh of fossil fuel per kWh of chemical energy eaten. The embodied energy of meat is higher. According to a study from the University of Exeter, the typical diet has an embodied energy of roughly 6 kWh per kWh eaten. To figure out whether driving a car or walking uses less energy, we need to know the transport efficiency of each mode. For the typical car of Chapter 3, the energy cost was 80 kWh per 100 km. Walking uses a net energy of 3.6 kWh per 100 km – twenty-two times less. So if you live entirely on food whose footprint is greater than 22 kWh per kWh then, yes, the energy cost of getting you from A to B in a fossil-fuel-powered vehicle is less than if you go under your own steam. But if you have a typical diet (6 kWh per kWh) then "it's better to drive than to walk" is a myth. Walking uses one quarter as much energy.

Notes and further reading

page no.

- 80 A typical dairy cow produces 16 litres of milk per day. There are 2.3 million dairy cows in the UK, each producing around 5900 litres per year. Half of all milk produced by cows is sold as liquid milk. http://www.ukagriculture.com/, http://www.vegsoc.org/info/cattle.html
- 81 It takes about 1000 days to create a steak. 33 months from conception to slaughterhouse: 9 months' gestation and 24 months' rearing. http://www.shabdenparkfarm.com/farming/cattle.htm
- Chicken. A full-grown (20-week old) layer weighs 1.5 or 1.6 kg. Its feed has an energy content of 2850 kcal per kg, which is 3.3 kWh per kg, and its feed consumption rises to 340 g per week when 6 weeks old, and to 500 g per week when aged 20 weeks. Once laying, the typical feed required is 110 g per day.

Meat chickens' feed has an energy content of 3200 kcal per kg, which is 3.7 kWh per kg. Energy consumption is 400–450 kcal per day per hen, or 0.5 kWh/d per hen, with 2 kg being a typical body weight. A meat chicken weighing 2.95 kg consumed a total of 5.32 kg of feed [5h69fm]. So the embodied energy of a meat chicken is about 6.7 kWh per kg of animal, or 10 kWh per kg of eaten meat. If I'd used this number instead of my rough guess, the energy contribution of the chicken would have been bumped up a little. But given that the mixed-meat diet's energy footprint is dominated by the beef, it really doesn't matter that I treated the chickens somewhat innacurately. Sources: Subcommittee on Poultry Nutrition, National Research Council [1994], http://www.nap.edu/openbook.php?isbn=0309048923, http://www.statistics.gov.uk/statbase/datasets2.asp, and MacDonald [2008].

Deep offshore wind: 32 kWh/d Shallow Food & offshore fertilizer: wind: 14 kWh/d 16 kWh/d Gadgets: 5 Light: 4 kWh/d Biomass: food, biofuel, wood, waste incin'n, landfill gas: 24 kWh/d Heating, cooling: 37 kWh/d PV farm $(200 \,\mathrm{m}^2/\mathrm{p})$: 50 kWh/d Jet flights: 30 kWh/d PV, 10 m²: 5 Solar heating: 13 kWh/d Car: 40 kWh/d Wind: 20 kWh/d

Figure 13.7. Food and farming.

- let's assume you eat half a pound (227 g) a day of meat, made up of equal quantities of chicken, pork, and beef. This is very close to the average meat consumption in America, which is 108 g chicken, 81 g beef, and 62 g of pork per day [MacDonald, 2008].
- 82 The embodied energy in Europe's fertilizers is about 2 kWh per day per person. In 1998–99, Western Europe used 17.6 Mt per year of fertilizers: 10 Mt of nitrates, 3.5 Mt of phosphate and 4.1 Mt potash. These fertilizers have energy footprints of 21.7, 4.9, and 3.8 kWh per kg respectively. Sharing this energy out between 375 million people, we find a total footprint of 1.8 kWh per day per person. Sources: Gellings and Parmenter [2004], International Fertilizer Industry Association [5pwojp].
- 83 A bag of crisps has an embodied energy of 1.4 kWh of fossil fuel per kWh of chemical energy eaten. The carbon footprint of a bag of crisps is 75 g CO₂ for a standard 35 g bag. [5bj8k3] Of this footprint, 44% is farming, 30% is processing, 15% packaging, and 11% transport and disposal. The chemical energy delivered to the consumer is 770 kJ. So this food has a carbon footprint of 350 g per kWh. Assuming that most of this carbon footprint is from fossil fuels at 250 g CO₂ per kWh, the energy footprint of the crisps is 1.4 kWh of fossil fuel per kWh of chemical energy eaten.
- The typical diet has an embodied energy of roughly 6 kWh per kWh eaten.
 Coley [2001] estimates the embodied energy in a typical diet is 5.75 times the derived energy. Walking has a CO₂ footprint of 42 g/km; cycling, 30 g/km. For comparison, driving an average car emits 183 g/km.
- Walking uses 3.6 kWh per 100 km. A walking human uses a total of 6.6 kWh per 100 km [3s576h]; we subtract off the resting energy to get the energy footprint of walking [Coley, 2001].

Further reading: Weber and Matthews [2008].

14 Tide

The moon and earth are in a whirling, pirouetting dance around the sun. Together they tour the sun once every year, at the same time whirling around each other once every 28 days. The moon also turns around once every 28 days so that she always shows the same face to her dancing partner, the earth. The prima donna earth doesn't return the complement; she pirouettes once every day. This dance is held together by the force of gravity: every bit of the earth, moon, and sun is pulled towards every other bit of earth, moon, and sun. The sum of all these forces is *almost* exactly what's required to keep the whirling dance on course. But there are very slight imbalances between the gravitational forces and the forces required to maintain the dance. It is these imbalances that give rise to the tides.

The imbalances associated with the whirling of the moon and earth around each other are about three times as big as the imbalances associated with earth's slower dance around the sun, so the size of the tides varies with the phase of the moon. At full moon and new moon the imbalances reinforce each other, and the resulting big tides are called spring tides. (Spring tides are *not* "tides that occur at spring-time"; spring tides happen every two weeks like clockwork.) At the intervening half moons, the imbalances partly cancel and the tides are smaller; these smaller tides are called neap tides. Spring tides have roughly twice the amplitude of neap tides: the spring high tides are twice as high above mean sea level as neap high tides, the spring low tides are twice as low as neap low tides, and the tidal currents are twice as big at springs.

Why are there two high tides and two low tides per day? Well, if the earth were a perfect sphere, a smooth billiard ball covered by oceans, the tidal effect of the earth-moon whirling would be to deform the water slightly towards and away from the moon, making the water slightly rugby-ball shaped (figure 14). Someone living on the equator of this billiard-ball earth, spinning round once per day within the water cocoon, would notice the water level going up and down twice per day: up once as he passed under the nose of the rugby-ball, and up a second time as he passed under its tail. This cartoon explanation is some way from reality. In reality, the earth is not smooth, and it is not uniformly covered by water (as you may have noticed). Two humps of water cannot whoosh round the earth once per day because the continents get in the way. The true behaviour of the tides is thus more complicated. In a large body of water such as the Atlantic Ocean, tidal crests and troughs form but, unable to whoosh round the earth, they do the next best thing: they whoosh around the perimeter of the Ocean. In the North Atlantic there are two crests and two troughs, all circling the Atlantic in an anticlockwise direction once a day. Here in Britain we don't directly see these Atlantic crests and troughs - we are set back from the Atlantic proper, separated from it by a few hun-



Figure 14.1. An ocean covering a billiard-ball earth. We're looking down on the North pole, and the moon is 60 cm off the page to the right. The earth spins once per day inside a rugby-ball-shaped shell of water. The oceans are stretched towards and away from the moon because the gravitational forces supplied by the moon don't perfectly match the required centripetal force to keep the earth and moon whirling around their common centre of gravity.

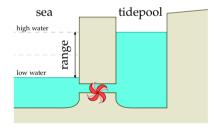
Someone standing on the equator (rotating as indicated by the arrow) will experience two high waters and two low waters per day.

dred miles of paddling pool called the continental shelf. Each time one of the crests whooshes by in the Atlantic proper, it sends a crest up our paddling pool. Similarly each Atlantic trough sends a trough. Consecutive crests and troughs are separated by six hours. Or to be more precise, by six and a bit hours, since the time between moon-rises is about 25, not 24 hours.

The speed at which the crests and troughs travel varies with the depth of the paddling pool. The shallower the paddling pool gets, the slower the crests and troughs travel and the larger they get. Out in the ocean, the tides are just a foot or two in height. Arriving in European estuaries, the tidal range is often as big as four metres. Tidal crests and troughs move up the English channel at roughly 70 km/h. In the northern hemisphere, the Coriolis force (a force, associated with the rotation of the earth, that acts only on moving objects) makes all tidal crests and troughs tend to hug the right-hand bank as they go. For example, the tides in the English channel are bigger on the French side. (That is, the vertical amplitude is bigger.) Similarly the crests and troughs entering the North Sea around the Orkneys hug the British side, travelling down to the Thames estuary then turning left at the Netherlands to pay their respects to Denmark.

Tidal energy is sometimes called lunar energy, since it's mainly thanks to the moon that the water sloshes around so. Much of the tidal energy, however, is really coming from the kinetic energy of the spinning earth. The earth is very gradually slowing down. Each century, the day gets longer by 2.3 milliseconds, thanks to tidal friction. Tidal energy is a renewable that will be available for millions of years.

So, how can we put tidal energy to use?



Tide pools

When you think of tidal power, you might think of an artificial pool next to the sea, with a waterwheel that is turned as the pool fills or empties (figures 14.2 and 14.3). We'll start by estimating the power available from such tide pools, assuming a range of 4 m. (This is a typical range in many European estuaries; in a few special spots – the Severn estuary, Blackpool, and The Wash – the range is sometimes 7 m or more.) The power of an artificial tide pool that's filled rapidly at high tide and emptied rapidly at

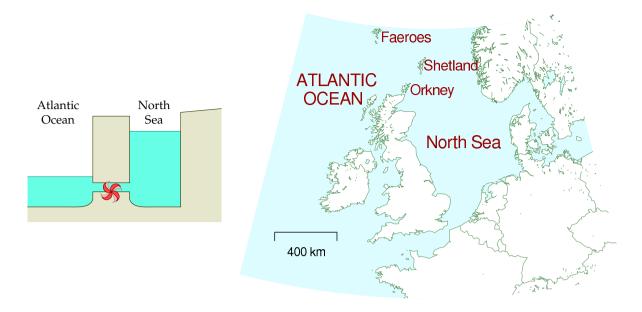


Figure 14.2. Woodbridge tidemill. Photos kindly provided by Ted Evans.

Figure 14.3. An artificial tide pool. The pool was filled at high tide, and now it's low tide. We let the water out through the electricity generator to turn the water's potential energy into electricity.

tidal	power
range	density
2 m	1W/m^2
$4\mathrm{m}$	3W/m^2
6 m	7W/m^2
8 m	$13 \mathrm{W/m^2}$

Table 14.4. Power density of tide-pools, assuming generation from both the rising and the falling tide.



low tide, generating power from both flow directions, is about 3 W/m^2 . This is the same as the power per unit area of an offshore wind-farm. And we already know how big offshore windfarms need to be to make a difference. *They need to be country-sized*. So similarly, to make tidepools capable of producing power comparable to Britain's total consumption, we'd need the total area of the tide pools to be similar to the area of Britain.

Amazingly, Britain is already supplied with a natural tidepool of just the required dimensions. This tidepool is known as the North Sea (figure G.1). All we need to do is insert the generators in appropriate spots, and significant power can be extracted. The generators might look like underwater windmills. Because the density of water is roughly a thousand times that of air, the power of water flow is one thousand times greater than the power of wind at the same speed. We'll come back to tide-farms in a moment, but first let's estimate how much raw tidal energy rolls around Britain every day.

Raw incoming tidal power

The tides around Britain are genuine tidal waves – unlike tsunamis, which are called "tidal waves," but are nothing to do with tides. Follow a high tide as it rolls in from the Atlantic. The time of high tide becomes progressively later as we move east up the English channel from the Isles of Scilly to Portsmouth and on to Dover. The crest of the tidal wave progresses up the channel at about 70 km per hour. (The crest of the wave moves much

Figure 14.5. A natural tide pool. The British Isles are in a fortunate position: the North Sea forms a natural tide pool, in and out of which great sloshes of water pour twice a day.

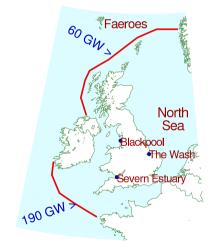


Figure 14.6. The average incoming power of lunar tidal waves crossing these two lines has been measured to be 250 GW. This raw power, shared between 60 million people, is 100 kWh per day per person.

		ower density
(m/s)	(knots)	(W/m^2)
0.5	1	1
1	2	8
2	4	60
3	6	200
4	8	500
5	10	1000

Table 14.7. Tide-farm power density (in watts per square metre of sea-floor) as a function of flow speed. (1 knot = 1 nautical mile per hour = 0.514 m/s.)

faster than the water itself, just like ordinary waves on the sea.) Similarly, a high tide moves clockwise round Scotland, rolling down the North Sea from Wick to Berwick and on to Hull at a speed of about 100 km per hour. These two high tides converge on the Thames Estuary. By coincidence, the Scottish crest arrives about 12 hours later than the crest that came via Dover, so it arrives in near-synchrony with the next high tide via Dover, and London receives the normal two high tides per day.

The power we can extract from tides can never be more than the total power of these tidal waves from the Atlantic. The total power crossing the lines in figure 14.6 has been measured; on average it amounts to 100 kWh per day per person. If we imagine extracting 10% of this incident energy, and if the conversion and transmission processes are 50% efficient, the average power delivered would be 5 kWh per day per person.

This is a tentative first guess, made without specifying any technical details. Now let's estimate the power that could be delivered by three specific solutions: tide-farms, barrages, and offshore tidal lagoons.

Tide farms

One way to extract tidal energy would be to build tide-farms, just like wind-farms. Assuming that the rules for laying out a sensible tide-farm are similar to those for wind-farms, and that the efficiency of the tide turbines will be like that of the best wind turbines, table 14.7 shows the power of a tide-farm for a few tidal currents.

Given that tidal currents of 2 to 3 knots are common, there are many places around the British Isles where the power per unit area of tide-farm would be $6 \, \text{W/m}^2$ or more. This power density can be compared to our estimates of the power densities of wind-farms (2–3 W/m²) and of photovoltaic solar farms (5 W/m²).

Tide power is not to be sneezed at! How would it add up, if we assume that there are no economic obstacles to the exploitation of tidal power at all the hot spots around the UK?

Chapter G estimates 9 kWh/d per person.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

14 — Tide 89

Barrages

The tidal range in the Bristol channel is unusually large. At Cardiff the range is 11.3 m at spring tides, and 5.8 m at neaps. If a barrage were put across the Bristol channel (from Weston super Mare to Cardiff), it would make a 500 km² tide-pool. What power could this tide-pool deliver, if we let the water in and out at the ideal times, generating on both the flood and the ebb? When the range is 11.3 m, the average power contributed by the barrage (at 30 W/m²) would be at most 14.5 GW, or 5.8 kWh/d per person. When the range is 5.8 m, the average power contributed by the barrage (at 8 W/m²) would be at most 3.9 GW, or **1.6 kWh/d per person**. This calculation assumes that the water is let in all in one pulse at the peak of high tide, and let out all in one pulse at low tide. In practice, the in-flow and out-flow would be spread over a few hours, which would reduce the power delivered a little; and the turbines would not extract all the potential energy perfectly: a 10 or 20% loss is likely. The engineers' reports on the proposed Severn barrage say that, generating on the ebb alone, it would contribute 0.8 kWh/d per person on average. The barrage would also provide protection from flooding valued at about £120M per year.

Tidal lagoons

Insert estimates of tidal lagoons here: 64 TWh/y available in six sea locations: Lancashire, North Wales, Lincolnshire, Southwest Wales, East Sussex, and The Wash.64 TWh/y is 7.3 GW, or 3 kWh/d per person.

Beauties of tide

Tide power has never been used on an industrial scale in Britain, so it's hard to know what economic and technical challenges will be raised as we build and maintain tide-turbines – corrosion, silt accumulation, entanglement with flotsam? But here are seven reasons for being excited about tidal power in the British Isles.

- 1. Tidal power is completely predictable. Unlike wind and sun, tidal power is a renewable on which one could depend. It works day and night all year round. Using tidal lagoons, energy can be stored so that power can be delivered on demand.
- 2. Successive high and low tides roll in from the Atlantic and take about 12 hours to progress around the British Isles, so the strongest currents off Anglesey, Islay, Orkney and Dover occur at different times from each other. Thus, together, a collection of tide-farms could produce a more constant contribution to the electrical grid than one tide-farm,

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

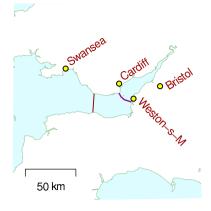


Figure 14.8. Two proposed locations for a Severn barrage. A barrage at Weston-super-Mare would deliver an average power of 2 GW. The outer alternative would deliver twice as much.

Should include maps of good locations of tidal lagoons and diagrams of the two possible flows.

Tide:

albeit a contribution that wanders up and down with the phase of the moon.

- 3. Tidal power will last for millions of years.
- 4. It doesn't require high-cost hardware, in contrast to solar photovoltaic power.
- 5. Moreover, because the power density of a typical tidal flow is greater than the power density of a typical wind, a 60 kW tide turbine would have a smaller size than a 60 kW wind turbine. Perhaps tide turbines could therefore be cheaper than wind turbines.
- 6. Life below the waves is peaceful. There is no such thing as a freak tidal storm. So, unlike wind turbines, which require costly engineering to withstand rare windstorms, underwater tide turbines will not require big safety factors in their design.
- 7. Humans mostly live on the land, and they can't see under the sea, so objections to the visual impact of tide turbines should be less than the objections to wind turbines.

Mythconceptions

"Tidal power is not renewable." "Tidal power, while clean and green, should not be called renewable. Extracting power from the tides slows down the earth's rotation. We definitely can't use tidal power long-term."

False. The natural tides already slow down the earth's rotation. Most tidal power proposals just tap into energy that was about about to be dissipated anyway.

The energy of the spinning earth is 2×10^{29} J. Total world power consumption is 15 TW. If we sucked all this power out of the earth's rotation then even after one million years, the rotational energy of the earth would be reduced by less than 1%.

Natural rotational energy loss is roughly 3 TW [Shepherd, 2003]. Natural slowing rate of the earth's rotation owing to tidal friction is 2.3 ms/day per century. Many tidal energy extraction systems are just extracting energy that would have been lost anyway in bottom friction. But even if we did *double* the energy extracted from the earth–moon system, how long would tidal energy last?

Answer: more than a billion years. In two million years, the length of a day would be longer by two minutes instead of one minute.

11 kWh/d Wave: 4 kWh/d Deep offshore wind: 32 kWh/d Shallow Food & offshore fertilizer: wind: 14 kWh/d 16 kWh/d Gadgets: 5 Light: 4 kWh/d Biomass: food. biofuel, wood, waste incin'n, landfill gas: 24 kWh/d Heating. cooling: 37 kWh/d PV farm $(200 \,\mathrm{m}^2/\mathrm{p})$: 50 kWh/d Jet flights: 30 kWh/d PV, 10 m²: 5 Solar heating: 13 kWh/d Car: 40 kWh/d Wind: 20 kWh/d

Figure 14.9. Tide.

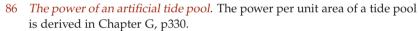
Notes and further reading

page no.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

14 — Tide 91





- 87 Britain is already supplied with a natural tidepool ... known as the North Sea. I should not give the impression that the North Sea fills and empties just like a tidepool on the English coast. The flows in the North Sea are more complex because the time taken for a bump in water level to propagate across the Sea is similar to the time between tides. Nevertheless, there are whopping tidal currents in and out of the North Sea, and within it too.
- 87 The total incoming power of lunar tidal waves crossing these lines has been measured to be 100 kWh per day per person. Cartwright et al. [1980] found by measuring currents and depths along the edge of the continental shelf that the average power transmission was 60 GW between Malin Head (Ireland) and Florø (Norway) and 190 GW between Valentia (Ireland) and the Brittany coast near Ouessant. The power entering the Irish Sea was found to be 45 GW, and entering the North Sea via the Dover Straits, 16.7 GW. For readers who like back-of-envelope models, Chapter G shows how to estimate these powers from first principles.
- 89 The engineers' reports on the Severn barrage...say 17 TWh/year. [Taylor, 2002]. This corresponds to 5% of current electricity consumption (2 GW), on average.

La Rance: generated 16 TWh over 30 years. That's an average power of 60 MW.

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com





Figure 14.10. The Severn barrage proposals (bottom left), and Strangford Lough, Northern Ireland (top left), shown on the same scale as the barrage at la Rance (bottom right). Strangford Lough's area is 150 km²; the tidal range in the Irish Sea outside is 4.5 m at springs and 1.5 m at neaps - sadly not as big as the range at la Rance or the Severn. The raw power of the natural tidepool at Strangford Lough is roughly 150 MW, which, shared between the 1.7 million people of Northern Ireland, comes to 2 kWh/d per person. Strangford Lough is the location of the first grid-connected tidal stream generator in the UK.

Tidal range up to $13.5 \,\mathrm{m}$; impounded area $22 \,\mathrm{km}^2$. Barrage $750 \,\mathrm{m}$ long. Average power density: $2.7 \,\mathrm{W/m^2}$. [6xrm5q]

Turbines are about 90% efficient for heads of $3.7\,\mathrm{m}$ or more. Baker et al. [2006].

The first tidal-stream generator to be connected to the grid was a "300 kW" turbine, installed in 2003 near the northerly city of Hammerfest, Norway. Currents there reach $2.5\,\text{m/s}$. It was expected to generate $80\,\text{kW}$ on average. Detailed power production results have not been published.

15 Stuff

The polluter is not the producer, but rather the consumer.

Dieter Helm

One of the main sinks of energy in the "developed" world is the creation of stuff. In its natural life cycle, stuff passes through three stages. First, a new-born stuff is displayed in shiny packaging on a shelf in a shop. At this stage, stuff is called "goods". As soon as the stuff is taken home and sheds its packaging, it undergoes a transformation from "goods" to its second form, "clutter." The clutter lives with its owner for a period of months or years. During this period, the clutter is largely ignored by its owner, who is off at the shops buying more goods. Eventually, by a miracle of modern alchemy, the clutter is transformed into its final form, rubbish. To the untrained eye, it can be difficult to distinguish this "rubbish" from the highly desirable "good" that it used to be. Nonetheless, at this stage the discerning owner pays the dustman to transport the stuff away.

Let's say we want to understand the full energy-cost of a stuff, with a view perhaps to designing better stuff. This is called life-cycle analysis. It's conventional to chop the energy-cost of anything from a hair-dryer to a cruise-ship into four chunks: [cite Mike Ashby]

Phase R: Making raw materials. This phase involves digging minerals out of the ground, melting them, purifying them, and modifying them into manufacturers' lego: plastics, glasses, metals, and ceramics, for example. The energy costs of this phase include the transportation costs of trundling the raw materials to their next destination.

Phase P: Production. In this phase, the raw materials are processed into a manufactured product. The factory where the hair-dryer's coils are wound, its graceful lines moulded, and its components carefully snapped together, uses heat and light. The energy costs of this phase include packaging and more transportation.

Phase U: Use. Hair-dryers and cruise-ships both guzzle energy when they're used as intended.

Phase D: Disposal. This phase includes the energy cost of putting the stuff back in a hole in the ground (landfill), or of turning the stuff back into raw materials (recycling); and of cleaning up all the pollution associated with the stuff.

To understand how much energy a stuff's life requires, we should estimate the energy costs of all four phases and add them up. Usually one of these four phases dominates the total energy cost, so to get a reasonable estimate of the total energy cost we need accurate estimates only of the



Figure 15.1. Selfridges' rubbish advertisement.

	embodied energy
	(kWh per kg)
fossil fuel	10
wood	5
paper	10
glass	7
PET plastic	30
aluminium	40
steel	6

Table 15.3. Embodied energy of materials.

cost of that dominant phase. If we wish to redesign a stuff so as to reduce its total energy cost, we should usually focus on reducing the cost of the dominant phase, while making sure that energy-savings in that phase aren't being undone by accompanying increases in the energy costs of the other three phases.

Rather than estimating in detail how much energy the production and transport of all stuff costs, let's first cover just a few common examples: drink containers, computers, batteries, junk mail, cars, and houses. This chapter focuses on the energy costs of phases R and P. These energy costs are sometimes called the "embodied" or "embedded" energy of the stuff – slightly confusing names, since usually that energy is neither embodied nor embedded.

Drink containers

Let's assume you have a coke habit: you drink five cans of multinational chemicals per day, and throw the aluminium cans away. For this stuff, it's the raw material phase that dominates. The production of metals is energy intensive, especially for aluminium. Making one aluminium drinks can needs 0.6 kWh. So a five-a-day habit wastes energy at a rate of 3 kWh/d.

As for a 500 ml water bottle made of PET (which weighs 25 g), the embodied energy is is 0.7 kWh – just as bad as an aluminium can!

Other packaging

The average Brit throws away 400 g of packaging per day – mainly food packaging. The embodied energy content of packaging ranges from 7 to 20 kWh per kg as we run through the spectrum from glass and paper to plastics and steel cans. Taking the typical embodied energy content to be 10 kWh per kg, we deduce that the energy footprint of packaging is 4 kWh/d. A little of this embodied energy is recoverable by waste incineration as we'll discuss in Chapter 27.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com



Aluminium: 3 kWh/d

Packaging: 4 kWh/d

Figure 15.2. Five aluminium cans per day is 3 kWh/d. The embodied energy in other packaging chucked away by the average Brit is 4 kWh/d.

<u>15 — Stuff</u> 95

Computers

Making a personal computer costs 250 kg of fossil fuels. So if you buy a new computer every two years, that's 4 kWh per day.

Batteries

I wonder what the energy cost of making AA batteries is?

Here is the answer for a rechargeable nickel-cadmium battery, storing 1Wh of electrical energy and having a mass of 25g. The energy cost of phases R and P is 1.4kWh per AA battery. The energy cost of batteries is thus likely to be a minor item in your stack of energy consumption. Buying and throwing away two AA batteries per month uses 0.1kWh/d.

Newspapers, magazines, and junk mail

A 36-page newspaper, distributed for free at railway stations, weighs 90 g. The Cambridge Weekly News (56 pages) weighs 150 g. The Independent (56 pages) weighs 200 g. A 56-page property-advertising glossy magazine and Cambridgeshire Pride Magazine (32 pages), both delivered free at home, weigh 100 g and 125 g respectively.

This river of reading material and advertising junk pouring through our letterboxes contains energy. It also costs energy to make and deliver. Making newspaper from virgin wood has an energy cost of about 5 kWh per kg, and the paper itself has an energy content similar to that of wood, about 5 kWh per kg. That's a total of 10 kWh embodied energy per kg of paper.

So the energy embodied in a typical personal flow of junk mail, magazines, and newspapers, amounting to 200 g of paper per day – that's equivalent to one Independent per day for example – is about 2kWh per day.

Paper recycling would save about half of the energy of manufacture; waste incineration or burning the paper in a home fire may make use of some of the contained energy.

Bigger stuff

The largest stuff most people buy is a house.

In Chapter H, I estimate the energy cost of making a new house. Assuming we replace each house every 100 years, the estimated energy cost is 2.3 kWh/d. This is the energy cost of the *shell* of the house only – the bricks, tiles, and roof beams. If the average house occupancy is 2.3, the average energy expenditure on house building is thus estimated to be 1 kWh per day per person.

What about a car, and a road? Some of us own the former, but we usually share the latter. A new car's embodied energy is 76 000 kWh – so if

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

Chips: 4 kWh/d



Figure 15.4. She's making chips. Photo: ABB.

Making one personal computer every two years costs 4 kWh/d.



Newspapers, junk mail, magazines: 2 kWh/d

House-building: 1kWh/d

Car-making: 14 kWh/d





Figure 15.5. Food-miles – Pasties, hand-made in Helston, Cornwall, shipped 360 miles for consumption in Cambridge.

you get one every 15 years, that's an average energy cost of $14 \, \text{kWh}$ per day. A life-cycle analysis by Treloar, Love, and Crawford estimates that building an Australian road costs $7600 \, \text{kWh}$ per metre (a continuously reinforced concrete road), and, including maintenance costs, the total cost over 40 years was $35\,000 \, \text{kWh}$ per metre. Let's turn this into a ballpark figure for the energy cost of British roads. There are $28\,000 \, \text{miles}$ of trunk roads and class-1 roads in Britain (excluding motorways). Assuming $35\,000 \, \text{kWh}$ per metre per 40 years, those roads cost us $2 \, \text{kWh/d}$ per person. For a second estimate, the Bath inventory of carbon and energy says that the embodied energy of a road is $2700 \, \text{MJ/m}^2$.

Road-building: 2 kWh/d

Transporting the stuff

Transport of stuff by road

HGVs do 2 miles per litre. (10 mpg) Total road transport in Britain by heavy goods vehicles was 156 billion t-km in 2006. Shared between 60 million, that comes to 2500 t-km per person per year, or (assuming 1 kWh per ton-km) 7 kWh per day per person. (In this chapter's notes I derive 1.06 kWh/tkm for UK road freight.) One quarter of the transport, by the way, was of food, drink and tobacco.

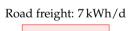


Figure 15.6. The lorry delivereth and the lorry taketh away. Energy cost of UK road freight: 7 kWh/d per person.

Transport by water

International shipping (2002, UK share – 560 million tons of freight): 7.5 Mtoe [Anderson et al., 2006] (6.2 MtC, 23 Mt CO₂). So 4 kWh/d per person.

Shipping: 4 kWh/d

Figure 15.7. Energy cost of the UK's share of international shipping.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com



15 — Stuff 97

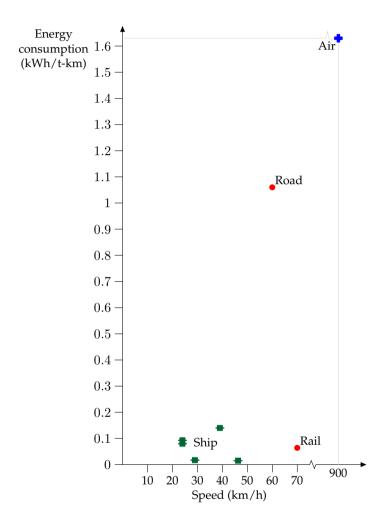


Figure 15.9. Energy requirements of different forms of freight-transport. The vertical coordinate shows the energy consumed in kWh per net ton-km, (that is, the energy per t-km of freight moved, not including the weight of the vehicle). See also figure 20.23 (energy requirements of passenger transport).





Water transport requires energy because boats make waves. Nevertheless, transporting freight by ship is surprisingly energy efficient.





Figure 15.11. Part of the reverse-osmosis facility at Jersey Water's desalination plant. The pump in the foreground has a power of 355 kW and shoves seawater at a pressure of 65 bar into 39 spiral-wound membranes in the banks of blue horizontal tubes, top, delivering 1500 m³ per day of clean water. The clean water from this facility has a total energy cost of 8 kWh per m³.

Transport of water; taking the pee

Water's not a very glamorous stuff, but we use a lot of it – about 160 kg per day per person. In turn, we provide about 160 l per day per person of sewage to the water companies. The cost of pumping water around the country and treating our sewage is about 0.4 kWh per day per person.

Desalination

At the moment the UK doesn't spend energy on water desalination. But there's talk of creating desalination plants in London. What's the energy cost of turning salt water into drinking water? The least energy-intensive method for desalination is reverse osmosis. Take a membrane that lets through only water, put salt water on one side of it, and pressurize the salt water. Water reluctantly oozes through the membrane, producing purer water – reluctantly, because pure water separated from salt has low entropy, and nature prefers high entropy states where everything is mixed up. We must pay high-grade energy to achieve unmixing.

The Island of Jersey has a desalination plant that can produce $6000\,\mathrm{m}^3$ of pure water per day figure 15.11. Including the pumps for bringing the water up from the sea and through a series of filters, the whole plant uses a power of 2 MW. That's an energy cost of 8 kWh per cubic meter of water produced.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

Water delivery and removal: 0.4 kWh/d

Figure 15.10. Water delivery: 0.3 kWh/d; sewage processing: 0.1 kWh/d.

At a cost of 8 kWh per m³, a daily water consumption of 160 l would require 1.3 kWh per day.)

Stuff retail

Supermarkets currently consume about 11 TWh of energy per year and have a carbon footprint of 4.1 Mt CO₂ (3% of all UK emissions). [yqbz13]

Shared out equally between 60 million happy shoppers, that's a power of $0.5 \, \text{kWh/d}$ per person. These numbers don't quite add up? Presumably the energy figure is just electricity, and the CO_2 figure includes some other forms of energy?

The significance of imported stuff

In standard accounts of "Britain's primary energy consumption" or "Britain's carbon footprint," imported goods are *not* counted. Britain used to make its own gizmos, and our per-capita footprint in 1910 was as big as America's is today. Now Britain doesn't manufacture so much (so our energy consumption and carbon emissions have dropped a bit), but we still love gizmos, and we get them made for us by other countries. Should we ignore the energy cost of making the gizmo, because it's imported? I don't think so. Dieter Helm and his colleagues in Oxford estimate that under a correct account, allowing for imports and exports, Britain's carbon footprint is nearly *doubled* from the official "11 tons $CO_2^{(e)}$ per person" to about 21 tons. This implies that the biggest item in the average British person's energy footprint is the energy cost of making imported stuff.

In Chapter H, I explore this idea further, by looking at the weight of Britain's imports. Leaving aside our imports of fuels, we import a little over two tons per person of stuff every year, of which about 1.3 tons per person are processed and manufactured stuff like vehicles, machinery, white goods, and electrical and electronic equipment. Such goods are mainly made of materials whose production required at least 10 kWh of energy per kg of stuff. I thus estimate that this pile of cars, fridges, microwaves, computers, photocopiers and televisions has an embodied energy of at least 40 kWh per day per person.

To summarize all these forms of stuff and stuff-transport, I will put on the consumption stack 48 kWh per day per person for the making of stuff (made up of at least 40 for imports, 2 for a daily newspaper, 2 for road-making, 1 for house-making, and 3 for packaging); and another 12 kWh per day per person for the transport of the stuff by sea and by road, and the storing of food in supermarkets.

Work till you shop.

Traditional saying

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

Supermarkets: 0.5 kWh/d

99

Figure 15.12. Shops.

Transporting stuff: 12 kWh/d Tide: 11 kWh/d Wave: 4 kWh/d Stuff: 48+ kWh/d Deep offshore wind: 32 kWh/d Shallow Food & offshore fertilizer: wind: 14 kWh/d 16 kWh/d Gadgets: 5 Light: 4 kWh/d Biomass: food, biofuel, wood, waste incin'n, landfill gas: 24 kWh/d Heating, cooling: 37 kWh/d PV farm $(200 \,\mathrm{m}^2/\mathrm{p})$: 50 kWh/d Jet flights: 30 kWh/d PV, 10 m²: 5 Solar heating: 13 kWh/d Car: 40 kWh/d Wind: 20 kWh/d

Figure 15.13. Making our stuff costs at

Notes and further reading

page no.

- One aluminium drinks can costs 0.6 kWh. The mass of one can is 15 g. Estimates of the total energy cost of aluminium manufacture vary from 60 MJ/kg to 300 MJ/kg. [yx7zm4], [r22oz], [yhrest]. The figure I used is from The Aluminum Association [y5as53]: 150 MJ per kg of Aluminium (40 kWh/kg). The energy cost of electrolysing Aluminium ore to produce Aluminium is about 15 kWh/kg (54 MJ/kg). In addition, the electrolysis burns up carbon electrodes: 1.5 to 2.2 tons of carbon dioxide are emitted for each ton of aluminum produced. If we value the electrodes at 27 GJ/ton of carbon (the same as coal), the electrodes are worth another 3–4.4 kWh/kg of aluminium. The remaining 80 MJ/kg in the Aluminum Association figure of 150 MJ per kg presumably comes from mining, processing and transport.
- The embodied energy of a water bottle made of PET. Source: Hammond and Jones [2006] – PET's embodied energy is 106.5 MJ per kg, which is 30 kWh per kg.
- 1995: 137 kg packaging used per person Hird et al. [1999]. 25 million tons of waste was produced in 1997 in the UK and a third of this was food packaging. That's a number worth remembering: Waste production: 400 kg per person per year, or roughly 1 kg per day.
 Dajnak and Lockwood [2000] says 490 kg of municipal solid waste per urban inhabitant in the UK in 1996. Four tons of municipal solid waste (MSW) contains as much energy as 1 ton of coal − 8000 kWh of heat. Gross calorific value of MSW: 1.8–2.8 kWh/kg. Electricity produced: 1–1.4 kWh/kg. 200 000 t MSW per year → 21.5 MW.
 Embodied energy of glass is 7 kWh/kg. Source: Prof. M. Ashby, CUED.
- 95 A personal computer costs 250 kg of fossil fuels. Manufacture of a PC requires (in energy and raw materials) the equivalent of about 10 times its own weight of fossil fuels. Fridges, cars, etc generally take 1-2 times their weight.
- a rechargeable nickel-cadmium battery. This estimate is from Rydh and Karlström [2002].
- 94 steel... From Swedish Steel, "The consumption of coal and coke is 700 kg per ton of finished steel, equal to approx. 5320 kWh per ton of finished steel. The consumption of oil, LPG and electrical power is 710 kWh per ton finished product. Total [primary] energy consumption is thus approx. 6000 kWh per ton finished steel." (6 kWh per kg.) [y2ktgg] Corus say they use 18 GJ/ton of steel (5 kWh/kg) [y55ppn].
- 95 A new car's embodied energy is 76 000 kWh. [Treloar et al., 2004]. Burnham et al. [2007] give a lower figure: 30 500 kWh for the net life-cycle energy cost of a car. One reason for the difference may be that the latter life-cycle analysis assumes the vehicle is recycled, thus reducing the net materials cost.
- (c) David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

Making newspaper from virgin wood has an energy cost of about 5 kWh per kg. Energy costs vary between mills and between countries. 5 kWh per kg is the figure for a Swedish newspaper mill in 1973 from Norrström [1980], who estimated that efficiency measures could reduce the cost to about 3.2 kWh per kg – part heat, part electricity. A more recent full lifecycle analysis [Denison, 1997] estimates the net energy cost of production of newsprint in the USA from virgin wood followed by a typical mix of landfilling and incineration to be 12 kWh/kg; the energy cost of producing newsprint from recycled material and recycling it is 6 kWh/kg. From a greenhouse-gas point of view, incidentally, the worst paper-chain of all is virgin paper production followed by landfilling: in landfill about half of the paper's carbon is turned into methane, which is a stronger greenhouse gas than CO₂.

- 95 the paper itself has an energy content similar to that of wood. Source: Ucuncu [1993], Erdincler and Vesilind [1993]; see p306.
- Water delivery and sewage treatment costs 0.4 kWh/d per person. The total energy use of the water industry in 2005–6 was 7703 GWh. Supplying 1 cubic metre (1 ton) of water has an energy cost of 0.59 kWh. Treating 1 cubic metre (1 ton) of sewage has an energy cost of 0.63 kWh. For anyone interested in greenhouse-gas emissions, water supply has a footprint of 289 g per cubic metre of water delivered, and wastewater treatment, 406 g per cubic metre of wastewater.
 - Domestic water consumption is 151 l per day per person. Total water consumption is 13 234 Ml per day, which is 221 l per day per person. Leakage amounts to 3418 Ml per day (571 per day per person).
 - Sources: Parliamentary Office of Science and Technology http://www.parliament.uk/documents/upload/postpn282.pdf, Water UK [2006].
- 97 Figure 15.9. Energy consumptions of ships. The five points in the figure are a container ship (46 km/h), a dry cargo vessel (24 km/h), an oil tanker (29 km/h), an inland marine ship (24 km/h), and the NS Savannah (39 km/h).
 - Dry cargo vessel 0.08 kWh/tkm. 3360 deadweight tons. (Deadweight tonnage is the mass of cargo that the ship can carry.) http://conoship.com/uk/vessels/detailed/page7.htm Length: 91 m, breadth 14 m, draught: 5 m. Speed 13 kn (24 km/h), one engine with 2 MW delivered power has a fuel-oil consumption of 186 g per kWh of delivered energy (42% efficiency). Grain capacity: 5200 m³.
 - Oil tanker A modern oil tanker uses 0.017 kWh/tkm. [61brab] Cargo weight 40 000 t. Capacity: 47 000 m³. Main engine: 11.2 MW maximum delivered power. Speed at 8.2 MW: 15.5 kn (29 km/h). Length 188 m, width 32 m. Draught: 10 m. Marine engine efficiencies are about 42%. The energy of the cargo is 520 × 10⁶ kWh. So 1% of the energy is lost is transporting it one-quarter of the way round the earth (10 000 km).
 - **Roll-on, roll-off carriers** The ships of Wilh. Wilhelmsen shipping company, deliver freight-transport with an energy cost between 0.028 and 0.05 kWh per t-km

99 Helm et al. suggest that, allowing for imports and exports, Britain's carbon footprint is nearly doubled to about 21 tons. Helm et al. [2007].

Plastics [354euo] In the UK, a total of approximately 4.7 million tons of plastic products were used in 2001 (78 kg per year per person; 200 g per day). 4% of the world's oil production is used as a feedstock for plastics production and an additional 3-4% during manufacture.

So the energy footprint of plastic stuff used in Britain is 8kWh/d per person.



16 Geothermal

Geothermal energy comes from two sources: from radioactive decay in the crust of the earth, and from heat trickling through the mantle from the earth's core. The heat in the core is there because the earth used to be redhot, and it's still cooling down; the heat in the core is also being topped up by tidal friction: the earth flexes in response to the gravitational fields of the moon and sun, in the same way that an orange changes shape if you squeeze it and roll it between your hands.

Geothermal is an attractive renewable because it is 'always on', independent of the weather; if we make geothermal power stations, we can switch them on and off so as to follow demand.

But how much geothermal power is available? We could estimate geothermal power of two types: the power available at an ordinary location on the earth's crust; and the power available in special hot spots like Iceland. While the right place to first develop geothermal technology is definitely the special hot spots, I'm going to assume that the greater total resource comes from the ordinary locations, since ordinary locations are so much more numerous.

The difficulty with making *sustainable* geothermal power is that the speed at which heat travels through solid rock limits the rate at which heat can be sustainably sucked out of the red-hot interior of the earth. It's like trying to drink a crushed-ice drink through a straw. You stick in the straw, and suck, and you get a nice mouthful of cold liquid. But after a little more sucking, you find you're sucking air. You've extracted all the liquid from the ice around the tip of the straw. Your initial rate of sucking wasn't sustainable.

If you stick a straw down a 15 km hole in the earth, you'll find it's nice and hot there, easily hot enough to boil water. So, you could stick two straws down, and pump cold water down one straw and suck from the other. You'll be sucking up steam, and you can run a power station. Limitless power? No. After a while, your sucking of heat out of the rock will have reduced the temperature of the rock. You weren't sucking sustainably. If you stop sucking, you now have a long wait before the rock at the tip of your straws warms up again. A possible attitude to this problem is to treat geothermal heat the same way we currently treat fossil fuels: as a resource to be mined rather than collected sustainably. Living off geothermal heat in this way might be better for the planet than living unsustainably off fossil fuels; but perhaps it would only be another stop-gap giving us another 100 years of unsustainable living? Let's do the sums. In this book I'm most interested in *sustainable* energy, as the title hinted.

First imagine using geothermal energy sustainably by sticking down straws to an appropriate depth, and sucking *gently*. Suck at such a rate that the rocks at the end of the our straws don't get colder and colder. This



Figure 16.1. Geothermal power in Iceland. Average geothermal electricity generation in Iceland (population, 300 000) in 2006 was 300 MW (24 kWh/d/person). More than half of Iceland's electricity is used for aluminium extraction. Photo by Gretar Ívarsson.

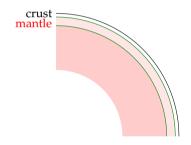


Figure 16.2. An earth in section, yesterday.

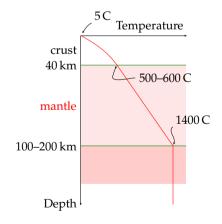


Figure 16.3. Temperature profile in a typical continent.

means sucking at the natural rate at which heat is already flowing out of the earth.

As I said before, geothermal energy comes from two sources: from radioactive decay in the crust of the earth, and from heat trickling through the mantle from the earth's core.

In a typical continent, the heat flux from the centre coming through the mantle is about $10\,\text{mW/m}^2$. The heat flux at the surface is $50\,\text{mW/m}^2$. So the radioactive decay has added an extra $40\,\text{mW/m}^2$ to the heat flux from the centre.

So at a typical location, the maximum power we can get per unit area is 50 mW/m². But that power is not high-grade power, it's low-grade heat that's trickling through at room temperature. We presumably want to make electricity, and that's why we must drill down. Heat is useful only if it comes from a source at a higher temperature than room temperature. The temperature increases with depth as shown in figure 16.3, reaching a temperature of about 500 °C at a depth of 40 km. Between depths of 0 km where the heat-flow is biggest but the rock temperature is too low, and 40 km, where the rocks are hottest but the heat flux is five times smaller (because we're missing out on all the heat generated from radioactive decay) there is an optimal depth at which we should suck. The exact optimal depth depends on what sort of sucking and power-station machinery we use. We can bound the maximum power sustainably deliverable by geothermal energy by finding the optimal depth assuming that we have an ideal engine for turning heat into electricity, and that drilling to any depth is free.

For the temperature profile shown in figure 16.3, the optimal depth is about 15 km. Under these conditions, an ideal heat engine would deliver 17 mW/m². At the world population density of 43 people per square km, that's 10 kWh per person per day, if *all* land area were used. In the UK, the population density is 5 times greater, so widescale geothermal power of this sustainable-forever variety could offer at most 2 kWh per person per day.

This is the sustainable-forever figures, ignoring hot spots, assuming perfect power stations, assuming every square metre of continent is exploited, and assuming that drilling is free. And that it is possible to drill 15-kilometre-deep holes.

The other geothermal strategy is to treat the heat as a resource to be mined. In "enhanced geothermal extraction" from hot dry rocks, we first drill down to a depth of 5 or 10 km, and fracture the rocks by pumping in water. (This step may create earthquakes, which don't go down well with the locals.) Then we drill a second well into the fracture zone. Then we pump water down one well and extract superheated water or steam from the other. This steam can be used to make electricity or to deliver heat. What's the hot dry rock resource of the UK? Sadly, Britain's not well endowed. Most of the hot rocks are concentrated in Cornwall, where some



Figure 16.4. Some granite, yesterday.

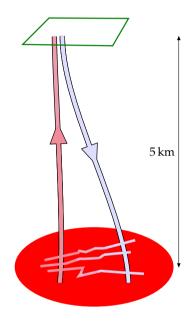


Figure 16.5. Enhanced geothermal extraction from hot dry rock. One well is drilled and pressurised to create fractures. A second well is drilled into the far side of the fracture zone. Then cold water is pumped down one well and heated water (indeed, steam) is sucked up the other

geothermal experiments were carried out in 1985 in a research facility at Rosemanowes, now closed down. Consultants assessing these experiments concluded that "generation of electrical power from hot dry rock was unlikely to be technically or commercially viable in Cornwall, or elsewhere in the UK, in the short or medium term."Nonetheless, what is the resource? The biggest estimate of the hot dry rock resource in the UK is a total energy of 130 000 TWh, which could conceivably contribute 1.1 kWh per day per person of electricity for about 800 years.

Other places in the world have more promising hot dry rocks, so if you want to know the geothermal answers for other countries, be sure to ask a local. But sadly for Britain, geothermal will only ever play a bit part.

Doesn't Southampton use geothermal energy already? How much does that deliver?

Yes, Southampton Geothermal District Heating Scheme was, in 2004 at least, the only geothermal heating scheme in the UK. It provides the city with a supply of hot water. The geothermal well is part of a combined heat, power, and cooling system that delivers hot and chilled water to customers, and sells electricity to the grid. Geothermal energy contributes about 15% of the heat delivered by this system. Their CHP system produces 70 GWh of energy per year. The population of Southampton at the last census was 217 445, so the geothermal power being delivered there is **0.13 kWh/d** per person in Southampton.

Notes and further reading

page no.

- The heat flux at the surface is 50 mW/m². (Massachusetts Institute of Technology [2006] says 59 mW/m² average, with a range, in the USA, from 25 mW to 150 mW.) Shepherd [2003] says 63 mW/m².
- "Generation of electrical power from hot dry rock was unlikely to be technically or commercially viable in the UK". Source: MacDonald et al. [1992]. See also Richards et al. [1994].
 - The biggest estimate of the hot dry rock resource in the UK ... could conceivably contribute 1.1 kWh per day per person of electricity for about 800 years. Source: MacDonald et al. [1992].
 - Other places in the world have more promising hot dry rocks. There's a good MIT study [Massachusetts Institute of Technology, 2006] describing the American hot dry rock resource. http://web.mit.edu/newsoffice/2007/geothermal.html. Another more speculative approach, researched by Sandia Labs in the 1970s, is to drill all the way down to magma at temperatures of 600–1300 °C, and get power there. The website www.magma-power.com reckons that the heat in pools of magma under the US would cover US energy consumption for 500 or 5000 years, and that it could be extracted economically.

Transporting stuff: 12 kWh/d Geothermal: 1kWh/d Tide: 11 kWh/d Wave: 4kWh/d Stuff: 48+ kWh/d Deep offshore wind: 32 kWh/d Shallow Food & offshore fertilizer: wind: 14 kWh/d 16 kWh/d Gadgets: 5 Light: 4 kWh/d Biomass: food, biofuel, wood, waste incin'n, landfill gas: Heating, 24 kWh/d cooling: 37 kWh/d PV farm $(200 \,\mathrm{m}^2/\mathrm{p})$: 50 kWh/d Jet flights: 30 kWh/d PV, 10 m²: 5 Solar heating: 13 kWh/d Car: 40 kWh/d Wind: 20 kWh/d

Figure 16.6. Geothermal.

- Southampton Geothermal District Heating Scheme. www.southampton.gov.uk.





Figure 16.8. More geothermal power in Iceland. Photo by Rosie Ward.

17 Public services

Every gun that is made, every warship launched, every rocket fired signifies, in the final sense, a theft from those who hunger and are not fed, those who are cold and are not clothed.

This world in arms is not spending money alone. It is spending the sweat of its laborers, the genius of its scientists, the hopes of its children.

President Dwight D. Eisenhower - April, 1953

The energy cost of "defence"

Let's try to estimate how much energy we spend on our military.

In 2007–8, the fraction of British central government expenditure that went to defence was £33 billion/£587 billion = 6%. If we include the UK's spending on counter-terrorism and intelligence (£2.5 billion per year and rising), the total for defensive activities comes to £36 billion.

As a crude estimate we might guess that 6% of this £36 billion is spent on energy at a cost of 2.7p per kWh. (6% is the fraction of GDP that is spent on energy, and 2.7p is the average price of energy.) That works out to about 80 TWh per year of energy going into defence: making bullets, bombs, nuclear weapons; making devices for delivering bullets, bombs, and nuclear weapons; and roaring around keeping in trim for the next game of good–against–evil. In our favourite units, this corresponds to 4kWh per day per person.

The cost of nuclear defense

The financial expenditure by the USA on manufacturing and deploying nuclear weapons from 1945 to 1996 was \$5.5 trillion (in 1996 dollars).

Nuclear weapons spending over this period exceeded the combined total federal spending for education; agriculture; training, employment, and social services; natural resources and the environment; general science, space, and technology; community and regional development (including disaster relief); law enforcement; and energy production and regulation.

If again we assume that 6% of this expenditure went to energy at a cost of 5¢ per kWh, we find that the energy cost of having nuclear weapons was 26 000 kWh per American, or **1.4 kWh per day per American** (shared among 250 million Americans over 51 years). [I use 250 million rather than the current 300 million to represent the typical USA population during 1945–1996.]

What energy would have been delivered to the lucky recipients, had all those nuclear weapons been used? The energies of the biggest thermonu-





"Defence": 4

Figure 17.1. The energy cost of defence in the UK is estimated to be about 4 kWh per day per person.

clear weapons developed by the USA and USSR are measured in megatons of TNT. A ton of TNT is 4.2 gigajoules or 1200 kWh. The bomb that destroyed Hiroshima had the energy of 15 000 tons of TNT or 15 *kilotons* (18 million kWh). A *megaton* bomb delivers an energy of 1.2 billion kWh. If dropped on a city of one million, a megaton bomb makes an energy donation of 1200 kWh per person, equivalent to 120 litres of petrol per person. The total energy of the USA's nuclear arsenal today is 2400 megatons, contained in 10 000 warheads. In the good old days when folks really took defense seriously, it was 20 000 megatons. These bombs, if used, would have delivered an energy of about 100 000 kWh per American.

That's equivalent to 7 kWh per day per person for a duration of 40 years – similar to all the electrical energy supplied to America by nuclear power.

Energy cost of making nuclear materials for bombs

Plutonium production: the most efficient plutonium-production facilities produce 1 gram of plutonium per megawatt day (thermal). [slbae]. So the direct energy-cost of making the USA's 104 tons of plutonium (1945–1996) was at least 2.5×10^{12} kWh which is 0.5 kWh/d per person (assuming 250 million Americans).

A SWU (separative work unit) is a unit of measurement used in the nuclear power industry. It measures the work needed to separate the U-235 and U-238 atoms in natural uranium in order to create a final product that is richer in U-235. Material enriched to between 4% and 5% U-235 is called low-enriched uranium (LEU). 90%-enriched uranium is called highenriched uranium (HEU). It typically takes three times as much work to enrich uranium from its natural state to 5 percent LEU as it does to enrich LEU to 90 percent HEU. If you begin with 100 kilograms of natural uranium, it takes about 60 SWU to produce 10 kilograms of uranium enriched in U-235 content to 4.5%. To produce a kilogram of U-235 as HEU takes 232 SWU. To make 1 kg of U-235 as LEU (in 22.7 kg of LEU) takes about 151 SWU. In both cases one starts from natural uranium (0.71% U-235) and discards depleted uranium with 0.25 percent U-235.

The commercial nuclear fuel market values an SWU at about \$100. It takes about 100000 SWU of enriched uranium to fuel a typical 1000 megawatt (MW) commercial nuclear reactor for a year. [yh45h8]

Two uranium enrichment methods are currently in commercial use: gaseous diffusion and gas centrifuge.

The gaseous diffusion process consumes about 2500 kWh per SWU, while modern gas centrifuge plants require only about 50 kWh per SWU. [t2948]

A modern centrifuge produces about 3 SWU per year.

OK, so the USA's production of 994 tons of highly-enriched uranium (the USA's total, 1945–1996) cost 230 million SWU, which was 0.1 kWh/d per person (assuming 250 million Americans). [Using 2500 kWh/SWU as

17 — Public services 109

the cost of diffusion enrichment.]

Arguments

"Trident creates jobs." Well, so does relining our schools with asbestos, but that doesn't mean we should do it!

Marcus Brigstocke

Universities

According to Times Higher Education Supplement (March 30th 2007), UK universities use 5.2 billion kWh per year. Shared out among the whole population, that's a power of 0.24 kWh per day per person.

Notes and further reading

page no.

of which defence is £33.4 billion [fcqfw] and intelligence and counterterrorism: [2e4fcs]. According to page 14 the Government's Expenditure Plans 2007/08 [33x5kc], the "total resource budget" of the Department of Defence is a bigger sum, £39 billion, of which £33.5 billion goes for "provision of defence capability" and £6 billion for armed forces pay and pensions and war pensions. A breakdown of this budget can be found here: [35ab2c]. [yg5fsj] [yfgjna]

The US military's energy consumption is known: "The Department of Defense is the largest single consumer of energy in the United States. In 2006, it spent \$13.6 billion to buy 110 million barrels of petroleum fuel [roughly 190 billion kWh] and 3.8 billion kWh of electricity" Department of Defense [2008]. This figure describes the direct use of fuel and electricity and doesn't include the embodied energy in the military's toys. Dividing by the population of 300 million, it comes to 1.7 kWh/d per person.

- The financial expenditure by the USA on manufacturing and deploying nuclear weapons from 1945 to 1996 was \$5.5 trillion (in 1996 dollars). http://www.brook.edu/fp/projects/nucwcost/schwartz.htm.



18 Can we live on renewables?

A close race! But please remember: in calculating our production stack we threw all economic, social, and environmental constraints to the wind. Also, some of our green contributors are probably incompatible with each other: our photovoltaic panels and hot-water panels would clash with each other on roofs; and our solar photovoltaic farm using 5% of the country might compete with our energy crops with which we covered 75% of the country. If we were to lose just one of our bigger green contributors – for example, if we decided that deep offshore wind is not an option, or that panelling 5% of the country with photovoltaics at a cost of £200 000 per person is not on – then the production stack would no longer match the consumption stack.

Furthermore, even if our red consumption stack were lower than our green production stack, it would not necessarily mean our energy sums are adding up. You can't power a TV with cat food, nor can you feed a cat on electricity from a wind turbine. Energy exists in different forms – chemical, electrical, kinetic, and heat, for example. For a sustainable energy plan to add up, we need the forms and amounts of energy consumption and production to match up. Converting energy from one form to another – from chemical to electrical, as at a power station, or from electrical to chemical, as in a factory making hydrogen from water – usually involves substantial losses of useful energy. We will come back to this important detail in a later chapter, which will describe some energy plans that do add up.

In this chapter we'll reflect on our estimates of consumption and production, compare them with official averages and with other people's estimates, and discuss what renewables could plausibly deliver in a country like Britain.

The questions we'll address in this chapter are

- 1. Is the size of the red stack roughly correct? What is the *average* consumption of Britain? We'll look at the official energy-consumption numbers for Britain and a few other countries.
- 2. Have I been unfair to renewables, underestimating their potential? We'll compare the estimates in the green stack with estimates published by organizations such as the Sustainable Development Commission, the Institution of Electrical Engineers, and the Centre for Alternative Technology.
- 3. What happens to the green stack when we take into account social and economic constraints?

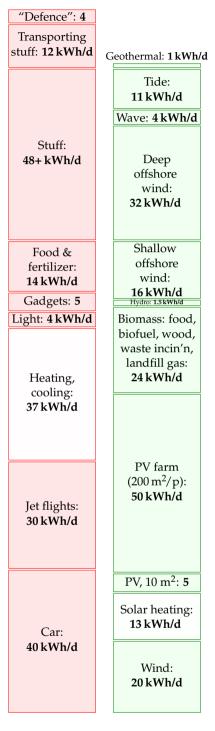


Figure 18.1. The state of play after we added up all the traditional renewables.

Road transport	Petroleum	22.5
Railways	Petroleum	0.39
Water transport	Petroleum	0.96
Aviation	Petroleum	7.4
All modes	Electricity	0.39
All energy used by transport		31.6

Table 18.4. 2006 breakdown of energy consumption by transport mode, in kWh/d per person.

Source: Department for Transport [2007].

Red reflections

Our estimate of a typical affluent person's consumption has reached 200 kWh per day. It is indeed true that many people use this much energy, and that many more aspire to such levels of consumption. The *average* American consumes about 250 kWh per day. If we all raised our standard of consumption to an average American level, the green production stack would definitely be dwarfed by the red consumption stack.

What about the average European and the average Brit? Average European consumption of "primary energy" is about 125 kWh per day per person. The UK average is also 125 kWh per day per person.

These official averages do not include two energy flows: First, the "embedded energy" in imported stuff (the upstream energy expended in making the stuff) is not included at all. We estimated in Chapter 15 that the embedded energy in imported stuff is at least $40\,\mathrm{kWh/d}$ per person. Second, the official estimates of "primary energy consumption" only include industrial energy flows – things like fossil fuels and hydroelectricity – and don't keep track of the natural embedded energy in food: energy that was originally harnessed by photosynthesis.

Another difference between the red stack we slapped together and the national total is that in most of the consumption chapters so far we tended to ignore the energy lost in converting energy from one form to another, and in transporting energy around. The national total accounts for all the energy, before any conversion losses. Conversion losses in fact account for about 22% of total national energy consumption. Most of these conversion losses happen at power stations. Losses in the electricity transmission network chuck away 1% of total national energy consumption.

When building our red stack, we tried to imagine how much energy a typical affluent person uses. Has this approach biased our perception of the importance of different activities? Let's look at some official numbers. Figure 18.2 shows the breakdown of energy consumption by end use. Table ?? gives the breakdown of final energy consumption by sector.

Let's look more closely at transport. In our red stack, we found that the energy footprints of driving a car 50 km per day and of flying to Los Angeles once per year are roughly equal. Table ?? shows the relative importances of the different transport modes in the national balance-sheet.

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com



Figure 18.2. Energy consumption, broken down by end use.

Transport	33%
Domestic	28%
Industry	19.5%
Commerce	6%
Non-energy use	7%

Table 18.3. Breakdown of final energy consumption by sector.

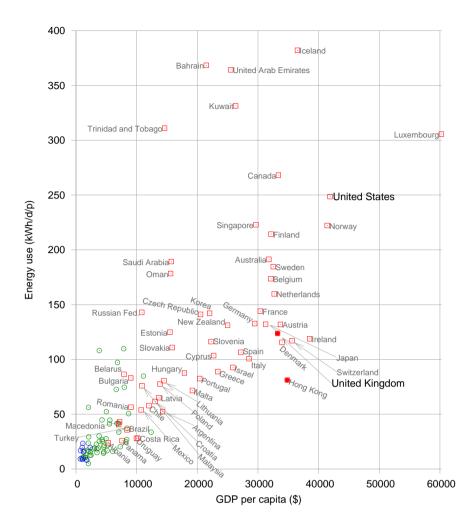


Figure 18.5. Energy consumption per capita, versus GDP per capita, in purchasing-power-parity US dollars. Squares show countries having "high human development;" circles, "medium" or "low." Figure 18.6 shows the same data on logarithmic scales.

Figure 18.5 shows the energy consumptions of lots of countries, versus their gross domestic products (GDPs). Figure 18.6 shows the same data on logarithmic scales.

Green reflections

People often say that Britain has plenty of renewables. Have I been mean to green? Are my numbers a load of rubbish? Have I underestimated sustainable production? Let's compare my green numbers first with several estimates found in the Sustainable Development Commission's publication *The role of nuclear power in a low carbon economy. Reducing CO*₂ *emissions* – *nuclear and the alternatives*. Remarkably, even though the Sustainable Development Commission's take on sustainable resources is very positive ("We have huge tidal, wave, biomass and solar resources"), *all the estimates*

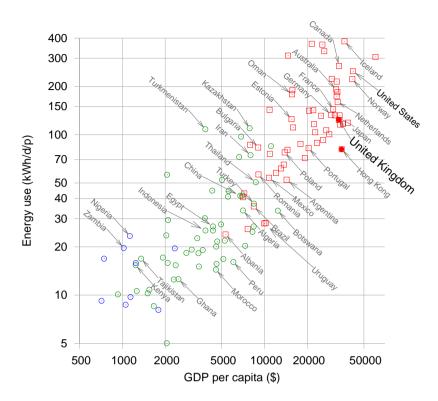


Figure 18.6. Energy consumption per capita versus GDP per capita, in purchasing-power-parity US dollars. Data from UNDP Human Development Report, 2007. Squares show countries having "high human development;" circles, "medium" or "low." Both variables are on logarithmic scales. Figure 18.5 shows the same data on normal scales.

in the Sustainable Development Commission's document are smaller than mine! (To be precise, all the estimates of the renewables total are smaller than my total.) Figure 18.7 shows numbers from the Sustainable Development Commission's publication and other sources, alongside my estimates.

IEE The Institute of Electrical Engineers published a report on renewable energy in 2002 – a summary of possible contributions from renewables in the UK. The second column of figure 18.7 shows the "technical potential" of a variety of renewable technologies for UK electricity generation – "an upper limit that is unlikely ever to be exceeded even with quite dramatic changes in the structure of our society and economy".

According to the IEE, the total of all renewables' technical potential is about 27 kWh/d per person. Their figures for biomass and wave all agree with mine; their estimates for tide and wind are quite a lot smaller than mine; The only figure in their list that is bigger than mine is geothermal, presumably because they did not impose the "sustainable" constraint that I did.

Tyndall The Tyndall Centre's estimate of the total practicable renewable-energy resource is 15 kWh per day per person.

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

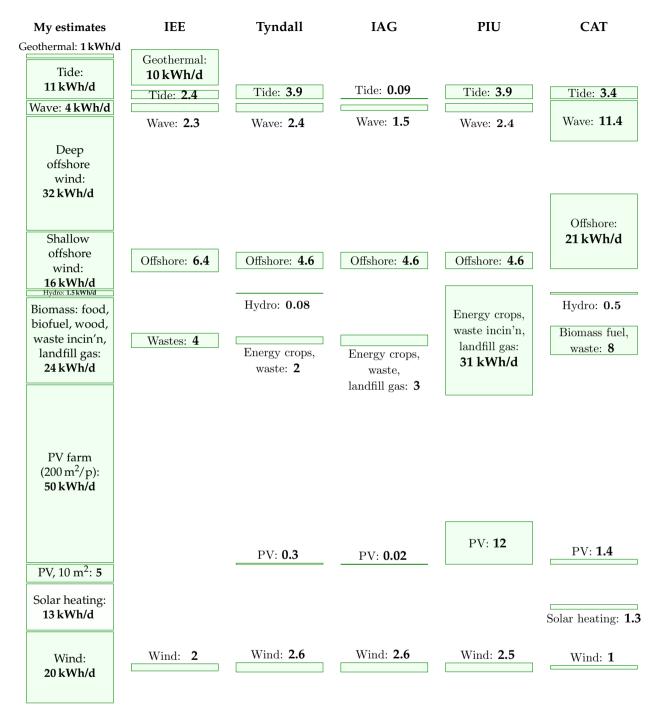


Figure 18.7. Estimates of theoretical or practical renewable resources in the UK, by the Institute of Electrical Engineers, the Tyndall Centre, the Interdepartmental Analysts Group, and the Performance and Innovation Unit; and the proposals from the Centre for Alternative Technology's "Island Britain" plan for 2027.

⁽c) David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

- **IAG** The Interdepartmental Analysts Group's estimates of renewables, take into account economic constraints. Their total practical *and* economical resource (at a retail price of 7p/kWh) is 12 kWh per day per person.
- PIU The "PIU" column shows the "indicative resource potential for renewable electricity generation options" from the DTI's contribution to the PIU review in 2001. For each technology I show their "practical maximum", or, if no practical maximum was given, their "theoretical maximum."
- **CAT** The final column shows the numbers from the Centre for Alternative Technology's "Island Britain" plan.

Bio-powered Europe

Sometimes people ask me "surely we used to live on renewables just fine, before the Industrial Revolution?" Yes, but don't forget that two things were different then: lifestyles, and population densities.

Turning the clock back more than four hundred years, Europe lived almost entirely on sustainable sources: mainly wood and crops, augmented by a little wind power, tidal power, and water power. It's been estimated that the average person's lifestyle consumed a power of 20 kWh per day. The wood used per person was 4 kg per day, which required 1 hectare $(10\,000\,\mathrm{m}^2)$ of forest per person. The area of all land per person in Europe in the 1700s was $52\,000\,\mathrm{m}^2$ per person. In the regions with highest population density, the area per person was $17\,500\,\mathrm{m}^2$ of arable land, pastures, and woods. Today the area of Britain per person is just $4000\,\mathrm{m}^2$, so even if we reverted to the lifestyle of the Middle Ages and completely forested the country, we could no longer live sustainably here. Our population density is far too high.

Green ambitions meet social reality

I consider figure 18.1 to be bleak news. Yes, technically, Britain has "huge" renewables. But realistically, I don't think Britain can live on its own renewables – at least not the way we currently live. I am partly driven to this conclusion by the chorus of opposition that greets any major renewable energy proposal. People love renewable energy, *unless it is bigger than a figleaf.* If the British are good at one thing, it's saying "no." Wind farms across the country? "No, they're ugly noisy things." Solar panels on roofs? "No, that would spoil the visual amenity of the street." An expansion of forestry? "Ruins the countryside." Waste incineration? "No, I'm worried about health risks, traffic congestion, dust and noise." Hydroelectricity? "Yes, but not *big* hydro – that harms the environment". Offshore wind? "No, I'm more worried about the ugly powerlines coming ashore than I

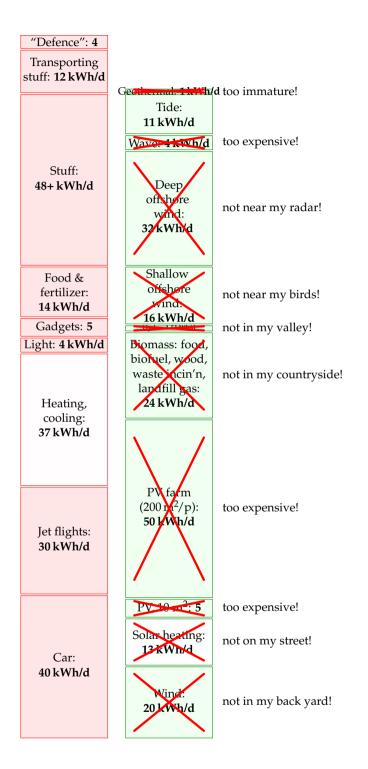
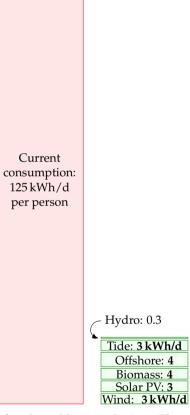


Figure 18.8. The state of play after we add up all the traditional renewables, and then have a public consultation.



After the public consultation. (The left-hand consumption figure, 125 kWh/d per person, by the way, is the average British consumption, excluding imports, and ignoring solar energy acquired through food production.)



Figure 18.9. Where the wild things are. One of the grounds for objecting to wind farms is the noise they produce. I've chopped out of this map of the British mainland a 2-km-radius exclusion zone surrounding every hamlet, village, and town. These white areas would presumably be excluded from wind-farm development. The remaining black areas would perhaps also be largely excluded because of the need to protect tranquil places from industrialization. Settlement data from www.openstreetmap.org.

was about a Nazi invasion." Wave or geothermal power? "No, far too expensive."

After all these objections, I fear that the maximum Britain would ever get from renewables would be something like what's shown in the bottom right of figure 18.8.

Figure 18.9 offers guidance to anyone trying to erect windfarms in Britain. On a map of the British mainland I've shown in white a 2-km-radius exclusion zone surrounding every hamlet, village, and town. These white areas would presumably be excluded from wind-farm development because they are too close to the humans. I've coloured in black all regions that are *more than 2 km* from any human settlement. These areas are largely excluded from wind-farm development because they are *tranquil*, and it's essential to protect tranquil places from industrialization. If you want to avoid objections to your windfarm, pick any piece of land that is not coloured black or white.

We are drawing to the close of the first part of this book. The assumption of the first half was that we want to get off fossil fuels, for one or more of the reasons listed in the preface – climate change, security of sup-

ply, and so forth. Figure 18.10 shows how much power we currently get from renewables and nuclear. They amount to just 4% of our total power consumption.

The two conclusions I expect you to draw from part I are:

1. To make a difference, renewable facilities have to be country-sized.

For any renewable facility to make a contribution comparable to our current consumption, *it has to be country-sized*. To get a big contribution from wind, we used windfarms with the area of Wales. To get a big contribution from solar photovoltaics, we required half the area of Wales. To get a big contribution from waves, we imagined wavefarms covering 500 km of coastline. To make energy crops with a big contribution, we took 75% of the whole country.

To sustain Britain's lifestyle on its renewables alone would be very difficult. A renewable-based energy solution will necessarily be large and intrusive.

2. *it's not going to be easy* to make a plan that adds up using renewables alone. If we are serious about getting off fossil fuels, Brits are going to have to learn to start saying "yes" to something. Indeed to several somethings.

In part II of the book I'll ask "assuming that we can't get production from renewables to add up to our current consumption, what are the other options?"

Notes and further reading

page no.

111 *UK average energy consumption is 125 kWh per day per person.* I took this number from the UNDP Human Development Report, 2007.

The DTI (now known as DBERR) publishes a Digest of United Kingdom Energy Statistics every year. [uzek2]. In 2006, according to DUKES, total primary energy demand was 244.0 million tons of oil equivalent, which corresponds to 130 kWh per day per person.

I don't know the reason for the small difference between the UNDP number and the DUKES number, but I can explain why I chose the slightly lower number. As I mentioned on p29, DUKES uses the same energy-summing convention as me, declaring one kWh of chemical energy to be equal to one kWh of electricity. But there's one minor exception: DUKES defines the "primary energy" produced in nuclear power stations to be the thermal energy, which in 2006 was 9kWh/d/p; this was converted (with 38% efficiency) to 3.4kWh/d/p of supplied electricity; in my accounts, I've focussed on the electricity produced by hydroelectricity, other renewables, and nuclear power; making this small switch in convention reduces the nuclear contribution to the total primary production by about 5kWh/d/p.

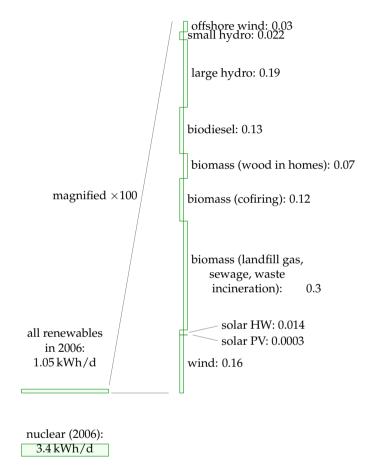


Figure 18.10. Production of renewables and nuclear energy in the UK in 2006. The breakdown of the renewables on the right hand side is scaled up one hundred-fold vertically.

- 112, 113 Figures 18.6 and 18.5. Data from UNDP Human Development Report, 2007. [3av4s9]
 - 111 Losses in the electricity transmission network chuck away 1% of total national energy consumption. To put it another way, the losses are 8% of the electricity generated. This 8% loss can be broken down: roughly 1.5% is lost in the long-distance high-voltage system, and 6% in the local public supply system. Source: MacLeay et al. [2007].
 - 115 In the Middle Ages, the average person's lifestyle consumed a power of 20 kWh per day. Source: Malanima [2006]



Part II Making a difference

19 Every BIG helps

We've established that the UK's present lifestyle can't be sustained on the UK's own renewables (except with the industrialization of country-sized areas of land and sea). So, what are our options, if we wish to get off fossil fuels and live sustainably? We can balance the energy budget either by reducing demand, or by increasing supply, or, of course, by doing both.

Have no illusions. To achieve our goal of getting off fossil fuels, these reductions in demand and increases in supply must be *big*. Don't be distracted by the myth that "every little helps." *If everyone does a little, we'll achieve only a little.* We must do a lot. What's required are *big* changes in demand and in supply.

"But surely, if 60 million people all do a little, it'll add up to a lot?" No. this "if-everyone" multiplying machine is just a way of making something small *sound* big. The "if-everyone" multiplying machine churns out inspirational statements of the form "if *everyone* did X, then it would provide enough energy/water/gas to do Y," where Y sounds impressive. Is it surprising that Y sounds big? Of course not. We got Y by multiplying X by the number of people involved – 60 million or so! Here's an example from the Conservative Party's otherwise straight-talking *Blueprint for a Green Economy*:

"The mobile phone charger averages around ... 1 W consumption, but if every one of the country's 25 million mobile phones chargers were left plugged in and switched on they would consume enough electricity (219 GWh) to power 66 000 homes for one year."

66 000? Wow, what a lot! 66 000 sounds a lot, but the sensible thing to compare it with is the total number of homes that we're imagining would carry out this feat of conservation. 66 000 is just one quarter of one percent of 25 million. So while the statement quoted above is true, I think a calmer way to put it is:

If you leave your mobile phone charger plugged in, it uses one quarter of one percent of your home's electricity.

And if everyone does it?

If *everyone* leaves their mobile phone charger plugged in, they'll use one quarter of one percent of their homes' electricity.

The "if-everyone" multiplying machine is a bad thing because it deflects people's attention towards 25 million minnows instead of 25 million sharks. The mantra, "Little changes can make a big difference", is bunkum, when applied to climate change and power. It may be true that "many people doing a little adds up to a lot", if all those "littles" are somehow focused into a



"We were going to have a wind turbine but they're not very efficient"

Figure 19.1. Reproduced by kind permission of PRIVATE EYE / Robert Thompson www.private-eye.co.uk.

single "lot" – for example, if one million people donate £10 to *one* accident-victim, then the victim receives £10 million. That's a lot. But power is a very different thing. We all use power. So to achieve a "big difference" in total power consumption, you need almost everyone to make a "big" difference to their own power consumption.

So, as I said, what's required are *big* changes in demand and in supply. Demand for energy could be reduced in three ways:

- 1. by reducing our population;
- 2. by changing our lifestyle;
- 3. by keeping our lifestyle, but reducing its energy intensity through 'efficiency' and 'technology'.

Supply could be increased in three ways:

- 1. We could get off fossil fuels by investing in 'clean coal' technology. Oops! Coal is a fossil fuel. Well, never mind – let's take a look at this idea. If we used coal 'sustainably', how much power could it offer? If we don't care about sustainability and just want 'security of supply', could coal offer that?
- 2. We could invest in nuclear fission. Is current nuclear technology 'sustainable'? Is it at least a stop-gap that might last for one hundred years?
- 3. We could buy, beg, or steal renewable energy from other countries bearing in mind that most countries will be in the same boat as Britain and will have no renewable energy to spare; and also bearing in mind that sourcing renewable energy from another country doesn't magically shrink the renewable power facilities required. If we import renewable energy from other countries in order to avoid building renewable facilities the size of Wales in our country, we must have no illusions: we will probably have to build facilities the size of Wales in those other countries.

The next seven chapters discuss first how to substantially reduce demand, and then how to increase supply to meet that reduced, but still "huge", demand.

There are many books describing "100 things you can do to save the planet." I don't want to bore you to death with a long list of all the things that might make a helpful contribution. I'm also worried that such lists encourage the notion that 'every little helps'.

In the chapters that follow, I won't mention *all* the good ideas. I'll discuss just the *big* ideas.

While the footprint of each individual cannot be reduced to zero, the absence of an individual does do so.

Chris Rapley, former head of the British Antarctic Survey

We need fewer people, not greener ones.

Daily Telegraph

Democracy cannot survive overpopulation. Human dignity cannot survive overpopulation.

Isaac Asimov



Figure 19.2. Population growth and emissions... Cartoon from New Scientist.

Cartoon Britain

To simplify and streamline our discussion of demand reduction, I propose to work with a cartoon of British energy consumption, omitting lots of details in order to focus on the big picture. My Cartoon-Britain consumes energy in just three forms: heating, transport, and electricity. The heating consumption of cartoon-Britain is 40 kWh per day per person (currently all supplied by fossil fuels); the transport consumption is also 40 kWh per day per person (currently all supplied by fossil fuels); and the electricity consumption is 18 kWh(e) per day per person; the electricity is currently almost all generated from fossil fuels; the conversion of fossil-fuel energy to electricity is 40% efficient, so supplying 18 kWh(e) of electricity in today's cartoon-Britain requires a fossil-fuel input of 45 kWh per day per person. This simplification ignores some fairly sizeable details, such as agriculture and industry, and the embodied energy of imported goods! But I'd like to be able to have a quick conversation about the main things we need to do to get off fossil fuels. Heating, transport, and electricity account for more than half of our energy consumption, so if we can come up with a plan that delivers heating, transport, and electricity sustainably, then we have made a good step on the way to a more detailed plan that adds up.

Having adopted this cartoon of Britain, our discussions of demand reduction will have just three bits. First, how can we reduce transport's energy-demand and eliminate all fossil fuel use for transport? This is the topic of Chapter 20. Second, how can we reduce heating's energy-demand and eliminate all fossil fuel use for heating? This is the topic of Chapter 21. Third, what about electricity (Chapter 22)?

Supply options – clean coal, nuclear, and other people's renewables – are then discussed in chapters 23, 24, and 25. Finally, Chapter 26 discusses how to cope with fluctuations in demand and fluctuations in renewable power production.

Having laid out the demand-reducing and supply-increasing options, Chapter 27 discusses various ways to put these options together to make plans that add up, in order to supply Cartoon-Britain's transport, heating, and electricity.

I could spend many pages discussing 'fifty things you can do to make a difference', but I think this cartoon approach, chasing the three biggest fish, may lead to more effective policies.

But what about 'stuff'? According to part I, the embodied energy in imported stuff might be the biggest fish of all! Yes, perhaps that fish is the mammoth in the room. But let's leave defossilizing that mammoth to one side, and focus on the animals over which we have direct control.

So, here we go: let's talk about transport, heating, and electricity.

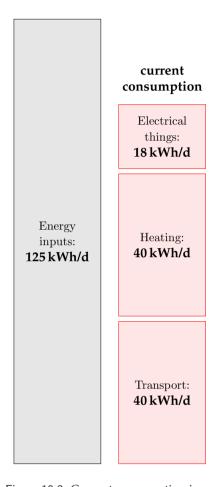


Figure 19.3. Current consumption in "cartoon-Britain 2008."

19 — Every BIG helps 125

For the impatient reader

Are you eager to know the end of the story right away? Here is a quick summary, a sneak preview of part II.

First, we electrify transport. Electrification both gets transport off fossil fuels, and makes transport more energy-efficient. (Of course, electrification increases our demand for sustainable electricity.)

Second, to supplement solar-thermal heating, we electrify most heating of air and water in buildings using *heat pumps*, which are four times more efficient than simple resistance-heaters. This electrification of heating further increases the required green electricity.

Third, we get all the green electricity from a mix of four sources: from our own renewables; perhaps from 'clean coal'; perhaps from nuclear; and finally, and with great politeness, from other countries' renewables.

Among other countries' renewables, solar power in deserts is the most plentiful option. As long as we are capable of building peaceful international collaborations, solar power in other people's deserts certainly has the technical potential to provide us, them, and everyone with 125 kWh per day per person.

Questions? Read on.

20 Better transport

Modern vehicle technology can reduce climate change emissions without changing the look, feel or performance that owners have come to expect.

California Air Resources Board

Roughly one third of our energy goes into transportation. Can *technology* deliver a reduction in consumption?

In this chapter we will explore options for achieving two goals: to deliver the biggest possible reduction in transport's energy use, *and* to eliminate fossil fuel use in transport.

Transport featured in three of our consumption chapters: Chapter ?? (cars), Chapter 5 (planes), and Chapter ?? (road freight and sea freight). So there's two sorts of transport to address: passenger transport, and freight. Our unit of passenger transport is the passenger-kilometre (p-km). If a car carries one person a distance of 100 km, it delivers 100 p-km of transportation. If it carries four people the same distance, it has delivered 400 p-km. Similarly our unit of freight transport is the ton-km (t-km). If a truck carries 5 t of cargo a distance of 100 km then it has delivered 500 t-km of freight-transport. We'll measure the energy consumption of passenger transport in "kWh per 100 passenger-kilometres," and the energy consumption of freight in "kWh per ton-km." Notice that these measures are the other way up compared to "miles per gallon": whereas we like vehicles to deliver *many* miles per gallon, we want energy-consumption to be *few* kWh per 100 p-km.

We'll start this chapter by discussing how to reduce the energy consumption of surface transport. To understand how to reduce energy consumption, we need to understand where the energy is going in surface transport. (These concepts are explained in more detail in Technical Chapter A.)

In *short-distance travel*, the energy mainly goes into speeding up the vehicle and its contents. Key strategies for consuming less in this sort of transportation are therefore to *weigh less*, and to *go further between stops*. Regenerative braking, which captures energy when slowing down, may help too. In addition, it helps to *move slower*, and to *move less*.

In *long-distance travel* at steady speed, by train or automobile, most of the energy goes into making air swirl around, because you only have to accelerate the vehicle once. The key strategies for consuming less in this sort of transportation are therefore to *move slower*, and to *move less*, and to *use long*, *thin vehicles*.

In all forms of travel, there's an energy-conversion chain, which takes energy in some sort of fuel and uses some of it to push the vehicle forwards. Inevitably this energy chain has inefficiencies. In a standard fossil-





Figure 20.1. This chapter's starting point: an urban luxury tractor consuming 80 kWh per 100 km. Can we do better?

fuel car, for example, roughly 75% of the energy is lost in making the engine and radiator hot, and only 25% is used for pushing. So a final strategy for consuming less energy is to make the energy-conversion chain more efficient.

To summarise, here are the principles of more-efficient surface transport:

- reduce the frontal area per person;
- reduce the vehicle's weight per person;
- when travelling, go at a steady speed and avoid using brakes;
- travel slower;
- · travel less; and
- make the energy chain more efficient.

How to roll better

A widely quoted statistic says something along the lines of "Only 1 percent of the energy used by a car goes into moving the driver." – the implication being that, surely, by being a bit smarter, we could make cars one hundred times more efficient? The answer is yes, almost, but only by applying the principles of vehicle design and vehicle use, listed above, to extreme degrees.

One illustration of extreme vehicle design is an eco-car, which has small frontal area and low weight, and – if any records are to be broken – is carefully driven at a low and steady speed. The *Team Crocodile* eco-car does 2184 miles per gallon (1.3 kWh per 100 km) at a speed of 24 km per hour. Weighing 50 kg and shorter in height than a traffic cone, it comfortably accommodates one teenage driver.

Hmm. I think that the driver of the urban tractor in figure 20.1 might detect a change in "look, feel and performance" if we switched them to the eco-car (figure 20.2) and asked them to keep their speed below 15 miles per hour. So, the idea that cars could easily be one hundred times more energy efficient is a myth. We'll come back to the challenge of making energy-efficient cars in a moment. But first, let's see some other ways of satisfying the principles of more-efficient surface transport.

Figure 20.3 shows a multi-passenger vehicle that is at least 25 times more energy-efficient than a standard petrol car: a bicycle. The bicycle's performance (in terms of energy per distance) is about the same as the ecocar's. Its speed is the same, its mass is lower than the eco-car's (because the human replaces the fuel tank and engine), and its effective frontal area is higher, because the cyclist is not so well streamlined as the eco-car. Figure 20.4 shows another possible replacement for the petrol car: a train,

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com



Figure 20.2. Team Crocodile's eco-car uses 1.3 kWh per 100 km. Photo kindly provided by Team Crocodile. http://www.teamcrocodile.com/



Figure 20.3. "Babies on board." This mode of transportation has an energy cost of 1 kWh per 100 person-km.



Figure 20.4. This 8-carriage stopping train from Cambridge to London, at its maximum speed of 100 mph (161 km/h), consumes 1.6 kWh per 100 passenger-km, if full.







Figure 20.5. Some Public transports, and their energy-efficiencies, when on best behaviour.
Tubes, inner and outer.
Two high-speed trains.
Trolleybuses in San Francisco.
Vancouver SeaBus. Photo by Larry.

3 kWh per 100 seat-km, if full







21 kWh per 100 p-km, if full

with an energy-cost, if full, of 1.6 kWh per 100 passenger-km. In contrast to the eco-car and the bicycle, trains manage to achieve outstanding efficiency without travelling slowly, and without having a low weight per person. Trains make up for their high speed and heavy frame by exploiting the principle of small frontal area per person. Whereas a cyclist and a regular car have effective frontal areas of about $0.8\,\mathrm{m}^2$ and $0.5\,\mathrm{m}^2$ respectively, a full commuter train from Cambridge to London has a frontal area per passenger of $0.02\,\mathrm{m}^2$.

But whoops, now we've broached an ugly topic – the prospect of sharing a vehicle with "all those horrible people." Well, squish aboard, and let's ask: How much could consumption be reduced by a switch from personal gas-guzzlers to excellent integrated public transport?

Public transport

At its best, shared public transport is far more energy-efficient than individual car-driving. A diesel-powered **coach**, carrying 49 passengers and doing 10 miles per gallon at 65 miles per hour, uses 6 kWh per 100 passenger-km – thirteen times better than the single-person car. Vancouver's **trolleybuses** have an energy consumption of 270 kWh per vehicle-km, and an average speed of 15 km/h. If the trolleybus has 40 passengers on board, then its passenger transport efficiency is 7 kWh/100 p-km. The Vancouver **SeaBus** has a transport efficiency of 83 kWh per vehicle-km at a speed of 13.5 km/h. It can seat 400 people, so its passenger transport

efficiency when full is 21 kWh/100 p-km. London underground trains, at peak times, use 4.4 kWh per 100 passenger-km – eighteen times better than individual cars. Even high-speed trains, which violate two of our energy-saving principles by going twice as fast as the car and weighing a lot, are much more energy efficient: if the train is full, its energy cost is 3 kWh per 100 p-km – that's twenty-seven times smaller than the car!

However, we must be realistic in our planning. Some trains, coaches, and buses are not full (figure 20.6). So the *average* energy cost of public transport is bigger than the best-case figures we just mentioned. What's the *average* energy-consumption of public transport systems, and what's a realistic appraisal of how good they could be?

In 2006-7, the total energy cost of all London's underground trains, including lighting, lifts, depots, and workshops, was 15 kWh per 100 passenger-km – five times better than our baseline car.

In 2006-7 the energy cost of all London buses was 32 kWh per 100 p-km. Energy cost is not the only thing that matters, of course. Passengers care about speed: and the underground trains delivered higher speeds (an average of 33 km/h) than buses (18 km/h). Managers care about costs: the staff costs, per passenger-km, of underground trains are less than those of buses.



Figure 20.6. Some trains aren't full. Three men and a cello – the sole occupants of this carriage of the 10.30 high-speed train from Edinburgh to Kings Cross.





32 kWh per 100 p-km



9 kWh per 100 p-km

Figure 20.7. Some public transports, and their *average* energy consumptions. Left: Some red buses. Right: Croydon Tramlink. Photo by Stephen Parascandolo.

The total energy consumption of the Croydon Tramlink system in 2006–7 (including the tram depot and facilities at tram-stops) was 9 kWh per 100 p-km, with an average speed of 25 km/h.

How good could public transport be? Perhaps we can get a rough indication by looking at data from Japan (Table 20.8). At 19 kWh per 100 p-km and 6 kWh per 100 p-km, bus and rail both look promising. Rail has the nice advantage that it can solve both of our goals – reduction in energy consumption, and independence from fossil fuels. Buses and coaches have obvious advantages of simplicity and flexibility, but keeping this flexibility at the same time as getting buses and coaches to work without fossil fuels may be a challenge.

To summarise, public transport (especially electric trains, trams, and buses), seem a promising way to deliver passenger transportation – better in terms of energy per passenger-km, perhaps five or ten times better than cars. However, if people demand the flexibility of a private vehicle, what

Car 68
Bus 19
Rail 6
Air 51
Sea 57

Table 20.8. Overall transport efficiencies of transport modes in Japan (1999) in kWh per 100 passenger-km.

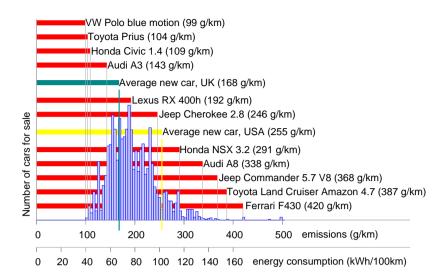


Figure 20.9. Carbon pollution, in grams CO₂ per km, of a selection of cars for sale in the UK. The horizontal axis shows the emission rate, and the height of the blue histogram indicates the number of models on sale with those emissions in 2006. Source: http://www.newcarnet.co.uk/. The second horizontal scale indicates approximate energy consumptions, assuming that 250 g CO₂ is associated with 1 kWh of chemical energy.

are our other options?

Legislation and incentives

How to ensure choosers make the right choice?

The energy consumption of individual cars can be reduced. The wide range of energy efficiencies of cars for sale proves this. In a single showroom in 2006 you could buy a Honda Civic 1.4 that uses roughly 44 kWh per 100 km, or a Honda NSX 3.2 that uses 116 kWh per 100 km (figure 20.9). The fact that people merrily buy from this wide range is also proof that we need extra incentives and legislation to encourage the blithe consumer to choose more energy-efficient cars. There are various ways to help consumers prefer the Honda Civic over the Honda NSX 3.2 gas guzzler: raising the price of fuel; cranking up the showroom tax (the tax on new cars) in proportion to the predicted consumption of the vehicle; cranking up the road-tax on gas guzzlers; parking privileges for economical cars; or fuel rationing. All such measures are unpopular with at least some voters. Perhaps a better legislative tactic would be to enforce reasonable energyefficiency, rather than continuing to allow unconstrained choice; to simply ban, from a certain date, the sale of any car whose energy consumption is more than 80 kWh per 100 km; and then, over time, reduce this ceiling to 60 kWh per 100 km, then 40 kWh per 100 km, and beyond. Additional legislation placing limits on the weight and frontal area of vehicles would simultaneously reduce fuel consumption and improve safety for other road-users (figure 20.11). People today choose their cars to make fashion statements. With strong efficiency legislation, there could still be a wide choice of fashions; they'd all just happen to be energy-efficient. You



Figure 20.10. Special parking privileges for electric cars in Ann Arbor, Michigan.



Figure 20.11. Monstercars not only use more fuel – they are also just tall enough to completely obscure the view and the visibility of pedestrians,

20 — Better transport 131

could choose any colour, as long as it was green.

While we wait for the voters and politicians to agree to legislate for efficient cars, what other options are available?





Figure 20.12. A roundabout in Enschede, Netherlands.

Bikes

My favourite suggestion is the provision of excellent cycle facilities, along with appropriate legislation (lower speed-limits, collision-regulations that favour cyclists). Figure 20.12 shows a roundabout in Enschede, Netherlands. There are two circles: the one for cars lies inside the one for bikes, with a comfortable car's length separating the two. The priority rules are the same as those of a British roundabout, except that cars exiting the central circle must give way to circulating cyclists (just as British cars give way to pedestrians on zebra crossings). Where excellent cycling facilities are provided, people will use them, as evidenced by the infinite number of cycles sitting outside a Dutch railway station (figure 20.13).

Somehow, British cycle provision (figure 20.14) doesn't live up to the Dutch standard.





Figure 20.13. A few Dutch bikes.

Figure 20.14. Meanwhile, back in Britain... Photo on right by Mike Armstrong.

In the French city of Lyon, a privately-run public bicycle network, Vélo'v, was introduced in 2005 and has proved popular. Lyon's popula-

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

tion of 470 000 inhabitants is served by 2000 bikes distributed around 175 cycle-stations in an area of $50\,\mathrm{km^2}$. In the city centre, you're usually within 400 metres of a cycle-station. Users join the scheme by paying a subscription fee of $\leqslant 10$ per year and may then hire bicycles free for all trips lasting less than 30 minutes. For longer hire periods, users pay up to $\leqslant 1$ per hour. Short-term visitors to Lyon can buy one-week subscriptions for $\leqslant 1$.

Other legislative opportunities

Speed limits are a simple knob that could be twiddled. As a rule, cars that travel slower use less energy (see Chapter A for detailed discussion.) With practice, drivers can learn to drive more economically: using the accelerator and brake less and always driving in the highest possible gear can give a 20% reduction in fuel consumption.

Another way to reduce fuel consumption is to reduce congestion. Stopping and starting, speeding up and slowing down, is a much less efficient way to get around than driving smoothly. Idling in stationary traffic is an especially poor deliverer of miles per gallon!

Congestion can be reduced by providing good alternatives (cycle lanes, public transport), and by charging road users extra if they contribute to congestion. In this chapter's notes I describe a fair and simple method for handling congestion-charging.

Congestion occurs when there are too many vehicles on the roads. So one simple way to reduce congestion is to group travellers into a smaller number of vehicles. A striking way to think about a switch from cars to coaches is to calculate the road area required by the two modes. Take a trunk road on the verge of congestion, where the desired speed is 60 mph. The safe distance from one car to the next at 60 mph is 77 m. If we assume there's one car every 80 m and that each car contains 1.6 people, then vacuuming up 40 people into a single coach frees up *two kilometres* of road!

Enhancing cars

Assuming that the developed world's love-affair with the car is not about to be broken off, what are the technologies that can deliver significant energy savings? Savings of 10 or 20% are easy – we've already discussed some ways to achieve them, such as making cars smaller and lighter. Another option is to switch from petrol to diesel. Diesel engines are more expensive to make, but they tend to be more fuel-efficient. But are there technologies that can radically increase the efficiency of the energy-conversion chain? (Recall that in a standard petrol car, 75% of the energy is turned into heat and blown out of the radiator!) And what about the goal of getting off fossil fuels?

In this section, we'll discuss five technologies: regenerative braking; hybrid cars; electric cars; hydrogen-powered cars; and compressed-air cars.



Figure 20.15. A Vélo'v station in Lyon.



Figure 20.16. With congestion like this, it's faster to walk.

20 — Better transport

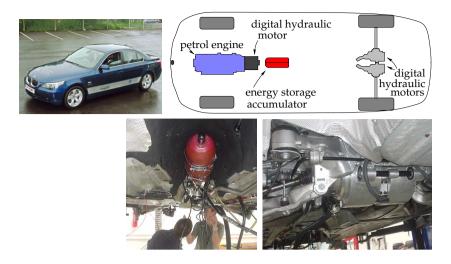


Figure 20.17. A BMW 530i modified by Artemis Intelligent Power to use digital hydraulics. Lower left: A 6-litre accumulator (the red canister), capable of storing about 180 kJ of energy in compressed nitrogen. Lower right: Two 200 kW hydraulic motors, one for each rear wheel, which both accelerate and decelerate the car. The car is still powered by its standard 190 kW petrol engine, but thanks to the digital hydraulic transmission and regenerative braking, it uses 30% less fuel.

Regenerative braking

There are four ways to capture energy as a vehicle slows down.

- 1. An electric generator coupled to the wheels can charge up an electric battery or supercapacitor.
- 2. Energy can be stored in a flywheel.
- 3. Hydraulic motors can make compressed air.
- 4. Braking energy can be stored gravitationally by driving the vehicle up a ramp whenever you want to slow down. This gravitational energy storage option is rather inflexible, since there must be a ramp in the right place. It's an option that most useful for trains, and it is illustrated by the London Underground's Victoria line, which has hump-back stations. Each station is at the top of a hill in the track. Arriving trains are automatically slowed down by the hill, and departing trains are accelerated as they go down the far side of the hill. The hump-back-station design provides an energy saving of 5% and a reduction in inter-station run time of 9%.

Electric regenerative braking (using a battery to store the energy) salvages roughly 50% of the kinetic energy in a braking event, leading to perhaps a 20% reduction in the energy cost of city driving.

Regenerative systems using hydraulics and flywheels seem to work a little better than battery-based systems, salvaging at least 70% of the braking energy. Figure 2 describes a hybrid car with a petrol engine powering digitally-controlled hydraulics. On a standard driving cycle, this car uses 30% less fuel than the original petrol car. In urban driving, its energy consumption is halved, from 131 kWh per 100 km to 62 kWh per 100 km

(20 mpg to 43 mpg). (Credit for this performance improvement must be shared between regenerative braking and the use of hybrid technology.) Hydraulics and flywheels are both promising ways to handle regenerative braking because small systems can handle large powers. A flywheel system weighing just 24 kg (figure 20.18), designed for energy storage in a racing car, can store 400 kJ (0.1 kWh) of energy – enough energy to accelerate an ordinary car up to 60 miles per hour (97 km/h); and it can accept or deliver 60 kW of power. Electric batteries capable of delivering that much power would weigh about 200 kg. So, unless you're already carrying that much battery on board, an electrical regenerative-braking system should probably use capacitors to store braking energy. Super-capacitors have similar energy-storage and power-delivery parameters to the flywheel.

Hybrid cars

Hybrid cars such as the Toyota Prius have more-efficient engines, but to be honest, today's hybrid vehicles don't really stand out from the crowd (figure 20.9).

The horizontal bars in figure 20.9 highlight a few cars including two hybrids. Whereas the average new car in the UK emits $168\,g$, the hybrid Prius emits about $100\,g$ of CO_2 per km, as do several other non-hybrid vehicles – the VW Polo blue motion emits $99\,g$ /km, and there's a Smart car that emits $88\,g$ /km.

The Lexus RX 400h is the second hybrid, advertised with the slogan "LOW POLLUTION. ZERO GUILT." But its CO_2 emissions are $192\,\mathrm{g/km}$ — worse than the average UK car! The advertising standards authority ruled that this advertisement breached the advertising codes on Truthfulness, Comparisons and Environmental claims. "We considered that ... readers were likely to understand that the car caused little or no harm to the environment, which was not the case, and had low emissions in comparison with all cars, which was also not the case."

In general, hybrid technologies seem to give fuel savings of 20 or 30%. So neither these petrol/electric hybrids, nor the petrol/hydraulic hybrid featured in figure 2 seems to me to have really cracked the transport challenge. A 30% reduction in fossil-fuel consumption is impressive, but it's not enough by this book's standards. Our opening assumption was that we want to get off fossil fuels, or at least to reduce fossil fuel use by 90%. Can this goal be achieved without reverting to bicycles?

Electric vehicles

The REVA electric car was launched in June 2001 in Bangalore and is exported to the UK as the G-Wiz. The G-Wiz's electric motor has a peak power of 13 kW, and can produce a sustained power of 4.8 kW. The motor provides regenerative braking. It is powered by eight 6-volt lead acid



Figure 20.18. A flywheel regenerative-braking system. Photos courtesy of Flybrid Systems.



Figure 20.19. Prius.

20 — Better transport









Figure 20.20. Electric vehicles. From left to right: the G-Wiz; the rotting corpse of a Sinclair C5; a Citroën Berlingo; and an Elettrica.

batteries, which when fully charged give a range of "up to $77\,\mathrm{km}$." A full charge consumes $9.7\,\mathrm{kWh}$ of electricity. These figures correspond to $13\,\mathrm{kWh}$ per $100\,\mathrm{km}$.

Manufacturers always quote the best possible performance of their products. What happens in real life?

The real-life performance of a G-Wiz in London is shown in figure 20.21. The average transport efficiency of the G-Wiz in these experiments is $21\,\mathrm{kWh}$ per $100\,\mathrm{km}$ – about four times better than an average fossil fuel car. The best result was $16\,\mathrm{kWh}$ per $100\,\mathrm{km}$, and the worst was $33\,\mathrm{kWh}$ per $100\,\mathrm{km}$. If you are interested in carbon emissions, $21\,\mathrm{kWh}$ per $100\,\mathrm{km}$ is equivalent to $105\,\mathrm{gCO}_2$ per km, assuming that the electricity's footprint is $500\,\mathrm{gCO}_2$ per kWh.

Now, the G-Wiz sits at one end of the performance spectrum. What if we demand more – more acceleration, more speed, and more range? At the other end of the spectrum is the Tesla Roadster. The Tesla Roadster 2008 has a range of 220 miles (354 km); its lithium-ion battery pack stores 53 kWh and weighs 450 kg (120 Wh/kg). The vehicle weighs 1220 kg and its motor's maximum power is 185 kW. What is the energy-consumption of this muscle car? Remarkably, it's better than the G-Wiz: 15 kWh per 100 km.

I've looked up the performance figures for lots of electric vehicles – they're listed in this chapter's end-notes – and they seem to be consistent with this summary: electric vehicles can replace fossil-cars, and can deliver transport at an energy cost of roughly 15 kWh per 100 km. That's five times better than our baseline car, and significantly better than any hybrid cars. Hurray! To achieve economical transport, we don't have to huddle together in public transport – we can still hurtle around, enjoying all the pleasures and freedoms of solo travel, thanks to electric vehicles.

This moment of celebration feels like a good time to unveil this chapter's big summary diagram, figure 20.23, which shows the energy requirements of all the forms of passenger-transport we have discussed and a couple that are still to come.

OK, the race is over, and I've announced two winners – public transport, and electric vehicles. But are there any other options crossing the finishing line? We have yet to hear about the compressed-air-powered car

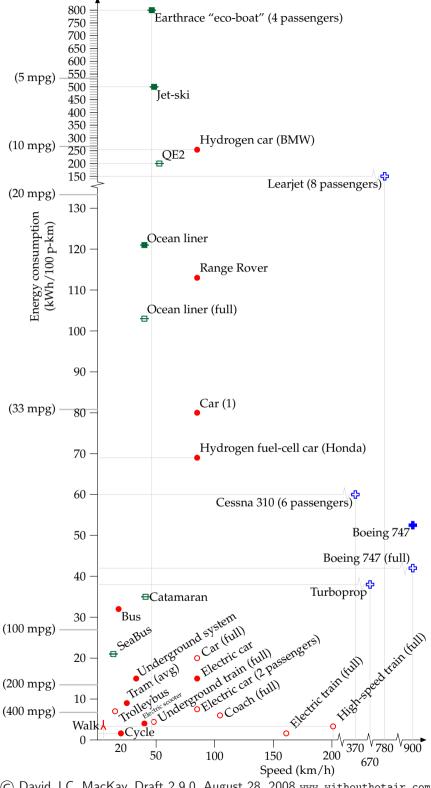
Figure 20.21. Measurements of electricity required to recharge a G-Wiz versus distance driven. Measurements were made at the socket with a Maplin meter. Each data point is labeled by the date (day/month).



Figure 20.22. Tesla Roadster: 15 kWh per 100 km.

http://www.teslamotors.com/.

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com



© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

Figure 20.23. Energy requirements of different forms of passenger-transport. The vertical coordinate shows the energy consumption in kWh per 100 passenger-km. The horizontal coordinate indicates the speed of the transport. The "Car (1)" is an average UK car doing 33 miles per gallon with a single occupant. The "Bus" is the average performance of all London buses. The "Underground system" shows the performance of the whole London Underground system, including the energy cost of its lighting, escalators, and depots. The catamaran is a diesel-powered vessel. In response to popular demand, I've indicated on the left-hand side equivalent fuel efficiencies in passenger-miles per imperial gallon (mpg). When comparing electric with chemical-powered vehicles, I've expressed both energy requirements in kWh with a one-for-one exchange

Hollow point-styles show best-practice performance, assuming all seats of a vehicle are in use. Filled point-styles indicate actual performance of a vehicle in typical

See also figure 15.9 (energy requirements of freight transport). and the hydrogen car. If either of these turns out to be better than electric car, it won't affect the long-term picture very much: whichever of these three technologies we went for, the vehicles would be charged up using energy generated from a "green" source.

Compressed-air cars

Air-powered vehicles are not a new idea. Hundreds of trams powered by compressed air and hot water plied the streets of Nantes and Paris from 1879 to 1911. Figure 20.24 shows a German pneumatic locomotive from 1958. I think that in terms of energy efficiency the compressed-air technique for storing energy isn't as good as electric batteries. The problem is that compressing the air generates *heat* that's unlikely to be used efficiently; and expanding the air generates *cold*, another byproduct that is unlikely to be used efficiently. But compressed air may be a superior technology to electric batteries in other ways. For example, air can be compressed thousands of times and doesn't wear out! It's interesting to note, however, that the first product sold by the Aircar company (also known as MDI) is actually an *electric* scooter. http://www.theaircar.com/acf/

There's talk of Tata Motors in India manufacturing air-cars, but it's hard to be sure whether the compressed-air vehicle is going to see a revival, because no-one has published the specifications of any modern prototypes. Here's the fundamental limitation: the energy-density of compressed-air energy-stores is only about 11–28 Wh per kg, which is similar to lead-acid batteries, and roughly five times smaller than lithium-ion batteries. So the range of a compressed-air car will only ever be as good as the range of the earliest electric cars. Compressed-air storage systems do have three advantages over batteries: longer life, cheaper construction, and fewer nasty chemicals.

Hydrogen cars – blimp your ride

I think hydrogen is a hyped-up bandwagon. I'll be delighted if I'm proved wrong, but I don't see how hydrogen is going to help us with our energy problems.

The "hydrogen economy" received support from Nature magazine in a column praising Arnold Schwarzenegger for filling up a hydrogen-powered Hummer. Nature's article uncritically praised Arnold's vision of hydrogen-powered cars replacing "polluting models" with the quote "the governor is a real-life climate action hero." But the critical question that needs to be asked when such hydrogen heroism is on display is "where is the *energy* to come from to *make* the hydrogen?" Hydrogen is not a miraculous *source* of energy; it's just an energy *carrier*, like a rechargeable battery. Moreover converting energy to and from hydrogen can only be done inefficiently.

Here are some numbers.





Figure 20.24. Top: A compressed-air tram taking on air and steam in Nantes. Powering the trams of Nantes used 4.4 kg of coal (36 kWh) per vehicle-km, or 115 kWh per 100 p-km, if full. [5qhvcb]
Bottom: A compressed-air locomotive; weight 9.2 t, pressure 175 bar, power 26 kW; photo courtesy of Rüdiger Fach, Rolf-Dieter Reichert, and Frankfurter Feldbahnmuseum.

- In the CUTE (Clean Urban Transport for Europe) project, which
 was intended to demonstrate the feasibility and reliability of fuel
 cell buses and hydrogen technology, fuelling the hydrogen buses required between 80% and 200% more energy than the baseline diesel
 bus.
- Fuelling the *Hydrogen 7*, the hydrogen-powered car made by BMW, requires 254 kWh per 100 km three times more energy than an average European car.

If our task were "please stop using fossil fuels for transport, allowing your-self the assumption that infinite quantities of green electricity are available for free," then of course an energy-profligate transport solution like hydrogen might be a contender (though hydrogen faces many other problems). But green electricity is not free. Indeed, getting green electricity on the scale of our current consumption is going to be very challenging. The fossil fuel challenge is an energy challenge. The climate-change problem is an energy problem. We need to focus on solutions that use less energy, not "solutions" that use more! I know of no form of wheeled transport whose energy consumption is worse than this hydrogen car. (Moving onto water, there's jet-skis – using about 500 kWh per 100 km; and the *Earthrace* biodiesel-powered speed-boat, absurdly called an eco-boat, which uses 800 kWh per 100 p-km.)

Hydrogen advocates may say "the BMW Hydrogen 7 is just an early prototype, and it's a luxury car with lots of muscle – the technology is going to get more efficient." Well, I hope so, because it has a lot of catching up to do. The Tesla Roadster (figure 20.22) is an early prototype too, and it's also a luxury car with lots of muscle. And it's more than ten times more energy-efficient than the Hydrogen 7! Feel free to put your money on the hydrogen horse if you want, and if it wins in the end, fine. But it seems foolish to invest in the horse that's so far behind in the race. Just look at figure 20.23 – if I hadn't squished the top of the vertical axis, the hydrogen car would not have fitted on the diagram!

Yes, the Honda fuel-cell car, the FCX Clarity, does better – it rolls in at $69\,\mathrm{kWh}$ per $100\,\mathrm{km}$ – but my prediction is that after all the "zero-emissions" trumpeting is over, we'll find that hydrogen cars use just as much energy as the average fossil car of today.

Other problems with hydrogen

Hydrogen is an inconvenient energy storage medium, whether stored as a high pressure gas or as a liquid (which requires a temperature of $-253\,^{\circ}$ C). Even at a pressure of 700 bar (which requires a hefty pressure vessel) its energy density (energy per unit volume) is 22% of gasoline's. The cryogenic tank of the BMW 745h weighs 120 kg and stores 8 kg of hydrogen.



Figure 20.25. The Earthrace "eco-boat". Photo by David Castor.



Figure 20.26. The Honda FCX Clarity hydrogen-powered fuel-cell sedan, with a Jamie Lee Curtis for scale. Photo courtesy of automobiles.honda.com.

20 — Better transport 139

Some questions about electric vehicles

Is there enough lithium to make all the batteries for a huge fleet of electric cars?

World lithium reserves are estimated to be 9.5 million tons in ore deposits. A lithium-ion battery is 3% lithium. If we assume each vehicle has a 200 kg battery, then we need 6 kg of lithium per vehicle. So the estimated reserves in ore deposits are enough to make the batteries for 1.6 billion vehicles. That's more than the number of cars in the world today (roughly 1 billion) – but not much more, so the amount of lithium may be a concern, especially when we take into account the competing ambitions of the nuclear fusion posse (Chapter 24) to guzzle lithium in their reactors. There's many thousands times more lithium in sea water, so perhaps the oceans will provide a useful backup. However, lithium specialist R. Keith Evans says "concerns regarding lithium availability for hybrid or electric vehicle batteries or other foreseeable applications are unfounded." And anyway, other lithium-free battery technologies such as zinc-air rechargeables are being developed http://www.revolttechnology.com/. I think the electric car is a goer!

You've shown that electric cars are more energy-efficient than fossil cars. But are they better if our objective is to reduce CO_2 emissions, and the electricity is still generated by fossil power-stations?

This is quite an easy calculation to do. Assume the electric vehicle's energy cost is $20 \, \text{kWh}(e)$ per $100 \, \text{km}$. (I think $15 \, \text{kWh}(e)$ per $100 \, \text{km}$ is perfectly possible, but let's play sceptical in this calculation.) If grid electricity has a carbon footprint of $500 \, \text{g}$ per kWh(e) then the effective emissions of this vehicle are $100 \, \text{g} \, \text{CO}_2$ per km, which is as good as the best fossil cars. So I conclude that switching to electric cars is *already* a good idea, even before we green our electricity supply.

Electric cars, like fossil cars, have costs of both manufacture and use. Electric cars may cost less to use, but if the batteries don't last very long, shouldn't you pay more attention to the manufacturing cost?

Yes, that's a good point. My transport diagram shows only the use cost. If electric cars have to have new batteries every few years, my numbers may be underestimates. The batteries in a Prius are expected to last just 10 years, and a new set at that time would cost £3500. Will anyone want to own a 10-year old Prius and pay that cost? It could be predicted that most Priuses will be junked at age 10 years. This is certainly a concern for all electric vehicles that have batteries. I guess I'm optimistic that, as we switch to electric vehicles, battery technology is going to improve.

I live in a hot place. How could I drive an electric car? I demand power-hungry air-conditioning!

There's an elegant fix for this demand in hot places: fit 4 m² of photovoltaic panels in the upward-facing surfaces of the electric car. If the

air-conditioning is needed, you must be outdoors and the sun must be shining. 20%-efficient panels will generate up to 800 W, which is enough to power a car's air-conditioning. The panels might even make a useful contribution to charging the car when it's parked, too. Solar-powered vehicle cooling was included in a Mazda in 1993; the solar cells were embedded in the glass sunroof.

I live in a cold place. How could I drive an electric car? I demand power-hungry heating!

The motor of an electric vehicle, when it's running, will on average use something like 10 kW, with an efficiency of 90 or 95%. Some of the lost power, the other 5–10%, will be dissipated as heat in the motor. Perhaps electric cars that are going to be used in cold places can be carefully designed so that this motor-generated heat, which might be in the ballpark of 250 or 500 W, can be piped from the motor into the car. That much power would be enough to provide some windscreen demisting or bodywarming.

Are lithium-ion batteries safe in an accident?

Some lithium-ion batteries are unsafe when short-circuited or overheated, but the battery industry are now producing safer batteries such as lithium phosphate. There's a fun safety video at www.valence.com.

The future of flying?

The superjumbo A380 is said by Airbus to be "a highly fuel-efficient aircraft." – in fact, as they then say, it burns just 12% less fuel per passenger than a 747.

Boeing has announced similar breakthroughs: their new 747–8 Intercontinental, trumpeted for its planet-saving properties, is (according to Boeing's advertisements) only 15% more fuel-efficient than a 747–400.

This slender rate of progress (contrasted with cars, where we saw changes in technology delivering two-fold or even ten-fold improvements in efficiency) is explained in Chapter ??. Planes are up against a fundamental limit imposed by the laws of physics. Any plane, whatever its size, *has to* expend an energy of at least 0.1 kWh per ton-km. Planes have already been fantastically optimized, and there is no prospect of significant improvements in plane efficiency.

I used to think that the way to solve the long-distance-transport problem was to revert to the way it was done before planes: ocean liners. Then I looked at the numbers. The sad truth is that ocean liners use more energy per passenger-km than jumbo jets. The QE2 uses four times as much energy as a jumbo. OK, it's a luxury vessel; can we do better with slower tourist-class liners? From 1952 to 1968, the economical way to cross the Atlantic was was in two Dutch-built liners known as "The Economy Twins,"



Figure 20.27. Airbus A380.



Figure 20.28. TSS Rijndam arriving in New York City.

20 — Better transport 141

the Maasdam and the Rijnsdam. These travelled at $16.5\,\mathrm{km}\,(30.5\,\mathrm{km/h})$, so the crossing from Britain to New York took eight days. Their energy consumption, if they carried a full load of 893 passengers, was $103\,\mathrm{kWh}$ per $100\,\mathrm{p-km}$. At a typical 85% occupancy, the energy consumption was $121\,\mathrm{kWh}$ per $100\,\mathrm{pkm}$ – more than twice that of the jumbo jet.

So, sadly, I don't think boats are going to beat planes in energy consumption. If eventually we want a way of travelling large distances without fossil fuels, perhaps nuclear-powered ships are an interesting option (figures 20.29 & 20.30).

What about freight?

International shipping is a surprisingly efficient user of fossil fuels; so decarbonising road transport is a higher priority than decarbonising ships. But fossil fuels are a finite resource, and eventually ships must be powered by something else. One option will be nuclear power. There are already many nuclear-powered ships, both military and civilian. Russia has ten nuclear-powered ice-breakers, for example, of which seven are still active. The first nuclear-powered ship for carrying cargo and passengers was the NS Savannah, launched in 1962 as part of President Dwight D. Eisenhower's Atoms for Peace initiative. Powered by one 74 MW nuclear reactor, the Savannah had a service speed of 21 knots (39 km/h) and could carry 60 passengers and 14 000 t of cargo. (That's a cargo transport cost of 0.14 kWh per ton-km.) She could travel 300 000 miles without refuelling.

Hang on!

You haven't mentioned magnetic levitation

"driving without wheels; flying without wings"

The German company, Transrapid, which made the major maglev trains for Germany and China, says this:

The Transrapid Superspeed Maglev System is unrivaled when it comes to noise emission, energy consumption, and land use. The innovative non-contact transportation system provides mobility without the environment falling by the wayside.

Magnetic levitation is one of many technologies that gets hyped up when people are discussing energy issues.

In energy-consumption terms, the comparison with other fast trains is actually not as flattering as the hype suggests. From the Transrapid site:

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com



Figure 20.29. NS Savannah, the first commercial nuclear-powered cargo vessel, passing under the Golden Gate Bridge in 1962. She has one 74 MW reactor, and her motor can deliver 15 MW.



Figure 20.30. The nuclear ice-breaker Yamal, carrying 100 tourists to the North Pole in 2001. She has two 171 MW reactors, and her motors can deliver 55 MW. Photo by Wofratz.

Fast trains compared at 200 km/h (125mph)

ICE 2.9 kWh per 100 seat-km Transrapid 2.2 kWh per 100 seat-km

[The InterCityExpress or ICE compared here is a high-speed electric train.]

The main reasons why maglev is slightly better than the ICE are: the magnetic propulsion motor has high efficiency; the train itself has low mass, because most of the propulsion system is in the track, rather than the train; and more passengers are inside the train because space is not needed for motors. Oh, and perhaps because the data are from the maglev website, so are bound to make the maglev look better!

Incidentally, people who have experienced the Transrapid train in Shanghai tell me that at full speed it is "about as quiet as a jet aircraft."

Notes and further reading

page no.

- 127 A widely quoted statistic says "Only 1 percent of fuel energy in a car goes into moving the driver." In fact the percentage varies in size as it commutes around the urban community. Some people say "5% of the energy goes into moving the driver." Others say "A mere three tenths of 1 percent of fuel energy goes into moving the driver." [4qgg8q] My take, by the way, is that none of these statistics is correct or helpful.
 - The bicycle's performance is about the same as the eco-car's. Cycling costs about 1.6 kWh per 100 km, assuming a speed of 20 km/h. For details and references, see Chapter ??.
 - The 8-carriage stopping train from Cambridge to London weighs 275 tonnes, and can carry 584 passengers seated. Its maximum speed is 100 mph (161 km/h), and the power output is 1.5 MW. If all the seats are occupied, this train at top speed consumes at most 1.6 kWh per 100 passenger-km.
- 129 London Underground. A Victoria-line train consists of four 30.5-ton and four 20.5-ton cars (the former carrying the motors). Laden, an average train weighs 228 tons. The maximum speed is 45 mile/h. The average speed is 31 mph. A train with most seats occupied carries about 350 passengers; crush-loaded, the train takes about 620. The energy consumption at peak times is about 4.4 kWh per 100 passenger-km [Ridley and Catling, 1966].
 - High-speed train.

Intercity trains A diesel-powered intercity 125 train (on the right in figure 20.5) weighs 410 tons, and uses a power of 3.4 MW when travelling at 125 mph. (The power delivered "at the rail" is 2.6 MW.) Each second-class carriage can carry about 74 passengers. (It used to be 64 seats to a carriage, but they have squashed us up.) First-class carriages can carry









Figure 20.31. Nine out of ten vehicles in London are electric. (And 95% of statistics are made up.)

Car (100km): **80 kWh**

Train: 3 kWh

Figure 20.32. 100 km on a fully-occupied high-speed train, compared with 100 km in a single-person car.

about 48 passengers. So the number of passengers in a full train is about 500; and the power per person is about 7 kW. The transport efficiency is about 3.3 kWh per 100 seat-km.

The Class 91 electric train on the left travels at $140\,\mathrm{mph}$ ($225\,\mathrm{km/h}$) and uses $4.5\,\mathrm{MW}$.

Further evidence for a figure of 3 kWh per 100 seat-km: The government document [5fbeg9] says that east-coast mainline and west-coast mainline trains both consume about 15 kWh per km (whole train). The number of seats in each train is 526 or 470 respectively. So that's 2.9–3.2 kWh per 100 seat-km.

- the total energy cost of all London's underground trains, was 15 kWh per 100 passenger-km. ... The energy cost of all London buses was 32 kWh per 100 p-km. Source: [679rpc]. Source for train speeds and bus speeds: Ridley and Catling [1982].
 - The Croydon Tramlink system. http://www.tfl.gov.uk/assets/downloads/corporate/TfL-environment-report-2007.pdf http://www.tfl.gov.uk/assets/downloads/corporate/London-Travel-Report-2007-final.pdf http://www.croydon-tramlink.co.uk/
- 131 ... provision of excellent cycle facilities ... The UK street design guide [http://www.manualforstreets.org.uk/] encourages designing streets to make 20 miles/h the natural speed. See also Franklin [2007].
- 132 fair and simple method for handling congestion-charging. I learnt a brilliant way of automating congestion-charging from Stephen Salter. A simple daily congestion charge, as levied in London, sends only a crude signal to drivers; once a car-owner has decided to pay the day's charge and drive into a congestion zone, he has no incentive to drive *little* in the zone. Nor is he rewarded with any rebate if he carefully chooses routes in the zone that are not congested.

Instead of having a centralized authority that decides in advance when and where the congestion-charge zones are, with expensive monitoring and recording of vehicle movements into and within all those zones, Salter has a simpler, decentralized, anonymous method of charging drivers for driving in heavy, slow traffic, wherever and whenever it actually exists. The system would work nationwide. Here's how it works. We want a device that answers the question "how congested is the traffic I am driving in?" A good measure of congestion is "how many other active vehicles are close to mine?" In fast-moving traffic, the spacing between vehicles is larger than slow-moving traffic. Traffic that's trundling in tedious queues is the most densely packed. The number of nearby vehicles can be sensed by fitting in every vehicle a radio transmitter/receiver (like a very cheap mobile phone) that transmits little radio-bleeps at a steady rate whenever the engine is running, and which counts the number of bleeps it hears from other vehicles. The congestion charge would be proportional to the number of bleeps received; this charge could be paid at refuelling stations whenever the vehicle is refuelled. The radio transmitter/receiver would replace the current UK road tax disc.

- hydraulics and flywheels salvage at least 70% of the braking energy Compressed air is used for regenerative braking in big trucks. eaton.com say "hydraulic launch assist" captures 70% of the kinetic energy. [5cp27j]

 The flywheel system of flybridsystems.com also captures 70% of the kinetic energy. http://www.flybridsystems.com/F1System.html

 Electric regenerative braking salvages 50%. Source: E4tech [2007].
- 134 Electric batteries capable of delivering 60 kW would weigh about 200 kg. Good lithium-ion batteries have a specific power of 300 W/kg Horie et al. [1997], Mindl [2003].
 - the average new car in the UK emits 168 g CO₂ per km. This is the figure for the year 2006 [King, 2008]. The average emissions of a new passenger vehicle in the USA were 255 g per km [King, 2008].
 - The Toyota Prius has a more-efficient engine. The Prius's petrol engine uses the Atkinson cycle, in contrast to the conventional Otto cycle. By cunningly mixing electric power and petrol power as the driver's demands change, the Prius gets by with a smaller engine than is normal in a car of its weight, and converts petrol to work more efficiently than a conventional petrol engine.
 - Hybrid technologies give fuel savings of 20 or 30%. For example, from Hitachi's research report describing hybrid trains Kaneko et al. [2004]: high-efficiency power generation and regenerative braking are "expected to give fuel savings of approximately 20% compared with conventional diesel-powered trains."
- 135 Lots of electric vehicles. Here they all are, in no particular order. Performance figures are mainly from the manufacturers. As we saw on p135, real-life performance doesn't always match what manufacturers' claims.
- Th!nk Electric cars from Norway. The four-seat, two-door Th!nk city has a range of 170 km and weighs 1113 kg. Its energy consumption is approximately 19 kWh per 100 km. http://www.think.no/

Electric Smart Car "The electric version is powered by a 40 bhp motor, can go up to 70 miles before the battery goes flat and has a top speed of 70 mph. Recharging is done through a standard electrical power point and costs about £1.20, producing the equivalent of $60\,\mathrm{g/km}$ of carbon dioxide emissions at the power station, Smart says.

A full recharge takes about eight hours, but the battery can be topped up from 80%-drained to 80%-charged in about three-and-a-half hours." http://www.whatcar.com/news-article.aspx?NA=226488 (cf equivalent petrol-powered Smart: 116 g/km.)

Berlingo Electrique 500E, an urban delivery van, has 27 nicad batteries and a 28 kW motor. It can transport a payload of 500 kg. Top speed: 100 km/h; range: 100 km. 25 kWh per 100 km. (Estimate kindly supplied by a Berlingo owner.) [4wm2w4]

i MiEV This electric car from Mitsubishi is projected to have a range of $160\,\mathrm{km}$ with a $16\,\mathrm{kWh}$ battery pack. That's $10\,\mathrm{kWh}$ per $100\,\mathrm{km}$, a little better than

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com



Figure 20.33. Th!nk Ox. http://www.think.no/.



Figure 20.34. Toyota RAV4 EV. Photo by Kenneth Adelman, http://www.solarwarrior.com/.

20 — Better transport 145

- the G-Wiz and whereas it's hard to fit two adult Europeans in a G-Wiz, the Mitsubishi prototype has four doors and four full-size seats. [658ode]
- EV1 The two-seater General Motors EV1 had a range of 120 to 240 km per charge, with nickel-metal hydride batteries holding 26.4 kWh. That's an energy consumption of between 11 and 22 kWh per 100 km.
- eBox The eBox has a lithium-ion battery with a capacity of 35 kWh and a weight of 280 kg; and a range of 140–180 miles. Its motor has a peak power of 120 kW peak and can produce a sustained power of 50 kW. Efficiency: 12 kWh per 100 km if carrying a single occupant; 3 kWh per 100 seat-km if four seats are used.
- Ze-0 A five-seat, five-door car. Maximum speed: 50 mph. Range: 50 miles. Weight, including batteries: 1350 kg. Lead acid batteries with capacity of 18 kWh. Motor: 15 kW. 22.4 kWh per 100 km.
- e500 An Italian Fiat-like car, with two doors and 4 seats. Maximum speed: 60 mph. Range in city driving: 75 miles. Battery: lithium-ion polymer.
- MyCar The MyCar is an Italian-designed two-seater. Maximum speed: up to 40 mph. Maximum range: up to 60 miles. Lead-acid battery.
- Mega City A two-seater car with a maximum continuous power of 4 kW and maximum speed of 40 mph: 11.5 kWh per 100 km. Weight unladen (but including batteries) 725 kg. The lead batteries have a capacity of 10 kWh.
- Aptera This fantastic slippery fish is a two-seater vehicle, said to have an energy cost of 6kWh per 100km. It has a drag coefficient of 0.11. Electric and hybrid models are being developed.
- Xebra Claims 40 km range from a 4.75 kWh charge. Lead-acid batteries. 12 kWh per 100 km. Maximum speed 65 km/h.
- Venturi Fetish Has a 28 kWh battery, weighing 248 kg. Range 160-250 km. Car weighs 1000 kg. That's 11-17 kWh per 100 km. http://www.venturifetish.fr/fetish.html
- Toyota RAV4 EV This vehicle an all-electric mini-SUV was sold by Toyota between 1997 and 2003. The RAV4EV has 24 12-volt 95Ah NiMH batteries capable of storing 27.4 kWh of energy. Range of 130 to 190 km. So that's an energy consumption of 14–21 kWh per 100 km. The RAV4EV was popular with Jersey Police force.
 - Kaz An 8-passenger 8-wheel vehicle that never made it into production. Weight: 3000 kg. Range: 300 km at 100 km/h. 20 kWh per 100 km. Top speed 311 km/h.
 - http://www.electrifyingtimes.com/kaz.html
- Phoenix SUT a five-seat "sport utility truck" made in California has a range of "up to 130 miles" from a 35 kWh lithium-ion battery pack. (That's 17 kWh per 100 km.) The batteries can be recharged from a special outlet in 10 minutes. http://www.gizmag.com/go/7446/

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com



Figure 20.35. The i MiEV. From Mitsubishi Motors Corporation. It has a 47 kW motor, weighs 1080 kg, and has a top speed of 130 km/h.



Figure 20.36. The Aptera. 6 kWh per 100 km.

Modec delivery vehicle http://www.modec.co.uk/ Modec carries two tons a distance of 100 miles. Kerb weight 3000 kg.

Electric minibus From http://www.smithelectricvehicles.com/:
40 kWh lithium ion battery pack. 90 kW motor with regenerative brakes.
Range 'up to 100 miles'. 15 seats. Vehicle kerb weight 3026 kg. Payload 1224 kg. That's a vehicle-performance of at best 25 kWh per 100 km. If the vehicle is fully occupied, it could deliver transportation at an impressive cost of 2 kWh per 100 p-km.

Smith Ampere Smaller delivery van, 24 kWh Lithium ion. Range "over 100 miles." http://www.smithelectricvehicles.com/

Electric coach The Thunder Sky bus has a range of 180 miles and a recharge time of three hours. http://www.thunder-sky.com/

Electric scooters The Vectrix is a substantial scooter. Its battery (nickel metal hydride) has a capacity of 3.7 kWh. It can be driven for up to 68 miles at 25 miles/h (40 km/h), on a two-hour charge from a standard electrical socket. That's 110 km for 3 kWh, or 2.75 kWh per 100 km. It has a maximum speed of 62 mph (100 km/h). It weighs 210 kg and has a peak power of 20 kW. http://www.vectrix.com/

The "Oxygen Cargo" is a smaller scooter. It weighs 121 kg, has a 38 mile range, and takes 2–3 hours to charge. Peak power: 3.5 kW; maximum speed 28 mph. It has two lithium-ion batteries and regenerative brakes. The range can be extended by adding extra batteries, which store about 1.2 kWh and weigh 15 kg each. Transport energy cost: 4 kWh per 100 km.

- the energy-density of compressed-air energy-stores is only about 11–28 Wh per kg The theoretical limit, assuming perfect isothermal compression: if 1 m³ of ambient air is slowly compressed into a 5-litre container at 200 bar, the potential energy stored is 0.16 kWh in 1.2 kg of air. In practice, a 5-litre container appropriate for this sort of pressure might weigh about 7.5 kg if made from steel or 2 kg using kevlar or carbon fibre, and the overall energy density achieved would be about 11–28 Wh per kg. The theoretical energy density is the same, whatever the volume of the container.
 - Arnold Schwarzenegger ... filling up a hydrogen-powered Hummer. Nature 438, 24 November 2005.

I'm not saying that hydrogen will *never* be useful for transportation; but I would hope that such a distinguished journal as *Nature* would address the hydrogen bandwagon with some critical thought, not only euphoria. Perhaps this quote is relevant:

Hydrogen and fuel cells are not the way to go. The decision by the Bush administration and the State of California to follow the hydrogen highway is the single worst decision of the past few years.

James Woolsey, Chairman of the Advisory Board of the US Clean Fuels Foundation, 27th November 2007.

- 138 In the Clean Urban Transport for Europe project the overall energy required to power the hydrogen buses was between 80% and 200% greater
- © David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com



Figure 20.37. Vectrix: 2.75 kWh per 100 km. http://www.vectrix.com/

20 — Better transport 147

than that of the baseline diesel bus. . Source: CUTE [2006], Binder et al. [2006].

— Fuelling the hydrogen-powered car made by BMW requires three times more energy than an average car. Half of the boot of the BMW "Hydrogen 7" car is taken up by its 170-litre hydrogen tank, which holds 8 kg of hydrogen, giving a range of 200 km on hydrogen. http://news.bbc.co.uk/1/hi/business/6154212.stm The calorific value of hydrogen is 39 kWh per kg, and the best-practice energy cost of making hydrogen is 63 kWh per kg (made up of 52 kWh of natural gas and 11 kWh of electricity) [CUTE, 2006]. So filling up the 8 kg tank has an energy cost of at least 508 kWh; and if that tank indeed delivers 200 km, then the energy cost is 254 kWh per 100 km. This is more than three times the energy consumption of an average European fossil-fuel car, which costs 80 kWh per 100 km (as we'll see on p32).

The Hydrogen 7 and its hydrogen-fuel-cell cousins are, in many ways, simply flashy distractions.

David Talbot, MIT Technology Review http://www.technologyreview.com/Energy/18301/

Honda's fuel-cell car, the FCX Clarity, weighs 1625 kg, stores 4.1 kg of hydrogen at a pressure of 345 bar, and is said to have a range of 280 miles, consuming 57 miles of road per kg of hydrogen (91 km per kg) in a standard mix of driving conditions [czjjo], [5a3ryx]. Using the cost for creating hydrogen mentioned above, assuming natural gas is used as the main energy source, this car has a transport cost of 69 kWh per 100 km.

Honda might be able to kid journalists into thinking that hydrogen cars are "zero emission" but unfortunately they can't fool the climate.

Merrick Godhaven

- 139 A lithium-ion battery is 3% lithium. Source: Fisher et al. [2006].
 - Lithium specialist R. Keith Evans says "concerns regarding lithium availability ... are unfounded." Evans [2008]
- 141 Two Dutch-built liners known as "The Economy Twins." http://www.ssmaritime.com/rijndam-maasdam.htm

Range Only 8.3% of commuters travel over 30 km to their workplace. Eddington [2006]

Electric trams Battery-powered electric trams - further reading: http://www.tdi.uk.com/, http://www.tbus.org.uk, http://www.scottishelectrictransit.org.uk



Figure 20.38. Tram 147 in Blackpool. Photo from www.blackpool.gov.uk.



21 Smarter heating

In the last chapter, we learned that electrification could shrink transport's energy consumption to one fifth of its current levels; and that public transport and cycling can be about 40 times more energy-efficient than cardiving. How about heating? What sort of energy-savings can technology or lifestyle-change offer?

The power used to heat a building is given my multiplying together three quantities:

$$power used = \frac{average \ temperature \ difference \times leakiness \ of \ building}{efficiency \ of \ heating \ system}.$$

Let me explain this formula (which is discussed in detail in Chapter E) with an example. My house is a three-bedroom semi-detached house built about 1940 (figure E.6). The average temperature difference between the inside and outside of the house depends on the setting of the thermostat and on the weather. If the thermostat is at 20 °C, the average temperature difference might be 9 °C. The *leakiness* of the building describes how quickly heat gets out through walls, windows, and cracks, in response to a temperature difference. The leakiness is sometimes called the *heat-loss coefficient* of the building. It is measured in kWh per day per degree of temperature difference. In Chapter E I work out that the leakiness of my house in 2006 was 7.7 kWh/d/°C. The product

average temperature difference × leakiness of building

is the rate at which heat flows out of the house by conduction and ventilation. For example, if the average temperature difference is $9\,^\circ\text{C}$ then the heat loss is

$$9 \,^{\circ}\text{C} \times 7.7 \,\text{kWh/d/}^{\circ}\text{C} \simeq 70 \,\text{kWh/d}$$

Finally, to calculate the power required, we divide the heat loss by the efficiency of the heating system. In my house, the condensing gas boiler has an efficiency of 90%, so we find:

power used =
$$\frac{9 \text{ °C} \times 7.7 \text{ kWh/d/°C}}{0.9} = 77 \text{ kWh/d}.$$

That's bigger than the space-heating requirement we estimated in Chapter 7. It's bigger for two reasons: first, this formula assumes that all the heat is supplied by the boiler, whereas in fact some heat is supplied by incidental heat gains from occupants, gadgets, and the sun; second, in Chapter 7 we assumed that one kept just two rooms at 20 °C all the time; keeping an entire house at this temperature all the time would require more.

OK, how can we reduce the power used by heating? Well, obviously, there are three lines of attack.



Figure 21.1. My house.

21 — Smarter heating 149

1. Reduce the average temperature difference. This can be achieved by turning thermostats down (or, if you have friends in high places, by changing the weather).

- 2. Reduce the leakiness of the building. This can be done by improving the building's insulation think double glazing, draught-proofing, and fluffy blankets in the loft or, more radically, by knocking the building down and replacing it with a better insulated building, or perhaps by a building of smaller size per person. (Leakiness tends to be bigger, the bigger a building's floor area.)
- 3. Increase the efficiency of the heating system. You might think that 90% sounds hard to beat, but actually we can do much better.

Cool technology: the thermostat

The thermostat (accompanied by woolly jumpers) is hard to beat, when it come to value-for-money technology. You turn it down, and your building uses less energy. Magic! In Britain, for every degree that you turn the thermostat down, the heat loss decreases by about 10%. Turning the thermostat down from 20 $^{\circ}\text{C}$ to 15 $^{\circ}\text{C}$ would nearly halve the heat loss. Thanks to incidental heat gains by the building, the savings in heating power will be even bigger than these reductions in heat loss.

Unfortunately, however, this remarkable energy-saving technology has side-effects. Some humans call turning the thermostat down a lifestyle change, and are not happy with it. I'll make some suggestions later about how to finesse this lifestyle issue. Meanwhile, as proof that "the most important smart component in a building with smart heating is the occupant," figure 21.2 shows data from a Carbon Trust study, observing the heat consumption in twelve identical modern houses. This study permits us to gawp at the family at number 1, whose heat consumption is twice as big as that of Mr. and Mrs. Woolly at number 12. However, we should pay attention to the numbers: the family at number 1 are using 43 kWh per day. But if this is shocking, hang on – a moment ago, didn't I estimate that my house might use more than that? Indeed, my average gas consumption from 1993 to 2003 was a little more than 43 kWh per day, and I thought I was a frugal person; looking carefully at the caption, all the modern houses in the Carbon Trust study had a leakiness of 2.7 kWh/d/°C; while my house had a leakiness of 7.7kWh/d/°C! People who live in leaky houses...!

The war on leakiness

What can be done with leaky old houses, apart from calling in the bull-dozers? Figure 21.3 shows estimates of the space heating required in old

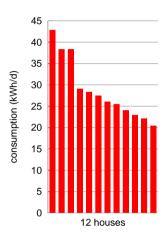


Figure 21.2. Actual heat consumption in 12 identical houses with identical heating systems. All houses were designed to have a leakiness of 2.7 kWh/d/°C. Source: Carbon Trust [2007].

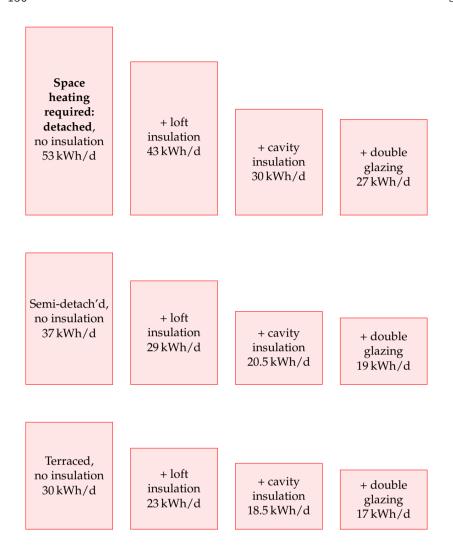


Figure 21.3. Estimates of the space heating required in a range of UK houses. From Eden and Bending [1985].

detached, semi-detached, and terraced houses as progressively more effort is put into patching them up. The addition of loft insulation and cavity-wall insulation reduces heat loss in a typical old house by about 25%. Thanks to incidental heat gains, this 25% reduction in loss translates into roughly a 40% reduction in heating consumption.

Let's put these ideas to the test.

A case study

I introduced you to my house on p57. Let's pick up the story where we left it. In 2004 I had a condensing boiler installed, replacing the old gas boiler. At the same time I removed the house's hot water tank (so hot water is now made only on demand), and I put thermostats on all the bedroom

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

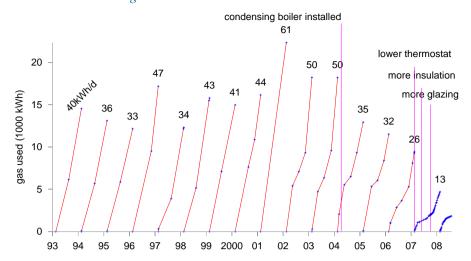


Figure 21.4. My domestic gas consumption, each year from 1993 to 2007. Each line shows the cumulative consumption during one year in kWh. The number at the end of each year is the average rate of consumption for that year, in kWh per day.

radiators. Along with the new condensing boiler came a new heating controller allowing me to set different target temperatures for different times of day.

With these changes, my consumption decreased from an average of 50 kWh/d to about 32 kWh/d.

This reduction from 50 to $32 \,\text{kWh/d}$ is quite satisfying, but it's not enough, if the aim is to reduce one's fossil fuel footprint below one ton of CO_2 per year. $32 \,\text{kWh/d}$ of gas corresponds to over 2 tonnes CO_2 per year.

In 2007, I started paying more careful attention to my energy meters. I had cavity-wall insulation installed and improved my loft insulation. Most important of all, I paid more attention to my thermostat settings. This attentiveness has led to a further halving in gas consumption. The latest year's consumption was 13 kWh/d!

I'm sorry that this case study is such a hodge-podge of building modifications and behaviour changes – it makes it hard to be sure which changes were the most important. According to my calculations, the improvements in insulation reduced the leakiness by 25%, from $7.7\,\mathrm{kWh/d/^\circ C}$ to $5.8\,\mathrm{kWh/d/^\circ C}$. This is still much leakier than any modern house. It's frustratingly difficult to reduce the leakiness of an already-built house.

So, my tip is cunning thermostat management. What's a reasonable thermostat setting to aim for? Nowadays many people seem to think that 17 °C is unbearably cold. However, the average winter-time temperature in British houses in 1970 was 13 °C! A human's perception of whether they feel warm enough depends on what they are doing, and what they've been doing for the last hour or so. My suggestion is, *don't think in terms of a thermostat setting*. Rather than fixing the thermostat to a single value, try setting it to a really low value most of the time (say 13 or 15 °C), and turn it up temporarily whenever you feel cold. It's like the lights in a library. If you ask "what is the right light level in the bookshelves?" then you'll no doubt answer "bright enough to read the book titles," and you'll have



Figure 21.5. Cavity-wall insulation going in.

bright lights on all the time. But that question presumes that we have to fix the light level; and we don't have to. In wonderful Cambridge University Library – a quirky institution where the books are sorted by size, to save shelf space – the lights of every shelf-stack are individually switch-on-able by the reader, and they are on clockwork timers so that they switch off again within a few minutes.

Before we leave the topic of thermostats, we should mention air-conditioning. It drives me crazy to go into a building in summer where the thermostat of the air-conditioning is set to $18\,^{\circ}$ C. These loony building managers are subjecting everyone to temperatures that in winter-time they would whinge are too cold! In Japan, the government's "CoolBiz" guidelines recommend that air-conditioning be set to $28\,^{\circ}$ C (82 F).

The energy cost of heat

Now we turn to the third factor in the equation:

$$\frac{\text{power used}}{\text{efficiency of heating system}} = \frac{\text{average temperature difference} \times \text{leakiness of building}}{\text{efficiency of heating system}}$$

How efficiently can heat be produced? Can we get heat on the cheap? Today, building-heating is primarily delivered by natural gas. Can we get off fossil fuels at the same time as making building-heating more efficient?

One technology that is held up as an answer to Britain's heating problem is called "combined heat and power" (CHP), or its cousin, "micro-CHP." I will explain combined heat and power now, but I've come to the conclusion that it's a bad idea, because there's a better technology for heating, called heat pumps, which I'll describe in a few pages.

Combined heat and power

The standard view of conventional big centralised power stations is that they are terribly inefficient, chucking heat willy-nilly up chimneys and cooling towers. A more sophisticated view recognizes that to turn thermal energy into electricity, we inevitably have to dump heat in a cold place (figure 21.7). That is how heat engines work. There *has* to be a cold place. But surely, it's argued, we could use *buildings* as the dumping place for this "waste" heat instead of cooling towers or sea water? This idea is called "combined heat and power" (CHP) or cogeneration, and it's been widely used in continental Europe for decades – in many cities, a big power station is integrated with the city's centralized district heating system. Proponents of the modern incarnation of combined heat and power, "micro-CHP," suggest that new tiny power stations should be created within single buildings or small collections of buildings, delivering heat and electricity to those buildings, and exporting some electricity to the grid.







Figure 21.6. Eggborough. Not a power station participating in smart heating.

21 — Smarter heating 153

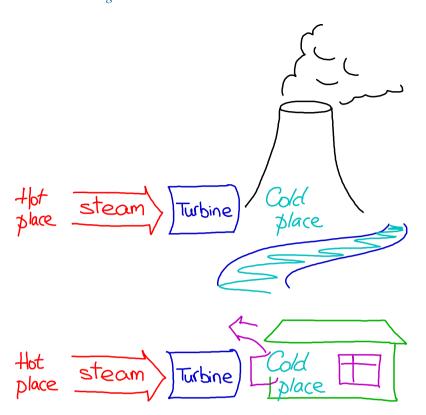


Figure 21.7. How a power station works. There has to be a cold place to condense the steam to make the turbine go round. The cold place is usually a cooling tower or river.

Figure 21.8. Combined heat and power. District heating absorbs heat that would have been chucked up a cooling tower.

There's certainly some truth in the view that Britain is rather backward when it comes to district heating and combined heat and power, but discussion is hampered by a general lack of numbers, and by two particular errors. First, when comparing different ways of using fuel, the wrong measure of "efficiency" is used, namely one that weights electricity as having equal value to heat. Electricity is more valuable than heat. Second, it's widely assumed that the "waste" heat in a traditional power station could be captured for a useful purpose without impairing the power station's electricity production. This sadly is not true, as the numbers will show. Delivering useful heat to a customer always reduces the electricity produced to some degree. The true net gains from combined heat and power are often much smaller than the hype would lead you to believe. (Just 10% or so.)

A final impediment to rational discussion of combined heat and power is an unfounded assumption that has grown up recently, that decentralizing a technology somehow makes it greener. So whereas big centralized fossil fuel power stations are "bad," flocks of local micro-power stations are imbued with goodness. But if decentralization is actually a good idea then "small is beautiful" should be evident in the numbers. Decentralization should be able to stand on its own two feet. And what the numbers actually show is that *centralized* electricity generation has many benefits in both economic and energy terms. Only in large buildings is there any

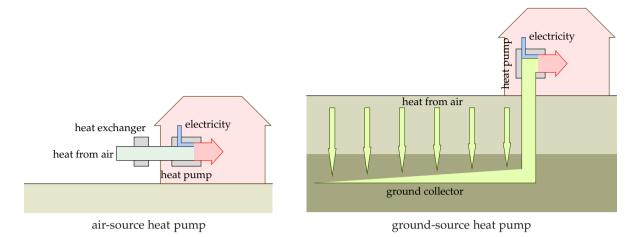


Figure 21.9. Heat pumps

benefit to local generation, and usually that benefit is only about 10% or 20%. And what we'll see in a moment is that there is another technology that is superior to combined heat and power: this technology is the heat pump. Like district heating and combined heat and power, heat pumps are already widely used in continental Europe. In contrast to most combined heat and power systems, heat pumps are not locked in to a fossil fuel such as gas.

The government has a target for growth of combined heat and power to 10 GW(e) by 2010, but I think that growth of gas-powered combined heat and power would be a mistake. Such combined heat and power is not green: it uses fossil fuel, and it locks us into continued use of fossil fuel. Given that heat pumps are a better technology, I believe we should leapfrog over gas-powered combined heat and power.

Heat pumps

Heat pumps are back-to-front refrigerators. Feel the back of your refrigerator: it's warm. A refrigerator moves heat from one place (its inside) to another (its back panel). So one way to heat a building is to turn a refrigerator inside-out – put the *inside* of the refrigerator in the garden, thus cooling the garden down; and leave the outside of the refrigerator in your kitchen, thus warming the house up. What isn't obvious is that this is a really efficient way to warm your house. For every kilowatt of power drawn from the electricity grid, the back-to-front refrigerator can pump three kilowatts of heat from the garden, so that a total of four kilowatts of heat gets into your house. So heat pumps are roughly four times as efficient as a standard electrical bar-fire.

Heat pumps can be configured in various ways. Your pump can cool down the *air* in your garden using a heat-exchanger (typically a 1-metre tall white box), in which case it's called an air-source heat pump. Alternatively,

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

21 — Smarter heating 155

the pump may cool down the ground using big loops of underground plumbing (many tens of metres long), in which case it's called a groundsource heat pump. Heat can also be pumped from rivers and lakes.

Heat pumps can usually be pump heat in either direction. If you reverse an air-source heat pump, it uses electricity to warm up the outside air and cool down the air inside your building. This is called air-conditioning, and it's exactly how many air-conditioners work. Many air-conditioners are heat-pumps. Ground-source heat pumps can also work as air-conditioners. So a single piece of hardware can be used to provide winter heating and summer cooling.

People sometimes say that ground-source heat pumps are using "geothermal energy," but that's not the right name. As we saw in Chapter 16, geothermal energy offers only a tiny trickle of power per unit area (about 50 mW/m²), in most parts of the world; but heat pumps can be used everywhere, and they can be used both for heating and for cooling. Heat pumps simply use the ground as a place to suck heat from, or to dump heat into.

There's two things left to do in this chapter. We need to compare heat pumps with combined heat and power. Then we need to discuss what are the limits to ground-source heat pumps.

Heat pumps, compared with combined heat and power

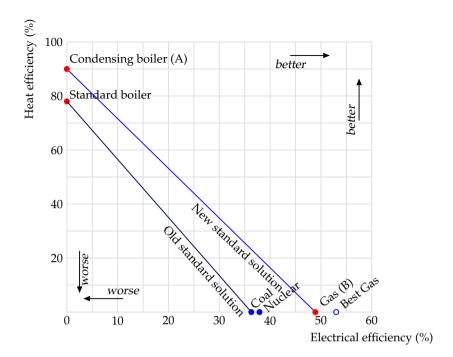
I used to think that combined heat and power was a no-brainer. "Obviously, we should use the discarded heat from power stations to heat buildings rather than just chucking it up a cooling tower!" However, looking carefully at the numbers describing the performance of real CHP systems, I've come to the conclusion that there are better ways of providing electricity and building-heating.

I'm going to build up a diagram in three steps. The diagram shows what electrical energy or heat energy can be delivered from chemical energy.

The standard solution with no CHP

In the first step, we show simple power stations and heating systems that deliver pure electricity or pure heat.

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

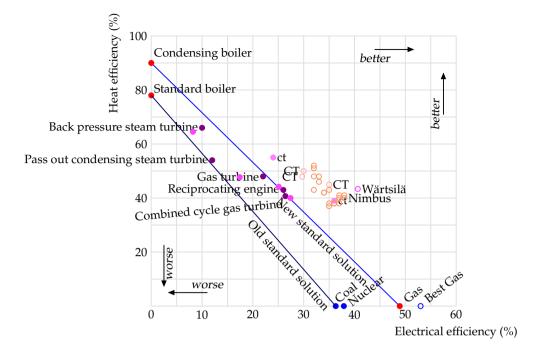


Condensing boilers (the top-left dot, A) are 90% efficient because 10% of the heat goes up the chimney. Britain's gas power stations (the bottom-right dot, B) are currently 49% efficient at turning the chemical energy of gas into electricity. If you want any mix of electricity and heat, you can obtain it by burning appropriate quantities in the electricity power station and in the boiler. Thus the new standard solution can deliver any electrical efficiency and heat efficiency up to the line A–B.

Combined heat and power

Next we add combined heat and power systems to the diagram. These simultaneously deliver, from chemical energy, some electricity and some heat.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com



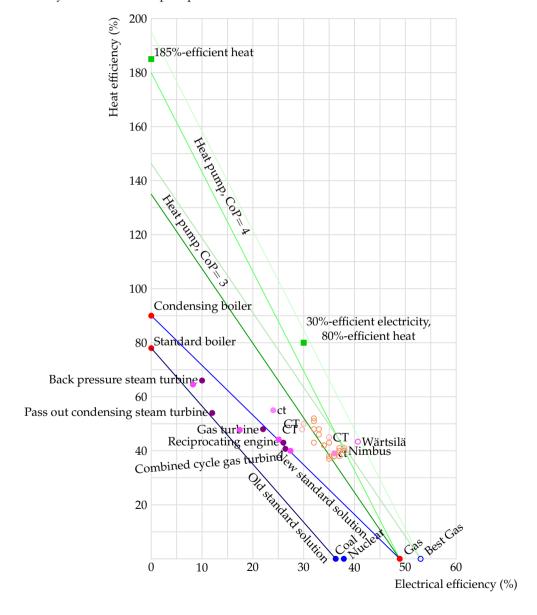
Each of the filled dots shows actual average performances of CHP systems in the UK, grouped by type. The hollow dots marked "CT" show the performances of ideal CHP systems quoted by the Carbon Trust; the hollow dots marked "Nimbus" are from a manufacturer's spec sheets. The dots marked "ct" are the performances quoted by the Carbon Trust for two real systems (at Freeman hospital and Elizabeth house). It's common practice to lump together the two numbers (the efficiency of electricity production and heat production) into a single "total efficiency" – for example, the back pressure steam turbines delivering 10% electric and 66% heat would be called "76% efficient," but I think this is a poor summary of performance. After all, by this measure, the condensing boiler is "more efficient" than all the CHP systems! The fact is, electrical energy is more valuable than heat.

Many of the CHP points in this figure are superior to the "old standard way of doing things" (getting electricity from coal and heat from standard boilers). And the ideal CHP systems are slightly superior to the "new standard way of doing things" (getting electricity from gas and heat from condensing boilers). But we must bear in mind that this slight superiority comes with some drawbacks – a CHP system delivers heat only to the places it's connected to, whereas condensing boilers can be planted anywhere with a gas main; and compared to the standard way of doing things, CHP systems are not so flexible in the mix of electricity and heat they deliver; a system will work best when delivering a particular mix; this inflexibility leads to inefficiencies at times when, for example, excess heat is produced; in a typical house, much of the electricity demand comes

in relatively brief spikes, bearing little relation to heating demand. A final problem with some micro-CHP systems is that when they have excess electricity to share, they may do a poor job of delivering power to the network.

One exceptional CHP system – the Wärtsilä 34SG – has specifications significantly better than all those described by the Carbon Trust. The spec sheets for a CHP engine for district heating claim an electrical efficiency of 41% and a heat efficiency of 43%.

Finally we add in heat pumps.



© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

The steep lines show the combinations of electricity and heat that you can obtain assuming that heat pumps have a coefficient of performance of 3 or 4, assuming the electricity is generated by an average gas power station or by a top-of-the-line gas power station, and allowing for 8% loss in the national electricity network between the power station and the building where the heat pumps pump heat. The top-of-the-line gas power station's efficiency is 53%, if it's running at its optimal setting. I imagine the Carbon Trust (CT) and Nimbus made a similar assumption when providing the numbers used in this diagram for CHP. In the future, heat pumps will probably get even better than I assumed here. In Japan, thanks to strong legislation favouring efficiency improvements, heat pumps are now available with a coefficient of performance of 4.9.

Notice that heat pumps offer a system that can be "better than 100%-efficient." For example the "best gas" power station with heat pumps can deliver a combination of 30%-efficient electricity and 80%-efficient heat, a total efficiency of 110%. No plain CHP system could ever match this performance.

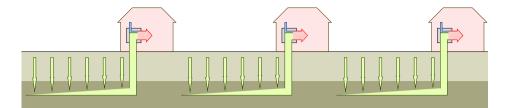
Let me spell this out. Heat pumps are superior in efficiency to condensing boilers, even if the heatpumps are powered by electricity from a power station burning natural gas. If you want to heat lots of buildings using natural gas, you could install condensing boilers, which are "90% efficient," or you could put up a new gas power station and install heat pumps in all the buildings; the second solution's efficiency would be somewhere between 140% and 185%. It's not necessary to dig big holes in the garden and install under-floor heating to get the benefits of heat pumps; the best air-source heat pumps (which require just a small external box, like an air-conditioner's) can deliver hot water to normal radiators with a coefficient of performance above 3.

I thus conclude that combined heat and power, even though it sounds a good idea, is probably not the best way to heat buildings and make electricity using natural gas, assuming that air-source or ground-source heat pumps can be installed in the buildings. The heat-pump solution has further advantages that should be emphasized: heat pumps can be located in any buildings where there is an electricity supply; they can be driven by any electricity source, so they keep on working when the gas runs out or the gas price goes through the roof; and heat pumps are flexible: they can be turned on and off to suit the demand of the building occupants.

I emphasize that this critical comparison does not mean that CHP is always a bad idea. What I'm comparing here are methods for heating ordinary buildings, which requires only very low-grade heat. CHP can also be used to deliver higher-grade heat to industrial users (at $200\,^{\circ}$ C, for example). In such industrial settings, heat pumps are unlikely to compete well because their coefficient of performance would not be so big.



Figure 21.10. The inner and outer bits of an air-source heat pump that has a coefficient of performance of 4. The inner bit is accompanied by a ball-point pen, for scale. One of these Fujitsu units can deliver 3.6 kW of heating when using just 0.845 kW of electricity. It can also run in reverse, delivering 2.6 kW of cooling when using 0.655 kW of electricity.



Limits to growth (of heat pumps)

Because the temperature of the ground, a few metres down, stays sluggishly close to $11\,^{\circ}$ C, whether it's summer or winter, the ground is theoretically a better place for a heat pump to grab its heat from than the air, which in midwinter may be ten or fifteen degrees cooler. So heat-pump advisors encourage the choice of ground-source over air-source heat pumps, where possible.

However, the ground is not a limitless source of heat. The heat has to come from somewhere, and ground is not a very good conductor of heat. If we suck heat too hard from the ground, the ground will become as cold as ice, and the advantage of the ground-source heat pump will be diminished. (Heat pumps don't work quite so efficiently when there's a big temperature difference between the inside and outside.)

In Britain, the main purpose of heat pumps would be to get heat into buildings in the winter. The ultimate source of this heat is the sun, which replenishes heat in the ground by direct radiation and by conduction through the air. The rate at which heat is sucked from the ground must satisfy two constraints: it must not cause the ground's temperature to drop too low during the winter; and the heat sucked in the winter must be replenished during the summer. If there's any risk that the natural trickling of heat in the summer won't make up for the heat removed in the winter, then the system must be run in reverse in summer, putting heat down into the ground (and thus providing air-conditioning up top).

Let's put some numbers into this discussion. How big a piece of ground does a heat pump need? And is it feasible to store up a load of heat over the summer and suck it back again in the winter?

Assume that we have a neighbourhood with quite a high population density – say 6200 people per km² (160 m² per person), the density of a typical English suburb. Can *everyone* use ground-source heat pumps, without using the summer replenishment trick? A calculation on p322 gives a tentative answer of *no*: if we were aiming for everyone in the neighbourhood to be able to pull from the ground a heat flow of about 48 kWh/d per person (my estimate of our typical winter heat demand), we'd end up freezing the ground in the winter. Avoiding unreasonable cooling of the ground requires that the sucking rate be less than 12 kWh/d per person. So when we switch to heat pumps, we should plan to include substantial summer heat-dumping in the design, to refill the ground with heat for use in the

Figure 21.11. How close together can ground-source heat pumps be packed?

area per person (m ²)		
Bangalore	37	
Manhattan	39	
Paris	40	
Chelsea	66	
Tokyo	72	
Moscow	97	
Taipei	104	
The Hague	152	
San Francisco	156	
Singapore	156	
Cambridge MA	164	
Sydney	174	
Portsmouth	213	

Table 21.12. Some urban areas per person.

161 21 — Smarter heating

winter. This summer heat-dumping could use heat from air-conditioning, or heat from roof-mounted solar water-heating panels. (Summer solar heat is stored in the ground for subsequent use in winter by Drake Landing Solar Community in Canada http://www.dlsc.ca/.) Alternatively, we should expect to need to use some air-source heat pumps too, and then we'll be able to get all the heat we want - as long as we have the electricity to pump it. In the UK, air temperatures don't go very far below freezing, so concerns about poor winter-time performance of air-source pumps, which might apply in North America and Scandanavia, probably do not apply in Britain.

My conclusion: can we reduce the energy we consume for heating? Yes. Can we get off fossil fuels at the same time? Yes. Not forgetting the low-hanging fruit - building-insulation and thermostat shenanigans - we should replace all our fossil-fuel heaters with electric-powered heat pumps, we can reduce the energy required to 25% of today's levels. Of course this plan for electrification would require more electricity. But even if the extra electricity came from gas-fired power stations, that would still be a much better way to get heating than what we do today, simply setting fire to the gas. Heat-pumps are future-proof, allowing us to heat buildings efficiently with electricity from any source.

Nay-sayers object that the coefficient of performance of air-source heat pumps is lousy – just 2 or 3. But their information is out of date. If we are careful to buy top-of-the-line heat pumps, we can do much better. The Japanese government legislated a decade-long efficiency drive that has greatly improved the performance of air-conditioners; thanks to this drive, there are now air-source heat pumps with a coefficient of performance of 4.9; these heat pumps can make hot water as well as hot air. http: //www.ecosystem-japan.com/

Another objection to heat pumps is "oh, we can't approve of people fitting efficient air-source heaters, because they might use them for airconditioning in the summer." Come on – I hate gratuitous air-conditioning as much as anyone, but these heat pumps are four times more efficient than any other winter heating method! Show me a better choice. Wood pellets? Sure, some people can burn wood. But there is not enough wood for everyone to do so. For forest-dwellers, there's wood. For the rest of us, there's heat pumps.

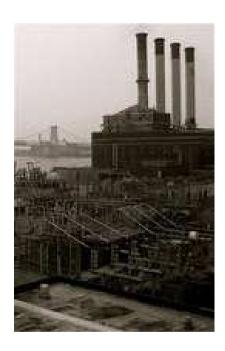


page no.

- 150 Loft and cavity insulation reduces heat loss in a typical old house by about
- 153 Britain is rather backward when it comes to district heating and combined heat and power. The rejected heat from UK power stations could meet

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

a quarter. Eden and Bending [1985]. the heating needs of the entire country [Wood, 1985]. In Denmark (in



1985 at least), district heating systems supply 42% of space heating, with heat being transmitted 20 km or more in hot pressurized water. In West Germany in 1985, four million dwellings received 7 kW per dwelling from district heating. Two thirds of the heat supplied was from power stations. These German district heating schemes were profitable. In Vasteras, Sweden in 1985, 98% of the city's heat was supplied from power stations.

(from Mott MacDonald 2001). 80% of the CHP capacity in the UK, which totals 4.2 GW(e) and 15 GW(th), is in large schemes (>10 MW). (81 installations)

Efficiency of the dominant technology: The biggest generator of CHP is combined-cycle natural gas. In 2005, it generated 17 347 GWh(e) and 26 740 GWh(th), using fuel with an energy of 65 701 GWh. That's 26.4% efficient electricity, 40.7% efficient thermal, overall efficiency 67%.

?? [36w8o7].

Some heat pumps available in the UK already have a COP bigger than 4.0 [yok2nw]. Indeed there is a government subsidy for water-source heat pumps that applies only to pumps with a COP better than 4.4 [2dtx8z]. Residential ground-source heatpumps are available with a coefficient of performance of 5.7 for cooling and 4.3 for heating. Commercial ground-source heatpumps are available with a coefficient of performance of 5.4 for cooling and 4.9 for heating. [2fd8ar]

To look into: In Switzerland, Heat Pumps, They have a fieldstudy running called FAWA which has been looking at 221 Heat Pumps (Air, Water, Brine) over the past 15 years or so. The best HP (which are in the study, so not the best you can get on the market today!) operate with a performance of 5.59 (Brine) and 3.38 (Air).

According to HPTCJ [2007], heat pumps with a coefficient of performance of 6.6 have been available in Japan since 2006. The performance of heat pumps in Japan improved from 3 to 6 within a decade thanks to government regulations. HPTCJ [2007] also describe an air-source-heat-pump water-heater called Eco Cute with a coefficient of performance of 4.9. The Eco Cute came on the market in 2001.

Summer heat storage In the Netherlands, summer heat from roads is stored in aquifers until the winter; and delivered to buildings via heat pumps: [2wmuw7].

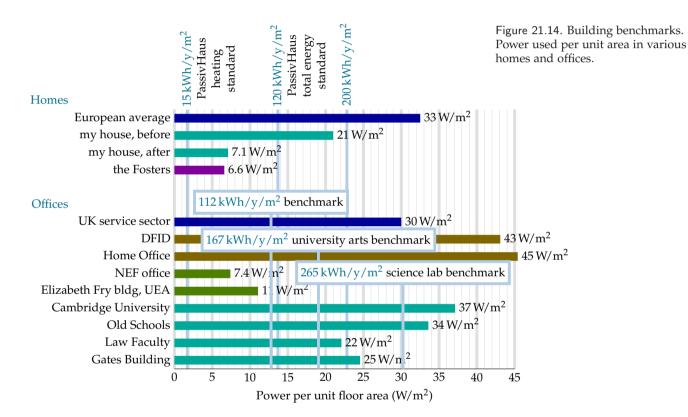
Further reading on heat pumps European Heat Pump Network

http://ehpn.fiz-karlsruhe.de/en/ http://www.kensaengineering.com/ http://www.iceenergy.co.uk/

Compare figure 21.14 with the other figures that show renewable power densities in W/m^2 . Then realize how difficult it is to power modern buildings entirely from on-site renewables. The power density of biofuels (figure 6.11, p45) is $0.5 W/m^2$; of windfarms, $2 W/m^2$; of solar photovoltaics,

(c) David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

21 — Smarter heating 163



 $20\,W/m^2(figure~6.18,~p49);$ only solar hot-water panels come in at the right sort of power density, $53\,W/m^2(figure~6.3,~p41).$

22 Efficient electricity use

Can we cut electricity use? Yes, switching off gadgets when they're not in use is an easy way to make a difference. Energy-efficient light bulbs will save you electricity too.

We already examined gadgets in Chapter 11. Some gadgets are unimportant, but some are astonishing guzzlers. The laser-printer in my office, sitting there doing nothing, is slurping nearly 0.5 kWh per day! If you add up a few stereos, DVD players, cable modems, and wireless devices, you may even find that half of your home electricity consumption can be saved.

Standby power consumption accounts for roughly 8% of residential electricity demand [International Energy Agency, 2001]. In the UK and France, the average standby power is about 0.75 kWh/d per household. For further reading on standby-power policies, see http://www.iea.org/textbase/subjectqueries/standby.asp.

I did an experiment at home, switching off all the gadgets that I normally left on, and I found that my total electricity consumption was halved. I've cemented this saving in place by making a habit of reading my meters every week, so as to check that the electricity-sucking vampires have been banished. If this magic trick could be repeated in all homes and all workplaces, we could obviously make substantial savings. So a bunch of us in Cambridge are putting together a website devoted to making regular meter-reading fun and informative. The website aims to help people carry out similar experiments to mine, make sense of the resulting numbers, and get a warm fuzzy feeling from using less.

I do hope that this sort of smart-metering activity will make a difference. In the future Cartoon Britain of 2050, however, I've assumed that all the electricity savings are cancelled out by the miracle of growth. Growth is one of the tenets of our society: people are going to be wealthier, and thus able to play with more gadgets. The demand for ever-more-superlative computer games forces computers' power consumption to increase. Last decade's computers used to be thought pretty neat, but now they are found useless, and must be replaced by faster hotter machines.

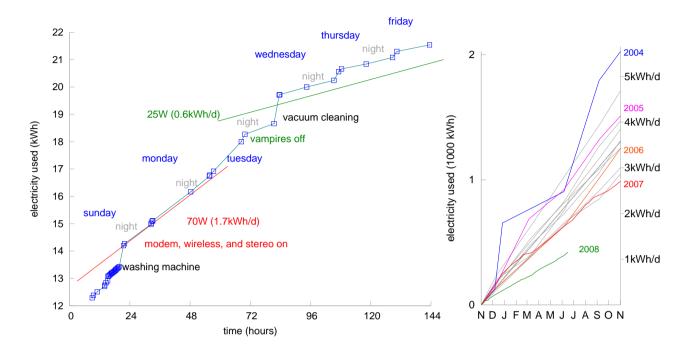


Figure 22.1. Left: One week of detailed meter readings in my house. This was a week when I was away at work most of each day, so both days and nights were almost devoid of useful activity. On the Tuesday I switched off my vampires: two stereos, a DVD player, a cable modem, and a wireless router; and an answering machine. The red line shows the trend of 'nobody-at-home' consumption before, and the green line shows the 'nobody-at-home' consumption after this change. Consumption fell by 1.2 kWh per day.

Right: My domestic cumulative electricity consumption, in kWh, each year from 1993 to 2008. The grey lines are years up to 2003. The coloured lines show the years 2004 onwards. The scale on the right shows the average rate of energy consumption, in kWh per day. The vampire experiment took place on 2nd October 2007. The combination of vampire-banishment with energy-saving-lightbulb installation reduced my electricity consumption from 4 kWh/d to 2 kWh/d.

23 Sustainable fossil fuels?

It is an inescapable reality that fossil fuels will continue to be an important part of the energy mix for decades to come.

UK government spokesperson, April 2008

Our present happy progressive condition is a thing of limited duration.

William Stanley Jevons, 1865

We've explored in the last three chapters the main technologies and lifestyle changes for reducing power consumption. We found that we could halve the power consumption of transport (and de-fossilize it) by switching to electric vehicles. We found that we could reduce the power consumption of heating even more by insulating all buildings better and using electric heat pumps instead of fossil fuels. So yes, we can reduce consumption. But still, matching even this reduced consumption with power from Britain's own renewables (figure 18.8) looks very challenging. It's time to discuss non-renewable options for power production.

Take the known reserves of fossil fuels, 1600Gt of coal, say. Share them equally between six billion people, and burn them "sustainably," such that they're all gone in 1000 years. (This is my arbitrary definition of "sustainable.") 1600 Gt of coal shared between 6 billion people is 270 tons each; and a ton of coal delivers 8000 kWh of a chemical energy. So the power delivered would be 6 kWh per day per person. A standard coal power station would turn this into electricity with an efficiency of about 37% – that means about 2.2 kWh(e) per day per person. If we care about the climate, however, then presumably we would not use a standard power station. Rather, we would go for "clean coal," also known as "coal with carbon capture and storage" – an as-yet scarcely-implemented technology that sucks most of the carbon dioxide out of the chimney-flue gases and then shoves it down a hole in the ground. Cleaning up power station emissions in this way has a significant energy cost – it would reduce the delivered electricity by about 25%. So a "sustainable" use of known coal reserves would deliver only about 1.6 kWh(e) per day per person.

We can compare this "sustainable" coal-burning rate $-1.6\,\mathrm{Gt}$ per year - with the current global rate of coal consumption: 6.3 Gt per year, and rising.

What about the UK alone? Britain is estimated to have 7 Gt of coal left. OK, if we share 7 Gt between 60 million people, we get 100 tons per person. If we want a 1000-year solution, that's this corresponds to 2.5 kWh per day per person. In a power station performing carbon capture and storage, this sustainable approach to UK coal would yield 0.7 kWh(e) per day per person.





Figure 23.1. Coal being delivered to Kingsnorth power station (capacity 1940 MW) in 2005. Photos by Ian Boyle www.simplonpc.co.uk.

Coal: 6 kWh/d

Figure 23.2. "Sustainable fossil fuels."

Clean coal is only a stop-gap.

If we do develop "clean coal" technology in order to reduce greenhouse gas emissions, we must be careful, while patting ourselves on the back, to do the accounting honestly. The coal-burning process releases greenhouse gases not only at the power station but also at the coal mine. Coal-mining tends to release methane, carbon monoxide, and carbon dioxide, both directly from the coal seams as they are exposed, and subsequently from discarded shales and mudstones which contain carbon, some of which oxidizes when exposed to air. There's a similar accounting problem with natural gas: if 5% of the natural gas leaks out along the journey from hole in the ground to power station, then this accidental methane pollution is equivalent (in greenhouse effect) to a 40% boost in the carbon dioxide released at the power station.

When's the end of business as usual?

The economist Jevons did a simple calculation in 1865. People were discussing how long British coal would last. They tended to answer this question by dividing the estimated coal remaining by their rate of coal consumption, and thus getting answers like "1000 years." But, Jevons said, consumption is *not* constant. It's been doubling every 20 years, and "progress" would have it continue to do so. So "reserves divided by consumption-rate" gives the wrong answer.

Instead, Jevons extrapolated the exponentially-growing consumption, calculating the time by which the total amount consumed would exceed the estimated reserves. This was a much shorter time. Jevons was not assuming that consumption would actually continue to grow at the same rate; rather he was making the point that growth was not sustainable. His calculation estimated for his British readership the inevitable limits to their growth, and the short time remaining before those limits would become evident. Jevons made the bold prediction that the end of British "progress" would come within 100 years of 1865. Jevons was right. British coal production peaked in 1910, and by 1965 Britain was no longer a world superpower.

Let's repeat his calculation for the world as a whole. In 2006, the coal consumption rate was 6.3 Gt per year. Comparing this with reserves of 1600 Gt of coal, people often say "there's 250 years of coal left". But if we assume business as usual implies a growing consumption, we get a different answer. If the growth rate of coal consumption were to continue at 2% per year (which gives a reasonable fit to the data from 1930 to 2000), then all the coal would be gone in 2096. If the growth rate is 3.4% per year (the growth rate over the last decade), the end of business-as-usual is guaranteed to be before 2072. Not 250 years, but 60!

If Jevons were here today, I am sure he would firmly predict that unless we steer ourselves on a course different from business as usual, there will,

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

by 2050 or 2060, be an end to our happy progressive condition.

The greatest shortcoming of the human race is our inability to understand the exponential function.

Albert Bartlett



Notes and further reading

page no.

- 167 1000 years my arbitrary definition of "sustainable." As justification for this sort of choice, Hansen et al (2007) equate "more than 500 years" with "forever."
 - ton of coal equivalent = 29.3 GJ = 8000 kWh of chemical energy, not electricity. This figure also neglects energy costs of mining, transport, and carbon sequestration.
 - UK coal. In December 2005, the reserves and resources at existing mines were estimated to be 350 million tons.
 In November 2005, potential opencast reserves were estimated to be 620 million tons; and the underground coal gasification potential was estimated to be at least 7 billion tons. [yebuk8]
 Further reading about underground coal gasification potential: [e2m9n]
 World Energy Council [yhxf8b] survey of energy resources.
- Coal-mining tends to release greenhouse gases. According to Owen Jordan (New Scientist magazine, issue 2652, 19 April 2008, page 16), the upstream greenhouse gas emissions from open-cast coal mining might be at least two times bigger, and possibly ten times bigger, than the emissions at the power station.
 - If 5% of the natural gas leaks, it's equivalent to a 40% boost in carbon dioxide. Accidental methane pollution has nearly eight times as big a global-warming effect as the CO₂ pollution that would arise from burning the methane; eight times, not the standard "23 times," because "23 times" is the warming ratio between equal masses of methane and CO₂. each ton of CH₄ turns into 2.75 tons of CO₂ if burned; if it leaks, it's equivalent to 23 tons of CO₂. And 23/2.75 is 8.4, which is near enough eight.

24 Nuclear?

We made the mistake of lumping nuclear energy in with nuclear weapons, as if all things nuclear were evil. I think that's as big a mistake as if you lumped nuclear medicine in with nuclear weapons.

Patrick Moore,

former Director of Greenpeace International

I am rewriting this chapter; experts advise me that the "Red Book" estimates of mineral reserves that I've used here are an underestimate of what humanity will be able to extract, because they don't account for exploration. So my "mined uranium" and "mined thorium" numbers are likely to need bumping up. And lithium too.

Nuclear power comes in two flavours: nuclear *fission* is the flavour that we know how to use in power stations, fission currently using uranium, an exceptionally heavy element, as its fuel. Nuclear *fusion* is the flavour that we don't yet know how to implement in power stations; it would use light elements, especially hydrogen, as its fuel. Fission reactions split up heavy nuclei into medium-sized nuclei, releasing energy. Fusion reactions fuse light nuclei into medium-sized nuclei, releasing energy.

"Sustainable" power from nuclear fission

Figure 24.1 shows how much electricity was generated globally by nuclear power in 2007.

Could nuclear power be "sustainable"? Leaving aside for a moment the usual questions about safety and waste-disposal, a key question is whether humanity could live for generations on fission. How great are the worldwide supplies of uranium, and of thorium? Do we have only a few decades' worth of uranium, or do we have enough for millennia?

To estimate a "sustainable" power from uranium, I took the total recoverable uranium in the ground and in sea-water, divided it fairly between 6 billion humans, and asked "how fast can we use this if it has to last 1000 years?" I'll be the first to admit this is an arbitrary definition of "sustainable"! But I think the results are interesting anyway.

Almost all the recoverable uranium is in the oceans, not in the ground: seawater contains 3.3 mg of uranium per m³ of water, which adds up to 4.5 billion tons worldwide. The uranium ore in the ground that's extractable at prices below \$130 per ton of uranium is about one thousandth of this. If prices went above \$130 per ton, phosphate deposits that contain uranium at low concentrations would become economic to mine. Recovery of uranium from phosphates is perfectly possible, and was done in America and Belgium before 1998. For the estimate of mined uranium, I'll add both the conventional uranium ore and the phosphates, to give a

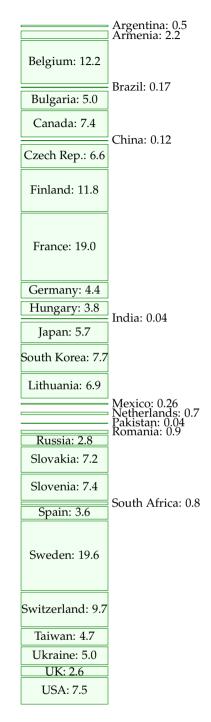


Figure 24.1. Electricity generated from nuclear power in 2007, in kWh per day per person, in each of the countries with nuclear power.

tho	usand tons	percentage
	uranium	of world total
Australia	1143	24%
Kazakhstan	816	17%
Canada	444	9%
USA	342	7%
South Africa	340	7%
Namibia	282	6%
Brazil	279	6%
Russian Federation	173	4%
Uzbekistan	116	2%
World total (in the ground)	4743	
Phosphate deposits	22 000	
Seawater	4 500 000	

Table 24.2. Known recoverable resources of uranium. The top part of the table shows the "reasonable assured resources" and "inferred resources," at cost less than \$130 per kg of uranium, as of 1 Jan 2005. These are the estimated resources in areas where exploration has taken place.

total resource of 27 000 tons of uranium (table 24.2). I called the uranium in the ocean "recoverable" but this is a bit inaccurate – most ocean waters are quite inaccessible, and the ocean conveyor belt rolls round only once every thousand years or so; and no-one has yet demonstrated uranium-extraction from seawater on an industrial scale. So we'll make separate estimates for two cases: first using only mined uranium, and second using ocean uranium too.

We'll also consider two ways to use uranium in a reactor: (a) the widely-used *once-through method* gets energy only from the ²³⁵U, which makes up just 0.7% of uranium, and discards the remaining ²³⁸U; (b) *fast breeder reactors*, which are more expensive to build, convert the ²³⁸U to fissionable plutonium-239 and obtain 60 times as much energy from the uranium.

Once-through reactors, using uranium from the ground

A once-through **one-gigawatt** nuclear power station uses **162 tons per year of uranium**. Or, to put it in human-sized units, **one gram of natural uranium** yields **44 kWh** of electricity. So the known mineable resources of uranium, shared between 6 billion people, would last for 1000 years if we produced nuclear power at a rate of 0.55 kWh per day per person. This is the output of just 136 nuclear power stations, and half of today's nuclear power production. It's very possible this is an underestimate, since, as there is not yet a uranium shortage, there is no incentive for exploration and little uranium exploration has been undertaken since the 1980s; so maybe more mineable uranium will be discovered. Indeed, one paper

published in 1980 estimated that the low-grade uranium resource is more than one thousand times greater than the 22 million tons we just assumed.

Could our current once-through use of mined uranium be sustainable? It's hard to say, since there is such uncertainty about the result of future exploration. Certainly at today's rate of consumption, once-through reactors could keep going for hundreds of years. But if we wanted to crank up nuclear power forty-fold worldwide, in order to get off fossil fuels and to allow standards of living to rise, we might worry that once-through reactors are not a sustainable technology.

Fast breeder reactors, using uranium from the ground

Uranium can be used sixty times more efficiently in fast breeder reactors, which burn up all the uranium – both the ²³⁸U and the ²³⁵U. (The oncethrough reactors burn only the ²³⁵U.) As long as we don't chuck away the spent fuel that is spat out by once-through reactors, this source of depleted uranium could be used too, so uranium that is put in once-through reactors need not be wasted. If we used all the mineable uranium in sixty-times-more-efficient fast breeder reactors, the power would be 33 kWh per day per person. Attitudes to fast breeder reactors range from "this is a dangerous failed experimental technology whereof one should not speak" to "we can and should start building breeder reactors right away." I am not competent to comment on the risks of breeder technology, and I don't want to mix ethical assertions with factual assertions. My aim is just to help understand the numbers. The one ethical position I wish to push here is "we should have a plan that adds up."

Once-through, using uranium from the oceans

The oceans' uranium, if completely extracted, corresponds to

```
4.5 billion tons per planet 162 tons uranium per GW year 28 million GW years per planet.
```

How fast could uranium be extracted from the oceans? The oceans circulate slowly: half of the water is in the Pacific, and deep Pacific waters circulate to the surface on the great ocean conveyor only every 1600 years. Let's imagine that 10% of the uranium is extracted over such a 1600-year period. That's an extraction rate of 280 000 tons per year. In once-through reactors, this would deliver power at a rate of

```
2.8 \text{ million GW years} / 1600 \text{ years} = 1750 \text{ GW},
```

which, shared between 6 billion people, is 7 kWh per day per person. (There's currently 369 GW of nuclear reactors, so this figure corresponds to a four-fold increase in nuclear power over today's levels.) I conclude that ocean extraction of uranium turns today's once-through reactors into

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

173

a "sustainable" option – assuming that the uranium reactors can cover the energy cost of the ocean extraction process.

Fast breeder reactors, using uranium from the oceans

If fast reactors are sixty times more efficient, the same extraction of ocean uranium could deliver 420 kWh per day per person. At last, a sustainable figure that beats current consumption! – but only with the joint help of two technologies that are respectively scarcely-developed and unfashionable: ocean extraction of uranium, and fast breeder reactors.

Using uranium from rivers

The uranium in the oceans is being topped up by rivers, which deliver uranium at a rate of 32 000 tons per year. If 10% of this influx were captured, it would provide enough fuel for 20 GW of once-through reactors, or 1200 GW of fast breeder reactors. The fast breeder reactors would deliver 5 kWh per day per person.

All these numbers are summarized in figure 24.3.

What about costs?

As usual in this book, my main calculations have paid little attention to economics. However, since the potential contribution of ocean-uraniumbased power is one of the biggest in our "sustainable" production list, it seems appropriate to discuss whether this uranium-power figure is at all economically plausible.

Japanese researchers have found a technique for extracting uranium from seawater at a cost of \$100-300 per kilogram of uranium, in comparison with a current cost of about \$20/kg for uranium from ore. Because uranium contains so much more energy per ton than traditional fuels, this five-fold or fifteen-fold increase in the cost of uranium would have little effect on the cost of nuclear power: nuclear power's price is dominated by the cost of construction and decommissioning, not by the cost of the fuel. Even a price of \$300/kg would increase the cost of nuclear energy by only about 0.3 p per kWh.

The expense of uranium extraction could be reduced by combining it with another use of sea water – for example, cooling.

We're not home yet: does the Japanese technique scale up? What is the energy cost of processing all the seawater? In the Japanese experiment, three cages full of adsorbent uranium-attracting material weighing 350 kg collected "more than 1 kg of yellow cake in 240 days;" this figure corresponds to about 1.6 kg per year. The cages had a cross-sectional area of $48 \,\mathrm{m}^2$. To power a once-through 1 GW nuclear power station, we need 160 000 kg per year, which is 100 000 times more. If we simply scaled up the

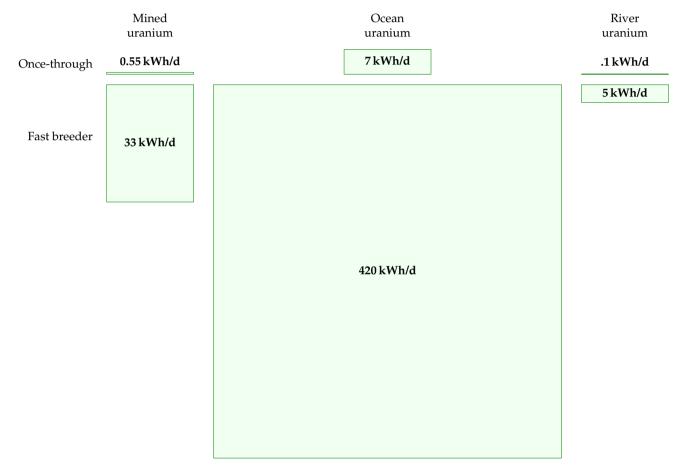


Figure 24.3. "Sustainable" power from uranium. For comparison, world nuclear power production today is 1.2 kWh/d per person. British nuclear power production was 4 kWh/d per person and is declining.

Japanese technique, which accumulated uranium passively from the sea, a power of 1 GW would thus need cages having a collecting area of 4.8 km² and containing a weight of 350 000 tons of adsorbent material – more than the weight of the steel in the reactor itself. To put these large numbers in human terms, if uranium were delivering, say, 22 kWh per day per person, each 1GW reactor would be shared between one million people, each of whom needs 0.16 kg of uranium per year. So each person would require one tenth of the Japanese experimental facility, with a weight of 35 kg per person, and an area of 5 m² per person. The proposal that such uraniumextraction facilities should be created is thus similar in scale to proposals such as 'every person should have 10 m² of solar panels' and 'every person should have a one-ton car and a dedicated parking place for it'. A large investment, yes, but not absurdly off scale. And that was the calculation for once-through reactors. For fast breeder reactors, sixty times less uranium is required, so the mass per person of the uranium collector would be $1/2 \,\mathrm{kg}$.

Thorium

Thorium is a radioactive element similar to uranium. Formerly used to make gas mantles, it is about three times as abundant in the earth's crust as uranium. Soil commonly contains around 6 parts per million of thorium, and some minerals contain 12% thorium oxide. Sea water contains little thorium, because thorium oxide is insoluble. Thorium can be completely used up in simple reactors without fast neutrons (in contrast to standard uranium reactors which use only 0.7% of natural uranium). Thorium is used in nuclear reactors in India. If uranium ore runs low, thorium will probably become the dominant nuclear fuel.

Thorium reactors deliver 3.6×10^9 kWh of heat per ton of thorium, which implies a 1 GW reactor requires about 6 tons of thorium per year, assuming its generators are 40% efficient. Worldwide thorium resources are estimated to total about 6 million tons, four times more than the known reserves shown in table 24.4. As with the uranium resources, it seems plausible that these thorium resources are an underestimate, since thorium prospecting is not highly valued today. If we assume, as with uranium, that these resources are used up over 1000 years and shared equally among six billion people, we find that the 'sustainable' power thus generated is $4 \, \text{kWh/d}$ per person.

An alternative nuclear reactor for thorium, the "energy amplifier" or "accelerator-driven system" proposed by Nobel prizewinner Carlo Rubbia and his colleagues would, they estimated, convert 6 million tons of thorium to 15 000 TWy of energy, or 60 kWh/d/person over 1000 years. Assuming conversion to electricity at 40% efficiency, this would deliver 24 kWh/d/person for 1000 years. And the waste from the energy amplifier would be much less radioactive too. They argue that, in due course,

Country Reserves (thousand tons)		
Turkey	380	
Australia	300	
India	290	
Norway	170	
USA	160	
Canada	100	
South Africa	35	
Brazil	16	
Other countries	s 95	
World total	1 580	

Table 24.4. Known world thorium resources in monazite (economically extractable).

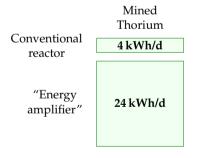


Figure 24.5. Thorium options

many times more thorium would be economically extractable than the current 6 million tons. If their suggestion – 300 times more – is correct, then thorium and the energy amplifier could offer $120\,\mathrm{kWh/d}$ per person for $60\,000$ years.

Land use

Let's imagine that Britain decides it is serious about getting off fossil fuels, and creates a lot of new nuclear reactors, even though this may not be "sustainable." If we build enough reactors to make possible a significant decarbonization of transport and heating, can we fit the required nuclear reactors into Britain? Let's discuss, for example, 22 kWh per day per person – equivalent to 55 GW (roughly the same as France's nuclear power), which could be delivered by 55 nuclear power stations, each occupying one square kilometre. That's about 0.02% of the area of the country. (Wind farms delivering the same average power would require 500 times as much land: 10% of the country.) If they were placed in pairs around the coast (length about 3000 km, at 5 km resolution), then there'd be two every 100 km. Thus while the area required is modest, the fraction of coastline gobbled by these power stations would be about 2% (two kilometres in every hundred). (There are already 17 nuclear power station sites in the UK.)

Economics of cleanup

Hodgson [1999] quotes 0.54p/kWh as the cost of decommissioning. The nuclear decommissioning authority has an annual budget of £2 billion for the next 25 years. The nuclear industry sold everyone in the UK 4kWh/d for about 25 years, so the nuclear decommissioning authority's cost is 2.3p/kWh. That's a hefty subsidy – though not, it must be said, as hefty as the subsidy currently given to offshore wind (7p/kWh).

So decommissioning past nuclear work is costly. But decommissioning in future should be cheaper as we get more experienced? Discuss Dan Kammen's paper on the unpredictability of nuclear costs.

TBC.

Safety

The safety of nuclear operations in Britain remains a concern. The THORP reprocessing facility at Sellafield, built in 1994 at a cost of £1.8 billion, had a growing leak from a broken pipe from August 2004 to April 2005. Over eight months, the leak let 85 thousand litres of uranium-rich fluid flow into a sump which was equipped with safety systems that were designed to detect immediately any leak of as little as 15 litres. But the leak went undetected because

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

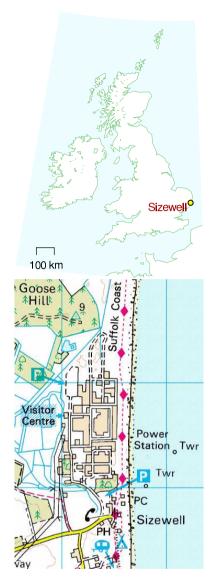


Figure 24.6. Sizewell power station has a capacity of about 1 GW, and occupies less than 1 km². The blue grid's spacing is 1 km. © Crown copyright; Ordnance Survey.

Nuclear?

the operators hadn't completed the checks that ensured the safety systems were working; and the operators were in the habit of ignoring safety alarms anyway.

The safety system came with belt and braces. Independent of the failed safety alarms, routine safety-measurements of fluids in the sump should have detected the abnormal presence of uranium within one month of the start of the leak; but the operators often didn't bother taking these routine measurements, because they felt too busy; and when they *did* take measurements that detected the abnormal presence of uranium in the sump (on 28 August 2004, 26 November 2004, and 24 February 2005), no action was taken.

By April 2005, 22 tons of uranium had leaked, but still none of the leak-detection systems detected the leak. The leak was finally detected by accountancy, when the bean-counters noticed that they were getting 10% less uranium out than their clients claimed they'd put in! Thank goodness this private company had a profit motive, hey? The criticism of the Chief Inspector of Nuclear Installations was withering: "The Plant was operated in a culture that seemed to allow instruments to operate in alarm mode rather than questioning the alarm and rectifying the relevant fault."

If we let private companies build new reactors, how can we ensure that higher safety standards are adhered to? I don't know.

At the same time, we must not let ourselves be swept off our feet in horror at the danger of nuclear power. Nuclear power is not infinitely dangerous. It's just dangerous, much as coal mines, petrol repositories, fossil-fuel burning and wind turbines are dangerous. Even if we have no guarantee against nuclear accidents in the future, I think the right way to assess nuclear is to compare it objectively with other sources of power.

When quantifying the public risks of different power sources, we need a new unit. I'll go with "deaths per GWy (gigawatt-year)." Let me try to convey what it would mean if a power source had a death rate of 1 death per GWy. One gigawatt-year is the energy produced by a 1GW power station, if it operates flat-out for one year. Britain's electricity consumption is roughly 45 GW, or, if you like, 45 gigawatt-years per year. So if we got our electricity from a source with a death rate of 1 death per GWy, that would mean the electricity supply system was killing 45 Brits per year. For comparison, 3000 people die per year on Britain's roads. So, if you are *not* campaigning for the abolition of roads, you may deduce that "1 death per GWy" is a death rate that, while sad, you might be content to live with.

OK, let's discuss the actual death rates of a range of electricity sources. The death rates vary a lot from country to country. In China, for example, the death rate per ton of coal is fifty times that of most nations. I've got these numbers, by the way, from published studies by the Paul Scherrer Institute and by a European Union project called ExternE, which made comprehensive estimates of all the impacts. Figure 24.8 shows their estimates on a logarithmic scale. According to the EU figures, coal, lignite,

and oil are the worst, followed by peat and biomass-power, with death rates above 1 per GWy. Nuclear and wind are the best, with death rates between 0.1 and 0.2 per GWy. Hydroelectricity is the best of all according to the EU study, but comes out worst in the Paul Scherrer Institute's study, because the latter surveyed a different set of countries.

TBC

Useful facts: cumulative output of nuclear power from 1969 to 1996 was 3685 GWy. Chernobyl deaths: direct deaths: 55. Predicted deaths caused by Chernobyl: very difficult to estimate because of the uncertainty of the response of bodies to very small doses; if a linear dose-response is assumed then the total number of deaths in the whole northern hemisphere could be 23 000 fatal cancers (which should perhaps be compared to the natural number of cancers in the same population, namely 650 000 000). Experts express reservations over this estimate of 23 000 deaths; it seems generally to be held that this is an overestimate.

TBC.

Nuclear compared with coal in China: the total health risk (but excluding low probability/high consequence accidents) of the coal-fired energy chain, 57.1 deaths per GWy, is about 12 times of that of the nuclear energy chain, 4.6 deaths per GWy.

Nuclear in the UK: 200 GWy, zero direct public deaths from radiation, how many statistical deaths? One worker died at Chapelcross in 1978. Wind: Caithness Windfarm Information Forum http://www.caithnesswindfarms.co.uk/ list 49 fatalities worldwide from 1970 to 2007 (35 wind industry workers and 14 members of the public). In 2007, Paul Gipe listed 34 deaths total worldwide. In the mid-1990s the mortality rate associated with wind power was 3.5 deaths per GWy. The worldwide mortality rate dropped to 1.3 deaths per GWy by the end of 2000. Source: Paul Gipe http://www.wind-works.org/articles/BreathLife.html.

TBC.

coal: (Mining accidents) plus statistical deaths from dust and radiation exposure. oil: (Nigerian deaths, Piper Alpha)

1970–1990: 380 fatalities associated with North Sea oil and gas.

Hydroelectric power was found (by Paul Gipe?) to have a fatality rate of 0.10 per TWh (0.883 fatalities per GWy) in the period 1969–1996. This includes the Banqiao Dam collapse in 1975 that killed thousands.

People in America living near coal-fired power stations are exposed to higher radiation doses than those living near nuclear power plants [McBride et al., 1978].

Inherently safe nuclear power

TBC.

"Conventional, low-temperature nuclear plants operate at about 32% thermal efficiency. GT-MHR power plants can achieve thermal efficiencies

(c) David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

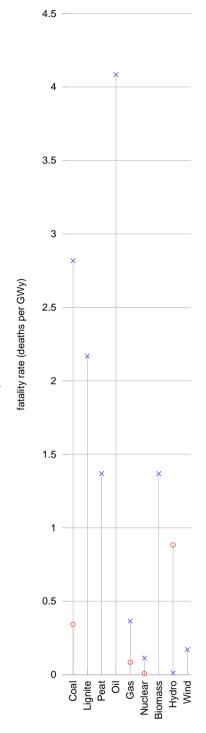


Figure 24.8. Death rates of electricity generation technologies. ×: European Union estimates by the ExternE project. ⊙: Paul Scherrer Institute.

24 — Nuclear? 179

of close to 50% now, and even higher efficiencies in the future." http: //gt-mhr.ga.com/

According to Brendan McNamara, there's a global stock of 1.3 Mt of depleted uranium, which could provide 1.3 million GWv of electricity. That's 5 kWh/d/p for 6 billion people for 1000 years.

Mythconceptions

Two widely-cited defects of nuclear power are construction costs, and waste. Let's examine some aspects of these issues.

Building a nuclear power station requires huge amounts of concrete and steel, materials whose creation involves huge CO₂ pollution.

The steel and concrete in a 1GW nuclear power station have a carbon footprint of roughly 300 000 tCO₂.

Spreading this huge number over a 25-year reactor life we can express this contribution to the carbon intensity in the standard units (gCO₂ per kWh(e)),

carbon intensity
$$\text{associated with construction} = \frac{300 \times 10^9 \, \text{g}}{10^6 \, \text{kW(e)} \times 220\,000 \, \text{h}}$$
$$= 1.4 \, \text{g/kWh(e)},$$

which is much smaller than the fossil-fuel benchmark of 400 g CO₂/kWh(e). The IPCC's estimate of the total carbon intensity of nuclear power (including construction, fuel processing, and decommissioning) is below 40 g CO₂/kWh(e) [Sims et al., 2007].

Please don't get me wrong: I'm not trying to be pro-nuclear. I'm just pro-arithmetic.

TBC

How does the volume of nuclear waste from a 1 GW power station compare with the volume of compressed CO₂ that a 'clean coal' power station would produce?

Very nasty, but very very small.

TBC – see nuclearwaste.tex

About one millionth?

Let's compare three things: the above two, and the volume of household waste for landfill that we currently produce, compared with the volume of nuclear waste if we got all our power from nuclear. Or, say $50 \, \text{kWh/d/p}$.

A French citizen's lifetime share of high-level waste has the size of a golfball.

Waste from new nuclear.

"If the UK were to build a fleet of 10 modern reactors of around 1 GW each (such as the AP1000) and operate these for their full design lifetime of 60 years, the additional waste produced would occupy less than 10% of the volume occupied by [nuclear-reactor] wastes already in existence."

Source: BNFL's evidence to House of Commons Environmental Audit Committee.

Express as a volume per person.

Would nuclear waste require cooling? Does 'just leaving it there' actually have an energy cost?

How does the radiation from all the waste from past nuclear fission relate to the natural background radiation? If we took all that radioactive waste and spread it uniformly over the surface of the earth, would the background radiation increase significantly?

The answer will depend on whether you want to imagine taking the new waste immediately when it comes out steaming and fresh from the reactors, or wait ten or twenty or one hundred years. The radiation levels of the waste fall significantly with time. I'll try to work out the answer.

TBC

If we got lots and lots of power from nuclear fission or fusion, wouldn't this contribute to global warming, because of all the extra energy being released into the environment?

That's a fun question. And because we've carefully expressed everything in this book in a single set of units, it's quite easy to answer. First, let's recap the key numbers about global energy balance from p21: the average solar power absorbed by atmosphere, land, and oceans is 238 W/m²; doubling the atmospheric CO₂ concentration would effectively increase the net heating by 4 W/m². This 1.7% increase in heating is believed to be enough to be bad news for climate. So now let's assume that in one hundred years or so, the world population is ten billion, and everyone is living at a European standard of living, using 125 kWh per day. The area of the earth per person would be 51 000 m². Dividing the power per person by the area per person, we find that the extra power contributed by human energy use would be 0.1 W/m². That's one fortieth of the 4 W/m² that we're currently fretting about. So yes, under these assumptions, human power production would *just* show up as a contributor to global climate change.

I heard that nuclear power can't be built at a sufficient rate to make a useful contribution.

The difficulty of building nuclear power fast has been exaggerated with the help of a misleading presentation technique I call "the magic playing field". In this technique, two things appear to be compared, but the basis

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

24 — Nuclear? 181

of the comparison is switched halfway through. The Guardian's environment editor, summarizing a report from the *Oxford Research Group*, says "For nuclear power to make any significant contribution to a reduction in global carbon emissions in the next two generations, the industry would have to construct nearly 3,000 new reactors – or about one a week for 60 years. A civil nuclear construction and supply programme on this scale is a pipe dream, and completely unfeasible. The highest historic rate is 3.4 new reactors a year." 3000 sounds much bigger than 3.4, doesn't it! In this application of "the magic playing field" technique, there is a switch not only of timescale but also of *region*. While the first figure (3,000 new reactors over 60 years) is the number required *for the whole planet*, the second figure (3.4 new reactors per year) is the maximum rate of building by a *single country* (France)!

The Guardian's reporter and the report's original authors should share the blame for this misleading comparison.

A more honest presentation would have kept the comparison on a perplanet basis. France has 59 of the world's 429 operating nuclear reactors, so it's plausible that the highest rate of reactor building for the whole planet was something like ten times France's, that is, 34 new reactors per year. And the required rate (3000 new reactors over 60 years) is 50 new reactors per year. So the assertion that 'civil nuclear construction on this scale is a pipe dream , and completely unfeasible' is poppycock. Yes, it's a big construction rate, but it's in the same ballpark as historical construction rates.

Are you not happy with my bold assertion that the world's maximum historical construction rate must have been about 34 new nuclear reactors per year? No problem. Let's look at the data. Figure 24.9 shows the power of the world's nuclear fleet as a function of time, showing only the power stations still operational in 2007. The rate of new build was biggest in 1984, and had a value of (drum-roll please...) about 30 GW per year – about 30 1-GW reactors. So there!

Some statistics

TBC.

From Jones [1984]: bear in mind that roughly one fifth of all deaths in developed countries are due to cancer. Exposure to radiation increases the risk of cancer by a relatively small amount: for example, about 180 excess cases of lung cancer have been identified among 15 000 uranium miners. Radiation doses are measured in units of sieverts (Sv) or millisieverts (mSv). As a benchmark, the average natural dose from background radiation is 2.4 mSv per year. The International Commission on Radiological Protection estimates that exposure to 1 Sv of radiation (400 times the annual background dose) gives a probability of dying from cancer of about 1%. There is no evidence of any deleterious effects from doses of less

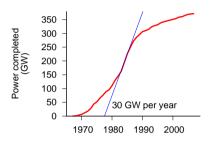


Figure 24.9. Graph of the total nuclear power in the world that was built since 1967 and that is still operational today. The world construction rate peaked at 30 GW of nuclear power per year in 1984.

than **0.01 Sv** (10 mSv, or 1 rem). Based on linear extrapolation, the expected cancer-death-rate would be 1 per 10 000 people – very difficult to measure. Three Mile Island's accident is unlikely to give rise to more than one or two extra cancers in the exposed population, 200 000 of whom would die naturally of cancer. Including the risk of large accidents, Jones [1984] reckons the average risk to members of the public is less than 1 death per GW year.

Accidents

TBC

Chernobyl

6.7 tons of radioactive junk released. 62 direct deaths. 4000 local cases of thyroid cancer of whom just 15 died. An estimate of 9000 total deaths worldwide. (Cancer already causes 25% of deaths in Europe, so an extra 9000 deaths is a small change in this percentage.)

What about nuclear fusion?

We say that we will put the sun into a box. The idea is pretty. The problem is, we don't know how to make the box.

Sébastien Balibar, director of research, CNRS

Fusion power is speculative and experimental. I think it is reckless to assume that the fusion problem *will* be cracked, but I'm happy to estimate how much power fusion could deliver, *if* the problems are cracked.

The two fusion reactions that are considered the most promising are:

The DT reaction, which fuses Deuterium with Tritium (obtained from lithium), making helium; and

The DD reaction, which fuses Deuterium with Deuterium.

ITER is an international project to figure out how to make a steadily-working fusion reactor. The ITER prototype will use the DT reaction. DT is preferred over DD, because the DT reaction yields more energy and because it requires a temperature of "only" one hundred million degrees to get it going, whereas the DD reaction requires 300 million degrees. (The maximum temperature in the sun is 15 million degrees.)

Let's fantasize, and assume that the ITER project is successful. What sustainable power could fusion then deliver? Power stations using the DT reaction, fuelled by lithium, will run out of juice when the lithium runs out. Before that time, hopefully the second installment of the fantasy will have arrived: fusion reactors using deuterium alone.

I'll call these two fantasy energy sources "lithium fusion" and "deuterium fusion," naming them after the principal fuel we'd worry about in each case. Let's now estimate how much energy each of these sources could deliver.

(c) David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

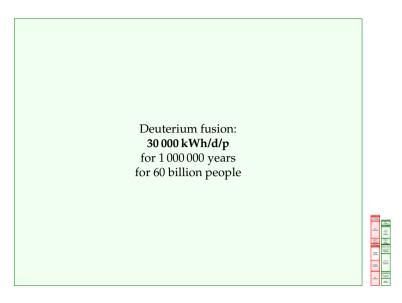


Figure 24.10. Deuterium-based fusion, if it is achievable, offers plentiful sustainable energy for millions of years. This diagram's scale is shrunk ten-fold in each dimension so as to fit fusion's potential contribution on the page. The red and green stacks of part I are shown for scale.

Lithium fusion

World lithium reserves are estimated to be 9.5 million tons in ore deposits. Taking all these reserves and devoting them to fusion over 1000 years, we find that the power delivered would be 10 kWh/d per person.

There's another source for lithium: seawater, where lithium has a concentration of 0.17 ppm. To produce lithium at a rate of $10^8\,\mathrm{kg/y}$ from seawater is estimated to have an energy requirement of 2.5 kWh(e) per gram of lithium. If the fusion reactors give back $2300\,\mathrm{kWh(e)/g}$ lithium, the power thus delivered would be $105\,\mathrm{kWh/d}$ per person (assuming 6 billion people). At this rate, the lithium in the oceans would last over a million years.

Deuterium fusion

Using the DD reaction (page 75 of Hodgson)

TBC

Deuterium is one part in 6000 in water. Deuterium represents approximately 0.015% of hydrogen in water.

From Ongena: $33\,g$ of deuterium per ton of water. 4.6e13 tons of D in oceans. Energy density: 350e15J per ton of D. $100\,000\,kWh$ per g of D. $3200\,kWh$ per litre of ordinary water.

Volume of oceans = 1.37 billion km³, which is 0.23 km³ each.

At 300 kWh per person per day, and 6 billion people, fusion would last 1 billion years (figure 24).

TBC

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

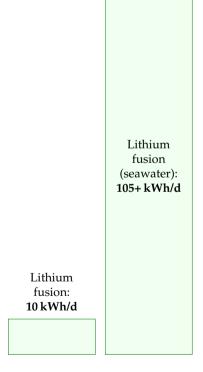


Figure 24.11. Lithium-based fusion, if used fairly and "sustainably," could match our current levels of consumption. Mined lithium would deliver 10 kWh/d per person for 1000 years; lithium extracted from seawater could deliver 105 kWh/d per person for a million years.

Notes

Budget for fusion research and development in the UK: £65M per year. (Total UKAEA turnover: £378M/y.)

(cf. UK renewable R&D budget, £12M/y.)

(What is the UK's contribution to the ITER project? And to IFMIF? Perhaps these contributions are made via the EU?)

Euratom R&D. The total budget for Euratom FP7 in the period 2007-2011 is €2.75 billion and allocated as follows: Fusion energy research: €1,947 million. Nuclear fission and radiation protection: €287 million.

Nuclear activities at the JRC: €517 million.

What is UK share of FP7? Total EU budget is €129b. UK's contribution is 11%.

So of the current €2b European budget (over 5 years) for fusion energy research, Britain is effectively paying €0.22b over 5 years, or €44M per year.

A reader writes: "The most promising looking fusion project appears to be the IECF approach. While not yet 'proven', it appears to offer the shortest implementation time. You can find a lot of background on it here: http://www.askmar.com/Fusion.html"

Notes and further reading

page no.

- 170 Figure 24.1. Source: World Nuclear Association [5qntkb]. The total capacity of operable nuclear reactors is 372 GW(e), using 65 thousand tons of uranium per year. The USA has 99 GW, France 63.5 GW, Japan 47.6 GW, Russia 22 GW, Germany 20 GW, South Korea 17.5 GW, Ukraine 13 GW, Canada 12.6 GW, and UK 11 GW. In 2007 these reactors generated 2608 TWh of electricity, which is an average of 300 GW, or 1.2 kWh per day per person.
- 171 Fast breeder reactors obtain sixty times as much energy from the uranium. Source: http://www.world-nuclear.org/info/inf98.html. Japan currently leads the development of fast breeder reactors.
 - A once-through one-gigawatt nuclear power station uses 162 tons per year of uranium. Source: http://www.world-nuclear.org/info/inf03.html.
 A 1 GW(e) station with a thermal efficiency of 33% running at a load factor of 83% has the following upstream footprint: mining 16 600 tons of 1%-uranium ore; milling 191 t of uranium oxide (containing 162 t of natural uranium); enrichment and fuel fabrication 22.4 t of uranium oxide (containing 20 t of enriched uranium). The enrichment requires 115 000 SWU; see p108 for the energy cost of SWU (separative work units).
- 172 it's been estimated that the low-grade uranium resource is more than one thousand times greater than the 22 million tons we just assumed. Deffeyes and MacGregor [1980] estimate that the resource of uranium in concentrations of 30 parts per million or more is 3×10^{10} tons. (The average ore
- (c) David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

grade processed in South Africa in 1985 and 1990 was 150 ppm. Phosphates typically average 100 ppm.)

Here's what the World Nuclear Association said on the topic of uranium reserves in June 2008. http://www.world-nuclear.org/info/inf75.html "From time to time concerns are raised that the known resources might be insufficient when judged as a multiple of present rate of use. But this is the Limits to Growth fallacy, ... which takes no account of the very limited nature of the knowledge we have at any time of what is actually in the Earth's crust. Our knowledge of geology is such that we can be confident that identified resources of metal minerals are a small fraction of what is there."

"Measured resources of uranium, the amount known to be economically recoverable from orebodies, are ... dependent on the intensity of past exploration effort, and are basically a statement about what is known rather than what is there in the Earth's crust."

"The world's present measured resources of uranium (5.5 Mt) ... are enough to last for over 80 years. This represents a higher level of assured resources than is normal for most minerals. Further exploration and higher prices will certainly, on the basis of present geological knowledge, yield further resources as present ones are used up."

"Normally-functioning metals markets and technology change provide the drivers to ensure that supply at costs affordable to consumers is continuously replenished, both through the discovery of new resources and the re-definition (in economic terms) of known ones."

"On the basis of analogies with other metal minerals, a doubling of price from present levels could be expected to create about a tenfold increase in measured resources, over time, due both to increased exploration and the reclassification of resources regarding what is economically recoverable." "Of course the resources of the earth are indeed finite, but ... the limits of the supply of resources are so far away that the truism has no practical meaning."

"available reserves of 'non-renewable' resources are constantly being renewed, mostly faster than they are used."

"Historic data show that the most commonly used metals have declined in both their costs and real commodity prices over the past century. Such price trends are the most telling evidence of lack of scarcity."

"Economically rational players will only invest in finding these new reserves when they are most confident of gaining a return from them, which usually requires positive price messages caused by undersupply trends. If the economic system is working correctly and maximizing capital efficiency, there should never be more than a few decades of any resource commodity in reserves at any point in time."

(Exploration has a cost; exploring for uranium, for example, has had a cost of \$1–\$1.50 per kg of uranium (\$3.4/MJ), which is 2% of the spot price of \$78/kgU; in contrast, the finding costs of crude oil have averaged around \$6/barrel (\$1050/MJ) (12% of the spot price) over at least the past three decades.)

"Unlike the metals which have been in demand for centuries, society has barely begun to utilize uranium. There has been only one cycle of exploration-discovery-production, driven in large part by late 1970s price peaks."

"It is premature to speak about long-term uranium scarcity when the entire nuclear industry is so young that only one cycle of resource replenishment has been required."

Further reading: Herring [2004], Price and Blaise [2002], Cohen [1983]. The IPCC, citing the OECD, project that at the 2004 utilization levels, the uranium in conventional resources and phosphates would last 670 years in once-through reactors, 20 000 years in fast reactors with plutonium recycling, and 160 000 years in fast reactors recycling uranium and all actinides [Sims et al., 2007].

Japanese researchers have found a technique for extracting uranium from seawater. The price estimate of \$100 per kg is from Seko et al. [2003] and [y3wnzr]; the estimate of \$300 per kg is from [OECD Nuclear Energy Agency, 2006, p.130].

The uranium extraction technique involves dunking tissue in the ocean for a couple of months; the tissue is made of polymer fibres that are made sticky by irradiating them before they are dunked; the sticky fibres collect uranium to the tune of 2g of uranium per kilogram of fibre.

- The expense of uranium extraction could be reduced by combining it with another use of sea water – for example, cooling. The idea of a nuclearpowered island producing hydrogen was floated by C. Marchetti. Breeder reactors would be cooled by sea water and would extract uranium from the cooling water at a rate of 600 t uranium per 500 000 Mt of sea water.
- 175 Thorium reactors deliver 3.6 × 10⁹ kWh of heat per ton of thorium. Source: http://www.world-nuclear.org/info/inf62.html. There remains scope for advancement in thorium reactors, so this figure could be bumped up in the future.
 - An alternative nuclear reactor for Thorium, the "energy amplifier"... See Rubbia et al. [1995], http://web.ift.uib.no/~lillestol/Energy_Web/EA.html, [32t5zt].
 See also [2qr3yr], [ynk54y].
 - World thorium resources in monazite. source: US Geological Survey, Mineral Commodity Summaries, January 1999. [y17tkm] Quoted in UIC Nuclear Issues Briefing Paper #67 November 2004.
 "Other ore minerals with higher thorium contents, such as thorite, would be more likely sources if demand significantly increased."
 [yju4a4] omits the figure for Turkey, which is found here. [yeyr7z]
- 176 The nuclear industry sold everyone in the UK 4 kWh/d for about 25 years. The total generated to 2006 was about 2200 TWh. Source: Stephen Salter's Energy Review for the Scottish National Party.
 - The nuclear decommissioning authority has an annual budget of £2 billion. In fact, this cleanup budget seems to rise and rise. The latest figure for the total cost of decommissioning is £73 billion. http://news.bbc.co.uk/1/hi/uk/7215688.stm
- © David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

177 The criticism of the Chief Inspector of Nuclear Installations was withering... [Weightman, 2007].

179 The steel and concrete in a 1 GW nuclear power station have a carbon footprint of roughly 300 000 t CO₂. How much concrete and steel are in a 1 GW nuclear power station? The Nuclear Energy Institute say 520 000 cubic meters of concrete and 67 000 tons of steel. [2k8y7o]

How much CO_2 is produced when making $520\,000$ cubic meters of concrete? Take the density of concrete $(2300\,\mathrm{kg/m^3})$, the CO_2 to make cement $(0.8\,\mathrm{kg\,CO_2/kg}$ cement), the cement in concrete (10% from cement.org). (A life-cycle analysis gives 43– $240\,\mathrm{kg}$ CO_2 per ton of concrete, depending on the type of concrete, with $100\,\mathrm{kg}$ per ton of concrete as a median figure http://www.sustainableconcrete.org.uk/main.asp?page=210.) This makes a figure of around $100\,000\,\mathrm{t\,CO_2}$ for one nuclear plant.

How much CO_2 is produced in making 67 000 tons of steel? Blue Scope Steel (http://csereport2005.bluescopesteel.com/) claim they put out 14.5 million tons of CO_2 equivalent gases in 2004/2005 to produce 5.72 million tons of steel product, which suggests around 2.5 tons of CO_2 per ton of steel.

Azom.com materials suggests around 2 tons of CO_2 per ton of steel, and Tata Steel claim ([36y2e4]) between 1.2 and 1.9 tons of CO_2 per ton of steel, depending on the process.

Taking the largest figure, 3 tons of CO_2 for a ton of steel, we have another 200 000 tons of CO_2 from the steel to make a 1 GW nuclear power station. Summing the steel and concrete figures: $300\,000\,t\,CO_2$ is associated with the construction of a 1 GW nuke.

182 Chernobyl, TBC

Nature April 20 2006 page 984 Review articles.

6.7 tons of radioactive junk released. 62 direct deaths. 4000 local cases of thyroid cancer of whom just 15 died. An estimate of 9000 total deaths worldwide, 4000 of whom are among a set of 600 000 people who were exposed to a significant amount of radiation, giving 4/600 chance of death; and the other 5000 are among a set of 6.8M others further away, exposed to 7 millisieverts, which is comparable to total natural yearly dose. Cancer already causes 25% of deaths in Europe.

- 183 World lithium reserves are estimated as 9.5 million tons. The main lithium sources are found in Bolivia (56.6%), Chile (31.4%) and the United States (4.3%). www.dnpm.gov.br
 - There's another source for lithium: seawater... Several extraction techniques have been investigated [Steinberg and Dang, 1975, Tsuruta, 2005, Chitrakar et al., 2001]. The extractable amount in seawater is roughly 10 000 times greater.

TBC

The energy density of natural lithium is about 7500 kWh per gram [Ongena and Van Oost, 2006]. There's considerable variation among the estimates of how efficiently fusion reactors would turn this into electricity, ranging from 310 kWh(e)/g [Eckhartt, 1995] to 3400 kWh(e)/g of natural



Figure 24.12. Steel plant in Tenaris Siderca, Argentina.

lithium [Steinberg and Dang, 1975]. I've assumed 2300 kWh(e)/g, based on this widely quoted summary figure: "A 1GW fusion plant will use about 100 kg of deuterium and 3 tons of natural lithium per year, generating about 7 billion kWh." [69vt8r] [60by22] [63121p]

Further reading: Rogner [2000], Williams [2000]. Uranium Information Center – http://www.uic.com.au/.

Additional material for reprocessing...

TBC

http://www.world-nuclear.org/co2&nfc.htm

Energy cost of full uranium cycle, broken down in detail here: [wnchw] Enrichment accounts for almost half of the cost of nuclear fuel and about 5% of the total cost of the electricity generated. [t2948]

This page [ygwh8a] gives a life-cycle analysis for nuclear. This seems to be the source for the 'Ireland' document. For nuclear power, enrichment is clearly the key energy input where the older diffusion technology is used - it comprises more than half the lifetime total. However, with centrifuge technology it is far less significant than plant construction. Includes a range of mining costs for different ore concentrations.

Bottom line: $1\,\text{GW}$ PWR power plant. where mine's ore is 0.234% U (energy cost of mining $165\,\text{GJ/t}\,\text{U}_3\text{O}_8$, or $195\,\text{GJ/t}\,\text{U}$, an output of $7\,\text{TWh/y}$ ($76\,000\,\text{TJ}$) required mining and milling input of $39\,\text{TJ}$ per y (for $230\,\text{t}$ per yr of $U_3\text{O}_8$). Larger was the enrichment cost. Overall the energy ratio (assuming a 40-year life) is $58\,\text{if}$ modern centrifuge enrichment used. (i.e., 1.7% of the output is the input, respectively). Construction and decommissioning are about half of the energy cost. But if the ore were 0.01% U then the mining bill goes up to $924\,\text{TJ/y}$ and the bottom line changes from 1.7% to 2.9%.

This same document also quotes other study (Forsmark 3GW) giving nuclear an input/output of 1.35%, and CO₂ emissions of 3.1 g/kWh.

Nuclear CO₂: 40 kg/MWh in the USA. In France, where nuclear power is used for the electricity for diffusion enrichment, 20 kg/MWh. The life cycle CO₂ emission coefficient for nuclear power, on the basis of centrifuge enrichment, is 2.7% of that for coal-fired generation.

British Energy's Torness nuclear power plant in 2002 was 5 g/kWh.

This same document also rebuts Storm van Leeuwen and Smith.

eg true modern Energy cost of mining: in-situ leaching (ISL) which can be more efficient than traditional mining methods in terms of both cost and energy use, e.g. about 19 kWh/kgU in Australia and 33 kWh/kgU in Kazakhstan.

Forsmark has three reactors totalling 3 GW(e). energy cost of construction and decom: The life cycle assessment for Vattenfall's Forsmark-3 nuclear plant showed that 4.1 PJ was required for construction and decommissioning, on basis of 40 year plant life.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

24 — Nuclear? 189

	g CO ₂ /kWh			
	Japan	Sweden	Finland	WEC summary
coal	975	980	894	820-1040
gas thermal	608	1170	_	_
gas combined cycle	519	450	472	400-500
solar photovoltaic	53	50	95	13-105
wind	29	5.5	14	7–22
nuclear	22	6	10-26	4-40
hydroelectric	11	3	_	5–90

Table 24.13. Greenhouse gas emissions associated with different electricity generation technologies. Sources: Japan, Sweden Finland from Kivisto (2000) in http://www.world-nuclear.org/info/inf11.htm; World Energy Council [2004]; Sims et al. [2007].

(Which is about 950 MWh per MW if F-3 was 1.2GW)

Energy cost in Finland for making nuclear power: (construction only?) 650 MWh/MW capacity. Incidentally, this gives a useful money to energy ratio for construction project. The Finnish reactors cost Olkiluoto 3 project cost has been estimated by TVO at around €3 Billion. Zaleski [2005][321ouu] – for a 1600 MW reactor and waste depository. [shrln]

Site for unbiased information on waste repositories.

Thorium: in the 1970s, 1GW reactor used 10 t Th per year.

Waste

Waste we already have to deal with. The projected volume of "higher activity wastes" up to 2120, following decommissioning of existing nuclear facilities, is $478\,000\,\mathrm{m}^3$. Of this volume, 2% (about $10\,000\,\mathrm{m}^3$) would be the high level waste ($1290\,\mathrm{m}^3$) and spent fuel ($8150\,\mathrm{m}^3$) that together contain 92% of the activity.

Building another 10 nuclear reactors (10 GW) would add another 31 900 m³ of spent fuel to this total. Committee on Radioactive Waste Management [2006]

The ten new nuclear reactors currently discussed for Britain would generate $31\,900\,\mathrm{m}^3$ of spent fuel.

That's the same volume as ten swimming pools.

From Bruno Comby: "One gram of uranium yields about as much energy as a metric ton of coal or oil; it's the famous 'factor of a million' effect. Nuclear wastes are accordingly about a million times smaller than fossil fuel wastes. Most fossil fuel waste is gases that go up the smokestack, which although unseen isn't without effect, causing global warming, acid rain, smog and other atmospheric pollution.

"The volume of nuclear waste produced is very small. In his or her whole lifetime, the volume of highly active vitrified waste produced by a typical French citizen is only the volume of a golf ball."

25 Living on other countries' renewables?

Our comparisons of consumption with conceivable sustainable production showed that land-based wind power can't match the energy consumption enjoyed by most Europeans. We would have come to a different conclusion, however, if the population density of the United Kingdom were ten times smaller.

Most of the resources for living sustainably are related to land area: if you want to use solar panels, you need land to put them on; if you want to grow crops, you need land again. Jared Diamond, in his book *Collapse*, observes that, while many factors contribute to the collapses of civilizations, a common feature of all collapses is that the human population density became too great.

So let's look at land areas per person.

Population densities

Figure 25.2 shows the areas of various regions versus their populations. Diagonal lines on this diagram are lines of constant population density. Bangladesh, on the rightmost diagonal, has a population density of 1000 per square kilometre; India, England, the Netherlands, and Japan have population densities one third that: about 350 per km². Many European countries have about 100 per km². At the other extreme, Canada, Australia, and Libya have population densities of about 3 people per km². The central diagonal line marks the population density of the world: 43 people per square kilometre. America is an average country from this point of view: the 48 contiguous states of the USA have the same population density as the world. Regions that are notably rich in area, and whose population density is below the average, include Russia, Canada, Latin America, Sudan, Algeria, and Saudi Arabia.

Of these large, area-rich countries, some that are close to Britain, and with whom Britain might therefore wish to be friendly, are Kazakhstan, Libya, Saudi Arabia, Algeria, and Sudan.

A technology that adds up

Whether the Mediterranean becomes an area of cooperation or confrontation in the 21st century will be of strategic importance to our common security.

Joschka Fischer, German Foreign Minister, February 2004

We've found that it's hard to get off fossil fuels by living on our own renewables. Nuclear has its problems too. So what else can we do? Well how

Use	area/person (m ²)		
domestic	30		
domestic	gardens	114	
other bui	ildings	18	
road		60	
rail		4	
path		3	
greenspa	ice	2335	
water		69	
other lan	d uses	37	
Total		2670	

Table 25.1. Land uses in England.





Figure 25.3. Andasol – a "100 MW" solar power station under construction in Spain. Excess thermal energy produced during the day will be stored in liquid salt tanks for up to seven hours,a allowing a continuous and stable supply of electric power to the grid. The power station is predicted to produce 350 GWh per year (40 MW). The parabolic troughs occupy 400 hectares, so the power per unit area will be 10 W/m². Upper photo: ABB. Lower photo: IEA

SolarPACES.

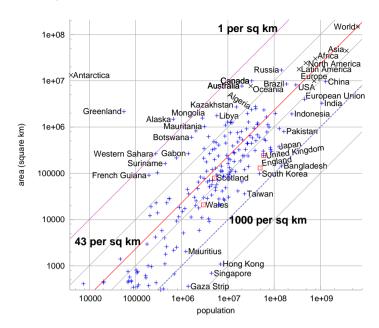


Figure 25.2. Populations and areas of countries and regions of the world. Both scales are logarithmic. Each sloping line identifies a population density; countries with highest population density are towards the lower right, and lower population densities are towards the upper left. These data are provided in tabular form in Chapter L (p368).

about living on someone else's renewables? – not that we have any entitlement to someone else's renewables, of course, but perhaps they might be interested in selling them to us.

"All the world's power could be provided by a square 100 km by 100 km in the Sahara." Is this true? Concentrating solar power in deserts delivers an average power per unit area of roughly $15\,\mathrm{W/m^2}$. So, allowing no space for anything else in such a square, the power delivered would be $150\,\mathrm{GW}$. This is not the same as current world power consumption. It's not even near current world electricity consumption, which is $2000\,\mathrm{GW}$. World power consumption today is $15\,000\,\mathrm{GW}$. So the correct statement about power from the Sahara is that today's consumption could be provided by a $1000\,\mathrm{km}$ by $1000\,\mathrm{km}$ square in the desert, completely filled with concentrating solar power. That's four times the area of the United Kingdom. And if we are interested in living in an equitable world, we should presumably aim to supply more than today's consumption. To supply every person in the world with an average European's power consumption (125 kWh/d), the area required would be two 1000 km by 1000 km squares in the desert, or eight United Kingdoms.

Fortunately, the Sahara is not the only desert, so maybe it's more relevant to chop the world into smaller regions, and ask what area is needed in each region's local desert. So, focussing on Europe, "what area is required in the North Sahara to supply *everyone in Europe and North Africa* with an average European's power consumption? Taking the population of Europe and North Africa to be one billion, the area required drops to 340 000 km², which corresponds to a square **600 km by 600 km**. This area is equal to one Germany, to 1.4 United Kingdoms, or to **16 Waleses**.

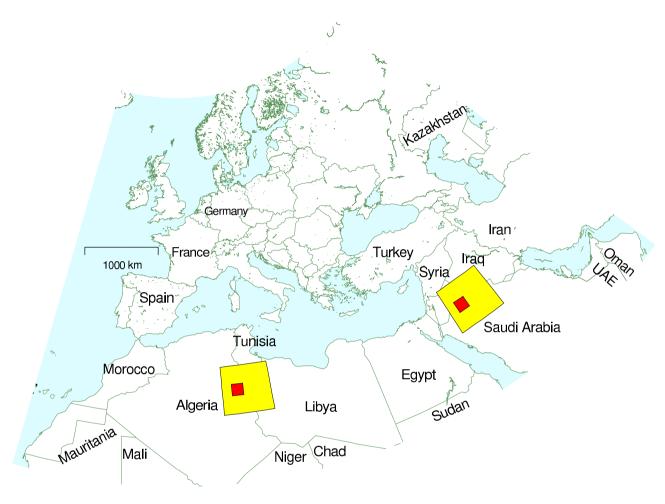


Figure 25.4. The celebrated little square. This map shows a square of size 600 km by 600 km in Africa, and another in Saudi Arabia, Jordan, and Iraq. Concentrating solar power facilities completely filling one such square would provide enough power to give one billion people the average European's consumption of 125 kWh/d. The area of one square is the same as the area of Germany, and 16 times the area of Wales. Within each big square is a smaller 145 km by 145 km square showing the area required in the Sahara – one Wales – to supply all British power consumption.

The UK's share of this 16-Wales area would be one Wales: a 145 km by 145 km square in the Sahara would provide all the UK's current primary energy consumption.

The DESERTEC plan

DESERTEC is a plan to use concentrating solar power and high-voltage direct-current (HVDC) transmission lines. HVDC technology has been in use since 1954 to transmit power both through overhead lines and through submarine cables (such as the interconnector between France and England). It is already used to transmit electricity over 1000-km distances in South Africa, China, America, Canada, Brazil, and Congo. A typical 500 kV line can transmit a power of 2 GW. A pair of HVDC lines in Brazil can transmit 6.3 GW.

The losses in each converter station are about 0.6% of the transmitted power.

Half-baked material

Algeria and Libya have about $2000 \, \text{kWh/m}^2/\text{y}$ of solar irradiance. Say $250 \, \text{W/m}^2$.

The German TREC report projects about 2000 TWh/y electricity from CSP thermal. That's about 5.5 kWh/day per person if shared between 1 billion people.

The TREC plan requires investment of \$75 billion.

Solar-to-electricity efficiency currently 10–15%, projected to be 18% for parabolic troughs.

Land use: $6 \text{ m}^2/(\text{MWh/y})$. Same as 20 W/m^2 . (Is that including the 30% factor below? I guess not.)

Going back to TREC:

According to page 60, about half of the land area of Libya and Algeria and Saudi Arabia would be "suitable." What's the cooling method? Do they use sea water, or do they use cold air collected at night? They assumed they could use 30% of this suitable area and that the efficiency would be 15% (parabolic troughs).

When electricity is produced, the "process heat" is also useable for cooling (how does that work? 'Vapour absorption chillers'), drying, or desalination.

Idea: Express the area required in terms of Londons. $6\,\text{m}^2/(MWh/y)$. $6\,\text{km}^2/(TWh/y)$. Same as $20\,\text{W/m}^2$. $50\,\text{km}^2/GW$.

I guess a London is about $1500\,\mathrm{km^2}$. So each London is $30\,\mathrm{GW}$. But if we assume a density of 30% land use, each London delivers $10\,\mathrm{GW}$. The required $650\,\mathrm{GW}$ (to deliver $16\,\mathrm{kWh/d}$ per person to one billion people) would need $65\,\mathrm{Londons}$.

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com



Figure 25.5. A high-voltage DC power system in China. Photo: ABB.



Figure 25.6. Laying a high-voltage DC link between Finland and Estonia. A pair of these cables transmit a power of 350 MW. Photo: ABB.



Figure 25.7. Stirling dish engine. These beautiful concentrators deliver a power density of $14 \, \text{W/m}^2$ of land. Photo courtesy of Stirling Energy Systems. www.stirlingenergy.com

Country	Economic potential	Coastal potential
	(TWh/y)	(TWh/y)
Morocco	20 000	300
Tunisia	9 200	350
Algeria	169 000	60
Libya	140 000	500
Egypt	74 000	500
Portugal	140	7
Spain	1 300	70
Turkey	130	12
Israel	3 100	1
Jordan	6400	0
Syria	10 000	0
Iraq	29 000	60
Qatar	800	320
UAE	2000	540
Kuwait	1 500	130
Oman	19 000	500
Saudi Arabia	125 000	2 000
Yemen	5 100	390
Total	620 000	6 000
	(70 000 GW)	(650 GW)

Table 25.8. Solar power potential in countries around and near to Europe. The "economic potential" is the power available in suitable places where the direct normal irradiance is more than $2000 \, \text{kWh/m}^2/\text{y}$. The "coastal potential" is the power available within 20 m (vertical) of sea level; such power is especially promising because of the potential combination with desalination. For comparison, the total power required to give 125 kWh per day to 1 billion people is 46 000 TWh/y (5 200 GW). 6000 TWh/y (650 GW) is 16 kWh per day per person for 1 billion people.



Figure 25.9 tries to convey the scale of these Londons relative to the hot spots. Each circular blob represents an area of 1500 km². Figure 25.10 shows detail from figure 25.9.

European countries by themselves have economic potential for $1730 \, \text{TWh/y}$ of solar energy. They (TREC) reckon the total renewable energy potential of Europe is $40\,000 \, \text{PJ/y}$ (62% of present primary energy consumption).

They (TREC) could get 2900 TWh/y electricity (which is the same as the total energy consumption of the UK) and 160 billion $\rm m^3$ of water per year using $\rm 120 \times 120 \, km^2$. That electricity generation is $\rm 23 \, W/m^2$.

Trans-Mediterranean Interconnection for Concentrating Solar Power

by German Aerospace Center (DLR) Institute of Technical Thermodynamics Section Systems Analysis and Technology Assessment

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

Figure 25.9. Each circular blob represents an area of 1500 km², which, if one-third-filled with solar power facilities, would generate 10 GW on average. 65 such blobs would provide one billion people with 16 kWh/d per person. To give a sense of the scale of these blobs I've dropped a few in Britain too.

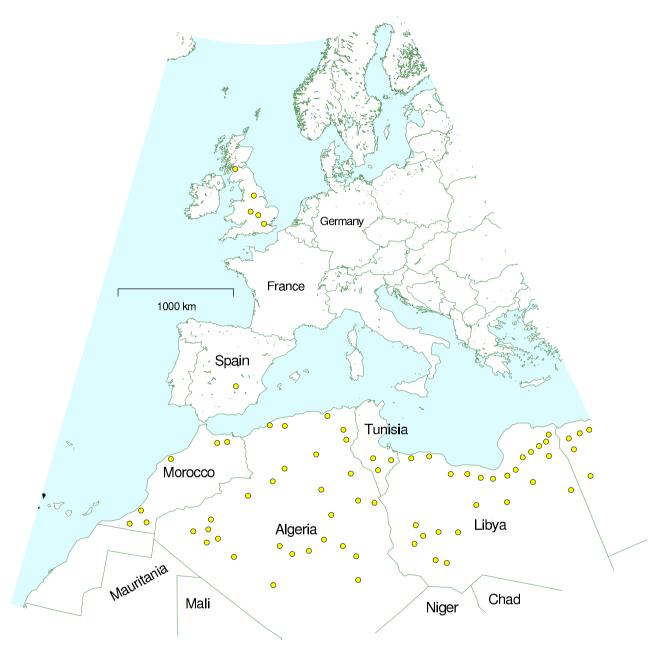


Figure 25.10. Detail from figure 25.9.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

France to GB interconnector transmits 10 000 GWh/y.

High voltage losses are 15% per $1000\,\mathrm{km}$ for $380\,\mathrm{kV}$ lines and 8% per $1000\,\mathrm{km}$ for $750\,\mathrm{kV}$. Each transformer station loses 0.25%. HVDC: High Voltage Direct Current transmission. $600\,\mathrm{kV}$ or $800\,\mathrm{kV}$. To transfer $50\,\mathrm{GW}$, need a tract of land $100{-}150\,\mathrm{m}$ wide for pylons. (Lower than HVAC ($800\,\mathrm{kV}$).) DC cables good for long distances: the loss in transport is only about 3% per $1000\,\mathrm{kilometres}$.

Queries: energy cost of making mirrors? – any scarce resources required? Associated CO₂ emissions?

Key points: can design a CSP thermal reactor to be driven by other fuels e.g., fossil fuels or biomass, so as to increase power availability.

Today, a thermal solar power station produces electricity at a cost between 0.14 and 0.18 \in per kilowatt-hour (kWh). If a capacity of 100 GW were created, the cost would fall to 0.04–0.06 \in per kWh, according to Franz Trieb.

Concentrating photovoltaics

An alternative to concentrating thermal solar power in deserts is large-scale concentrating photovoltaic systems. This means plopping a high-quality electricity-producing solar cell at the focus of cheap lenses or mirrors. Faiman et al. [2007] say that "solar, in its concentrator photovoltaics variety, can be completely cost-competitive with fossil fuel [in desert states such as California, Arizona, New Mexico, and Texas] without the need for any kind of subsidy."

According to manufacturers Amonix, this form of concentrating solar power would have an average power density of $18 \,\mathrm{W/m^2}$.

Another way to get a feel for required hardware is to personalize. One of the $25\,\mathrm{kWp}$ collectors shown in the photograph generates on average about $138\,\mathrm{kWh}$ per day; the American lifestyle currently uses $300\,\mathrm{kWh}$ per day per person. So to get America off fossil fuels using solar power, we need two of these $15\,\mathrm{m} \times 15\,\mathrm{m}$ collectors per person.

I'm confused! In chapter 6, you said that the best photovoltaic panels deliver $20 \, \text{W/m}^2$ on average, in a place with British sunniness. Presumably in the desert the same panels would deliver $40 \, \text{W/m}^2$. So how come the concentrating solar power stations deliver only $15-20 \, \text{W/m}^2$? Surely concentrating power should be even better than plain flat panels?

Good question. The short answer is no. Concentrating solar power does not achieve a better power per unit land area than flat panels. The concentrating contraption has to track the sun, otherwise the sunlight won't be focussed right; once you start packing land with sun-tracking contraptions, you have to leave gaps between them; lots of sunlight falls through the gaps and is lost. The reason that people nevertheless make concentrating solar power systems is that, today, flat photovoltaic panels are insanely



Figure 25.11. A 25 kWp concentrator photovoltaic collector produced by Californian company Amonix. Its 225 m² aperture contains 5760 Fresnel lenses with optical concentration ×260, each of which illuminates a 25%-efficient silicon cell. One such collector, in an appropriate desert location, generates 140 kWh per day – enough to cover the energy consumption of half an American. Photograph by David Faiman.

expensive, and concentrating systems are cheaper. The concentrating people's goal is not to make systems with big power per unit land area. Land area is cheap (they assume). The goal is to deliver big power per dollar. I keep on getting letters from people saying that I must have got the numbers for concentrating solar power wrong. Please save your stamp. Find any organization making a real concentrating solar product. Find out the real production they deliver, in kWh per year, and divide it by the land area required. No, not the area of the concentrating contraption's schnozz, you muppet, the *land area*. Work out the number in watts per square metre. Then send me a letter saying "Oh. You were right."

But if flat panels have bigger power density, why don't you describe covering the Sahara desert with them?

Because I am trying to discuss practical options for large-scale sustainable power production for Europe and North Africa by 2050. My guess is that by 2050, mirrors will still be cheaper than photovoltaic panels, so concentrating solar power is the technology on which we should focus.

What about getting power from Iceland, where hydroelectricity and geothermal energy are so plentiful?

Indeed, Iceland already effectively exports energy by powering industries that make energy-intensive products. Iceland produces nearly one ton of Aluminium per citizen per year, for example! But I would be surprised if Iceland's power production could be scaled up enough to make sizeable electricity exports to Britain. As a benchmark, let's compare with the England–France Interconnector, which can deliver up to 2 GW across the channel. That maximum power is equivalent 0.8 kWh/d per person, roughly 5% of British average electricity consumption. Iceland's average electricity production is 1.1 GW. So to create a link sending power equal to the capacity of the French interconnector, Iceland would have to *triple* its electricity production. To provide us with 4 kWh/d per person (roughly what Britain now gets from its own nuclear power stations), Iceland's electricity production would have to increase *ten-fold*.

Notes and further reading

Numbers for a $10\,\mathrm{GW}$ line. Loss of an $800\,\mathrm{kV}$ AC line is about 8% per $1000\,\mathrm{km}$; of a $750\,\mathrm{kV}$ DC line, about 4% per $1000\,\mathrm{km}$.

For transmission of $10\,\mathrm{GW}$, if the distance is larger than $600\,\mathrm{km}$, HVDC is the cheapest choice of transmission line. page no.

- 190 Figure L.1 shows the areas of various regions versus their populations. These data are presented in tables on p368.
- 191 Concentrating solar power in deserts delivers an average power per unit area of roughly $15 \, \text{W/m}^2$.
- © David J.C. MacKay.~Draft~2.9.0.~August 28, 2008 www.withouthotair.com

My sources for this number are two companies doing concentrating solar power for deserts.

www.stirlingenergy.com say one of their dishes with a $25\,\mathrm{kW}$ Stirling engine at its focus can generate $60\,000\,\mathrm{kWh/y}$ in a favourable desert location. They could be packed at a concentration of 8 per acre. That's an average power of $14\,\mathrm{W/m^2}$. They say that solar dish stirling makes the best use of land area, in terms of energy delivered.

http://www.ausra.com/ use flat mirrors to heat water to 285 °C and drive a steam turbine. The heated pressurized water can be stored in deep metal-lined caverns to allow power generation at night. Power density for a '240 MW(e)' plant proposed for Australia [Mills and Lièvre, 2004]: the designers claim that 3.5 km² of mirrors would deliver 1.2 TWh(e); that's 38 W/m² of mirror. To find the power per unit land area, we need to allow for the gaps between the mirrors. Ausra say they need a 153 km by 153 km square in the desert to supply all US electric power Mills and Morgan [2008]. Total US electricity is 3600 TWh/y, so they are claiming a power density of 18 W/m². This technology goes by the name compact linear fresnel reflector Mills and Morrison [2000], Mills et al. [2004], Mills and Morgan [2008]. Incidentally, rather than "concentrating solar power," the company Ausra prefers to use the term solar thermal electricity (STE); they emphasize the benefits of thermal storage, in contrast to concentrating photovoltaics, which don't come with a natural storage option.

Trieb and Knies [2004], who are strong proponents of concentrating solar power, project that the alternative CSP technologies would have the following powers per unit land area: parabolic troughs, 14– $19\,\text{W/m}^2$; linear fresnel collector, 19– $28\,\text{W/m}^2$; tower with heliostats, 9– $14\,\text{W/m}^2$; stirling dish, 9– $14\,\text{W/m}^2$.

There are three European demonstration plants for concentrating solar power. PS10, a tower near Seville; Andasol – using parabolic troughs; and Solartres, a tower using molten salt for heat storage. Solartres will occupy 142 ha and is expected to produce 96.4 GWh per year; that's a power density of $8\,\mathrm{W/m^2}$. The Andasol parabolic-trough system shown in figure 25.3 is predicted to deliver $10\,\mathrm{W/m^2}$. Andasol and Solartres will both use some natural gas in normal operation.

Solucar: This "11 MW" solar tower has 624 mirrors, each $121 \,\mathrm{m}^2$. The mirrors concentrate sunlight to a radiation density of up to $650 \,\mathrm{kW/m^2}$. The receiver receives a peak power of 55 MW. The power station can store 20 MWh of thermal energy, allowing it to keep going for 50 minutes of cloudiness. It was expected to generate 24.2 GWh of electricity per year, and it occupies 55 hectares. That's an average power density of $5 \,\mathrm{W/m^2}$.

193 HVDC is already used to transmit electricity over 1000-km distances in South Africa, China, America, Canada, Brazil, and Congo. Source: Asplund [2004].

Further reading on HVDC: Carlsson [2002]. From Bahrman and Johnson [2007], savings in line construction: roughly 30% relative to AC. Number of cables needed is roughly 40% of AC, and there are network stability benefits. Losses for different AC and DC transmission alternatives for a hypothetical 750-mile (1200 km), 3,000-MW transmission system: Best

(lowest loss) DC option: 3.43% (103 MW). Cost: \$2b. Best AC option: 4.62% (139 MW). \$4.8b.

Losses on a 3500 km-long HVDC line, including conversion from AC to DC and back, would be about 15% [Trieb and Knies, 2004, van Voorthuysen, 2008].

197 According to Amonix, concentrating photovoltaics would have an average power density of 18 W/m². http://www.amonix.com/ Their assumptions: the lens transmits 85% of the light; 32% cell efficiency; 25% collector efficiency; 10% further loss due to shading. Aperture/land ratio of 1/3. Normal direct irradiance 2222 kWh/m²/year. They expect each kWp to deliver 2000 kWh/kWp/y. A VLSPV plant of 1 GW peak capacity would occupy 12 km² of land and deliver 2000 GWh per year. That's 18 W/m².

eSolar esolar.com make medium-scale power stations: a $33\,\mathrm{MW}$ (peak) power unit on a 64 hectare site. That's $51\,\mathrm{W/m^2}$ peak, so I'd guess that in a typical desert location they would deliver about one quarter of that: $13\,\mathrm{W/m^2}$.

Further reading: European Commission [2007]. German Aerospace Center (DLR) Institute of Technical Thermodynamics Section Systems Analysis and Technology Assessment [2006]. http://www.solarmillennium.de/

For high voltage DC, the loss in transport is only about 3% per 1000 kilometres. I got this from DESERTEC. I'd like another source, as the ABB website didn't confirm this clearly.

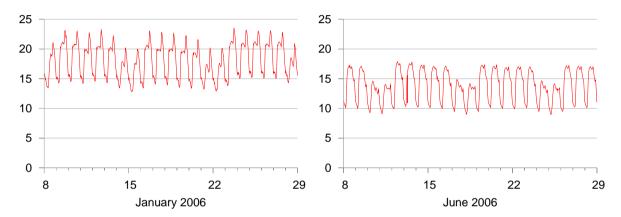


Figure 25.12. Two engineers assembling an eSolar concentrating power station.

26 Fluctuations and storage

The wind, as a direct motive power, is wholly inapplicable to a system of machine labour, for during a calm season the whole business of the country would be thrown out of gear. Before the era of steamengines, windmills were tried for draining mines; but though they were powerful machines, they were very irregular, so that in a long tract of calm weather the mines were drowned, and all the workmen thrown idle.

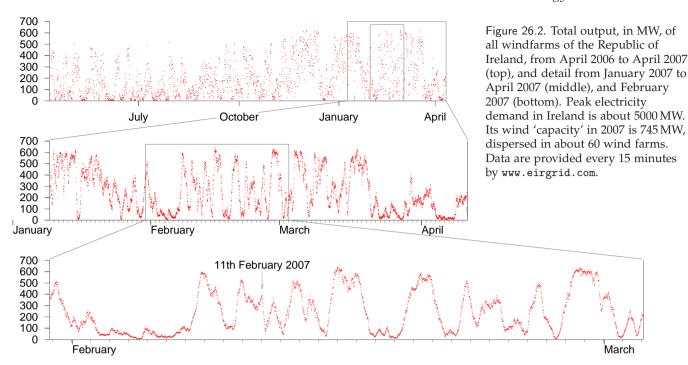
William Stanley Jevons, 1865



If we kick fossil fuels and go all-out for renewables, or all-out for nuclear, or a mixture of the two, we have a problem. Most of the big renewables are not turn-off-and-onable. When the wind blows and the sun comes out, power is there for the taking; but maybe two hours later, it's not available any more. Nuclear power stations are not usually designed to be turn-off-and-onable either. They are usually on all the time, and their delivered power can be turned down and up only on a timescale of hours. This is a problem because, on an electricity network, consumption and production must be exactly equal all the the time. The electricity grid can't store energy. To have an energy plan that adds up, we need something easily turn-off-and-onable. It's commonly assumed that the easily turn-offand-onable something should be a source of power that gets turned off and on to compensate for the fluctuations of supply relative to demand. But another equally effective way to match supply and demand would be to have an easily turn-off-and-onable demand for power – a sink of power that can be turned off and on at the drop of a hat.

Either way, the easily turn-off-and-onable something needs to be a *big* something because electricity demand varies a lot (figure 26.1). The demand sometimes changes significantly on a timescale of a few minutes.

Figure 26.1. Electricity demand in Great Britain (in kWh/d per person) during two winter weeks and two summer weeks of 2006. The peaks in January are at 6pm each day. The five-day working week is evident in summer and winter. (If you'd like to obtain the national demand in GW, remember the top of the scale, 24 kWh/d per person, is the same as 60 GW per UK.)



This chapter is going to discuss how to cope with fluctuations in supply and demand, without using fossil fuels.

How much do renewables fluctuate?

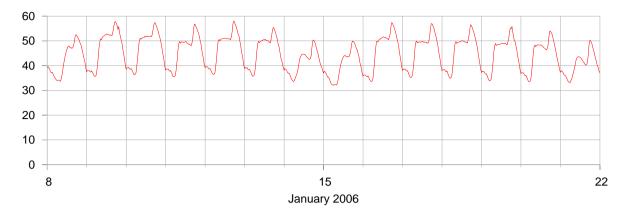
However much we love renewables, we must not kid ourselves about the fact that wind does fluctuate.

The anti-wind lobby say: "Wind power is intermittent and unpredictable, so it can make no contribution to security of supply; if we create lots of wind power, we'll have to maintain lots of fossil-fuel power plant to replace the wind when it drops." Headlines such as "Loss of wind causes Texas power grid emergency" reinforce this view. Supporters of wind energy play down this problem: "Don't worry – *individual* wind farms may be intermittent, but taken together, the *sum* of all wind farms is much less intermittent."

Let's look at real data and try to figure out a balanced viewpoint.

Figure 26.2 shows the summed output of the wind fleet of the Republic of Ireland from April 2006 to April 2007. Clearly wind *is* intermittent, even if we add up lots of turbines covering a whole country. The UK is a bit larger than Ireland, but the same problem holds there too. Between October 2006 and February 2007 there were 17 days when output from Britain's 1632 windmills was less than ten per cent of their capacity. During that period there were five days when output was less than 5% and one day when it was only 2%.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com



Let's quantify the fluctuations in country-wide wind power. The two issues are short-term changes, and long-term lulls. Let's find the fastest short-term change in a month of Irish wind data. On 11th February 2007, the Irish wind power fell steadily from 415 MW at midnight to 79 MW at 4am. That's a slew rate of 84 MW per hour for a country-wide fleet of capacity 745 MW. (By slew rate I mean the rate at which the delivered power fell – the slope of the graph on 11th February.) OK: if we scale British wind power up to a capacity of 33 GW (so that it delivers 10 GW on average), we can expect to have occasional slew rates of

$$84 \,\text{MW/h} \times \frac{33\,000 \,\text{MW}}{745 \,\text{MW}} = 3700 \,\text{MW/h}$$

(assuming Britain is like Ireland). So we need to be able to either power *up* replacements for wind at a rate of 3.7 GW per hour – that's 4 nuclear power stations going from no power to full power every hour, say – *or* we need to be able to suddenly turn *down* our *demand* at a rate of 3.7 GW per hour.

Rather than laughing at this countercultural notion and crucifying the naïve wind huggers, let's have a rummage outside the box and see if these windy demands could in fact be met.

This country-scale rummaging will require us to talk about "gigawatts." Gigawatts are big country-sized units of power. They are to a country what a kilowatt-hour-per-day is to a person: a nice convenient unit. The UK's average electricity consumption is about 40 GW. We can relate this national number to personal consumption: one kWh per day per person is equivalent to 2.5 GW per UK. So if every person uses 16 kWh per day of electricity, then national consumption is 40 GW.

Is a national slew-rate of 4GW per hour completely outside human experience? No. Every morning, as figure M.2 shows, British demand climbs by about 13GW between 6.30am and 8.30am. That's a slew rate of 6.5GW per hour. So our power engineers already cope, every day, with slew

Figure 26.3. Electricity demand in Great Britain (in GW) during two winter weeks of 2006. This is exactly the same data as in the left half of figure 26.1, but in the national unit (GW), instead of the personal unit (kWh/d/person).

rates bigger than 4 GW per hour on the national grid. An extra occasional slew of 4 GW per hour induced by sudden wind variations is no reasonable cause for ditching the idea of country-sized wind farms. It's a problem just like problems that engineers have already solved. We simply need to figure out how to match ever-changing supply and demand in a grid with no fossil fuels. I'm not saying that the wind-slew problem is already solved – just that it is a problem of the same size as other problems known to be solvable.

OK, before we start looking for solutions, we need to quantify wind's other problem: lulls. At the start of February 2007, Ireland had a country-wide lull that lasted five days. This was not an unusual event, as you can see in figure 26.2. Lulls lasting two or three days happen several times a year.

There are two ways to get through lulls. Either we can store up energy somewhere before the lull. Or we need to have a way of reducing demand during the entire lull. (Or a mix of the two.) If we have 33 GW of wind turbines delivering an average power of 10 GW then the amount of energy we must either store up in advance or do without during a five-day lull is

$$10 \,\text{GW} \times (5 \times 24 \,\text{h}) = 1200 \,\text{GWh}.$$

(The gigawatt-hour (GWh) is the cuddly unit of energy for nations. Britain's electricity consumption is roughly 1000 GWh per day.)

To personalize this quantity, an energy store of $1200\,\mathrm{GWh}$ for the nation is equivalent to an energy store of $20\,\mathrm{kWh}$ per person. Such an energy store would allow the nation to go without $10\,\mathrm{GW}$ of electricity for 5 days; or equivalently, every individual to go without $4\,\mathrm{kWh}$ per day of electricity for 5 days.

Coping with lulls and slews

We need to solve two problems – lulls (long periods with small renewable production), and slews (short-term changes in either supply or demand). We've quantified these problems, assuming that Britain had roughly 33 GW of wind power. To cope with lulls, we must effectively store up roughly 1200 GWh of energy (20 kWh per person). The slew rate we must cope with is 6.5 GW per hour (or 0.1 kW per hour per person).

There are two solutions, both of which could scale up to solve these problems. The first solution is a centralized solution, and the second is decentralized. The first solution stores up energy, then copes with fluctuations by turning on and off a *source* powered from the energy store. The second solution works by turning on and off a piece of *demand*.

The first solution is *pumped storage*. The second uses the batteries of the electric vehicles that we discussed in Chapter 20.

Before I describe these solutions, let's discuss a few other ideas for coping with slew.

(c) David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

Other supply-side ways of coping with slew

Some of the renewables are turn-off-and-onable. If we had a lot of renewable power that was easily turn-off-and-onable, all the problems of this chapter would go away. Countries like Norway and Sweden have very large and deep hydroelectric supplies which they can turn on and off. What might the options be in Britain?

First, Britain could have lots of waste incinerators and biomass incinerators – power stations playing the role that is today played by fossil power stations. If these stations were designed to be turn-off-and-onable, there would be cost implications, just as it costs to have extra fossil power stations that are only working part-time: their generators would sometimes be idle and sometimes work twice as hard; and most generators aren't as efficient if you keep turning them up and down, compared with running them at a steady speed. OK, leaving cost to one side, the crucial question is how big a turn-off-and-onable resource we might have. If all municipal waste were incinerated, and an equal amount of agricultural waste were incinerated, then the average power from these sources would be about 3 GW. If we built capacity equal to twice this power, making incinerators capable of delivering 6 GW, thus planning to have them operate only half the time, these would be able to deliver 6 GW throughout periods of high demand, then zero in the wee hours. These power stations could be designed to switch on or off within an hour, thus coping with slew rates of 6GW per hour – but only for a maximum slew range of 6GW! That's a helpful contribution, but not enough slew range in itself, if we are to cope with the fluctuations of 33 GW of wind.

What about hydroelectricity? Britain's hydroelectric stations have an average load factor of 20% so they certainly have the potential to be turned on and off. Furthermore, hydro has the wonderful feature that it can be turned on and off very quickly. Glendoe, a new hydro station with a capacity of 100 MW, will be able to switch from off to on in 30 seconds, for example. That's a slew rate of 12 GW per hour in just one power station! So a sufficiently large fleet of hydro power stations should be able to cope with the slew introduced by enormous windfarms. However, the capacity of the British hydro fleet is *not* currently big enough to make much contribution to our slew problem (assuming we want to cope with the rapid loss of say 10 or 33 GW of wind power). The total capacity of traditional hydroelectric stations in Britain is only about 1.5 GW.

So simply switching on and off other renewable power sources is not going to work in Britain. We need other solutions.

Pumped storage

Pumped storage systems use cheap electricity to shove water from a downhill lake to an uphill lake; then regenerate electricity when it's valuable,



Figure 26.5. Llyn Stwlan, the upper reservoir of the Ffestiniog pumped storage scheme in north Wales. Energy stored: 1.3 GWh. Photo by Adrian Pingstone.

station	power (MW)	head (m)	volume (million m ³)	energy stored (GWh)
Ffestiniog	360	320/295	1.7	1.3
Cruachan	400	365/334	11.3	10
Foyers	300	178/172	13.6	6.3
Dinorwig	1800	542/494	6.7	9.1

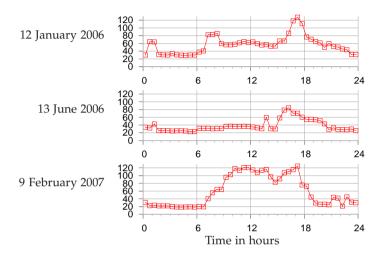


Table 26.4. Pumped storage facilities in Britain. The maximum energy storable in today's pumped storage systems in 30 GWh.

Figure 26.6. How pumped storage pays for itself. Electricity prices, in £ per MWh, on three days in 2006 and 2007.

using turbines just like the ones in hydroelectric power stations.

Britain currently has four pumped storage facilities, able to store 30 GWh between them (table 26.4). They are typically used to store excess electricity at night, then return it during the day, especially at moments of peak demand – a profitable business, as figure 26.6 shows. The Dinorwig power station – an astonishing cathedral inside a mountain in Snowdonia – also plays an insurance role: it has enough capacity to restart the national grid in the event of a major failure. Dinorwig can switch on, from 0 to 1.3 GW power, in 12 seconds.

Dinorwig is the Queen of the four facilities. Let's review her vital statistics. The total energy that can be stored in Dinorwig is about 9 GWh. Its upper lake is about 500 m above the lower, and the working volume of 7 million m³ flows at a maximum rate of 390 m³/s, allowing power delivery at 1.7 GW for 5 hours. The efficiency of this storage system is 75%.

If all four pumped storage stations are switched on simultaneously, they can produce a power of 2.8 GW. They can switch on extremely fast, coping with any slew rate that demand fluctuations or wind fluctuations could come up with. However the capacity of 2.8 GW is not enough to replace 10 GW or 33 GW of wind power if it suddenly went missing. Nor is the total energy stored (30 GWh) anywhere near the 1200 GWh we are interested in storing in order to make it through a big lull. Could pumped

Way	Ways to store 100 GWh					
drop from upper lake	working volume required (million m ³)	example size of lake area depth				
500 m	40	$2 \text{km}^2 \times 20 \text{m}$				
$500\mathrm{m}$	40	$4 \mathrm{km^2} \times 10 \mathrm{m}$				
200 m	100	$5\mathrm{km}^2 \times 20\mathrm{m}$				
200 m	100	$10\mathrm{km}^2 \times 10\mathrm{m}$				
$100\mathrm{m}$	200	$10 \mathrm{km}^2 \times 20 \mathrm{m}$				
$100\mathrm{m}$	200	$20 \mathrm{km}^2 \times 10 \mathrm{m}$				

proposed location	power	head	volume	energy stored
	(MW)	(m)	(million m ³)	(GWh)
Bowydd	2400	250	17.7	12.0
Croesor	1350	310	8.0	6.7

storage be ramped up? Can we imagine solving the entire lull problem using pumped storage alone?

Storing 1200 GWh

We are interested in making much bigger storage systems, storing a total of 1200 GWh (about 130 times what Dinorwig stores). And we'd like the capacity to be about 20 GW – about ten times bigger than Dinorwig's. So here is the pumped storage solution: we have to imagine creating roughly 12 new sites, each storing 100 GWh – roughly ten times the energy stored in Dinorwig. The pumping and generating hardware at each site would be the same as Dinorwig's.

Assuming the generators have an efficiency of 90%, table 26 shows a few ways of storing 100 GWh, for a range of height drops. (For the physics behind this table, see the technical chapter, p351.)

Is it plausible that twelve such sites could be found? Certainly we could build several more sites like Dinorwig in Snowdonia alone. Table 26.8 shows two alternative sites near to Ffestiniog where two facilities equal to Dinorwig could have been built. Pumped-storage facilities holding significantly more energy than Dinorwig could probably be built in Scotland by upgrading existing hydroelectric facilities.

Scanning a map of Scotland, one candidate location would use Loch Sloy as its upper lake and Loch Lomond as its lower lake. There is already a small hydroelectric power station linking these lakes. Figure 26.10 shows these lakes and the Dinorwig lakes on the same scale. The height differ-

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

Table 26.7. Pumped storage. Ways to store 100 GWh.

For comparison with column 2, the working volume of Dinorwig is 7 million m³, and the volume of Lake Windermere is 300 million m³. For comparison with column 3, Rutland water has an area of 12.6 km²; Grafham water 7.4 km². Carron valley reservoir is 3.9 km². Loch Lomond's area is 71 km² (it's the largest lake in Great Britain).

Table 26.8. Alternative sites for pumped storage facilities in Snowdonia. At both these sites the lower lake would have been a new artificial reservoir.

1 square mile = $2.6 \times 10^6 \,\text{m}^2 = 2.6 \,\text{km}^2$



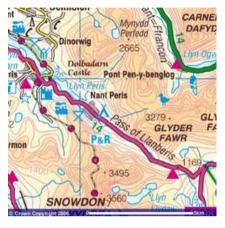




Figure 26.10. Dinorwig, in the Snowdonia National Park, compared with Loch Sloy and Loch Lomond. The upper maps show 10 km by 10 km areas. In the lower maps the blue grid is made of 1 km squares. Images produced from Ordnance Survey's Get-a-map service www.ordnancesurvey.co.uk/getamap. Images reproduced with permission of Ordnance Survey. © Crown Copyright 2006.





Dinorwig is the home of a 9 GWh storage system, using Marchlyn Mawr (615E, 620N) and Llyn Peris (590E, 598N) as its upper and lower reservoirs.

Loch Sloy illustrates the sort of location where a 40 GWh storage system could be created.



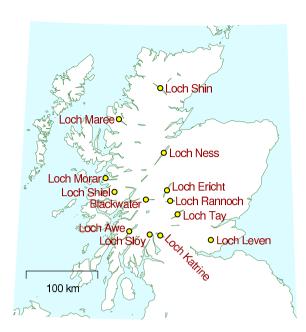


Figure 26.11. Lochs in Scotland with potential for pumped storage.

ence between Loch Sloy and Loch Lomond is about 270 m. Sloy's area is about 1.5 km². If Loch Sloy's height could be pumped up by about 40 m then the energy delivered on releasing that extra water would be about 40 GWh. If there were no compensating flows of water in and out of Loch Lomond, the water level in Loch Lomond would change by 80 cm during a cycle. This is less than the normal range of annual water level variations of Loch Lomond, namely 2 m.

Figure 26 shows fourteen locations in Scotland with potential for pumped storage. If ten of these had the same potential as I just estimated for Loch Sloy, then we could store 400 GWh – one third of the total of 1200 GWh that would compensate for major lulls in wind, assuming 33 GW of wind capacity.

Other storage locations

We could scour the map of Britain for other locations. The best locations would be near to big wind-farms. One idea would be to make a new artifical lake in a hanging valley (across the mouth of which a dam would be built) terminating above the sea, with the sea being used as the lower lake.

Thinking further outside the box, one could imagine getting away from lakes and reservoirs, putting half of the facility in an underground chamber. A possible advantage of using a tidal body of water as one of the reservoirs is the potential for a storage system to boost its efficiency by timing the pumping and generating to coincide – as near as possible – with low tide and high tide respectively.



Figure 26.12. Okinawa pumped-storage power plant, whose lower reservoir is the ocean. Energy stored: 0.2 GWh. Photo by courtesy of J-Power. www.ieahydro.org.

By building more pumped storage systems, I believe we could increase our maximum energy store from 30 GWh to 100 GW or perhaps 400 GWh. Achieving the full 1200 GWh that we were hoping for looks tough, however. Fortunately there is another solution.

Demand management using electric vehicles

To recap our requirements: we'd like to be able to store or do without about 1200 GWh, which is 20 kWh per person; and to cope with swings in supply of up to 33 GW – that's 0.5 kW per person. These numbers are delightfully similar in size to the energy and power requirements of electric cars. The electric cars we saw in Chapter 20 had storage capacities between 9 kWh and 53 kWh. A national fleet of 30 million electric cars would have a capacity similar to 20 kWh per person! Typical battery chargers draw a power of 2 or 3 kW. So simultaneously switching on 30 million battery chargers would create a change in demand of about 60 GW! The average power required to power all the nation's transport, if it were all electric, is roughly 40 or 50 GW. There's therefore a very close match between the increase in the use of electric cars proposed in Chapter 20 and the creation of roughly 33 GW of wind capacity, delivering 10 GW of power on average.

We could have an especially robust solution if the cars' batteries were exchangeable. Imagine popping in to a filling station and slotting in a brace of fresh batteries in exchange for your exhausted batteries. The filling station would be responsible for recharging the batteries; they could do this at the perfect times, turning up and down their chargers so that total supply and demand were always kept in perfect balance. Using exchangeable batteries is an especially robust solution because there would be millions of spare batteries in the filling stations' storerooms. These spare batteries would provide an extra buffer to help us get through wind lulls. Some people say, "Horrors! How could I trust the filling station to look after my batteries for me? What if they gave me a duff one?" Well, you could equally well ask today "What if the filling station gave me petrol laced with water?" Myself, I'd much rather use a vehicle maintained by a professional than by a muppet like me!

Other storage and demand-management ideas

Let's recap our options. We can balance fluctuating demand with fluctuating supply by switching on and off power *generators* (waste incinerators and hydroelectric stations, for example); by *storing* energy somewhere and regenerating it when it's needed; or by switching *demand* on and off.

The most promising of these options, in terms of scale, is switching on and off the power demand of electric-vehicle charging. 30 million cars, with 40 kWh of associated batteries each (some of which might be exchangeable batteries sitting in filling stations) adds up to 1200 GWh. If

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

freight delivery were electrified too then the total storage capacity would be bigger still.

There is thus a beautiful match of wind power and electric vehicles. If we ramp up electric vehicles at the same time as ramping up wind power, roughly 3000 new vehicles for every 3 MW wind turbine, and if we ensure that the charging systems for the vehicles are smart, this synergy would go a long way to solving the wind fluctuations problem. If my prediction about hydrogen vehicles is wrong, and hydrogen vehicles turn out to be the low-energy vehicles of the future, then the wind-and-electric-vehicles match-up that I've just described could of course be replaced by a wind-and-hydrogen match-up. The wind turbines would make electricity; and whenever electricity was plentiful, hydrogen would be produced and stored in tanks, for subsequent use in vehicles or in other applications, such as glass production..

There are a few other energy-storage and demand-management options, which we'll survey now.

The idea of modifying the rate of production of stuff to match the power of a renewable source is not new. Many aluminium production plants are located close to hydroelectric power stations; the more it rains, the more aluminium is produced. Wherever power is used to create stuff that is storable, there's potential for switching that power-demand on and off in a smart way. For example, reverse-osmosis systems (which make pure water from sea-water) are major power consumers in many countries (though not Britain). Another storable product is heat. If, as suggested in Chapter 21, we electrify heating and cooling systems, especially waterheating and air-heating, then there's potential for a lot more easily-turnoff-and-onable power demand to be attached to the grid. Well-insulated buildings hold their heat for many hours, so there's flexibility in the timing of their heating. Moreover, we could include large thermal reservoirs in buildings, and use heat-pumps to pump heat into or out of those reservoirs at times of electricity abundance. Then use a second set of heat pumps to deliver heat or cold from the reservoirs to the place where heating or cooling is wanted.

Controlling electricity demand automatically would be easy. The simplest way of delivering dynamic demand control is to have devices such as fridges and freezers listen to the frequency of the mains. When there is a shortage of power on the grid, the frequency drops below its standard value of 50 Hz; when there is a power excess, the frequency rises above 50 Hz. Fridges can be modified to nudge their internal thermostats up and down just a little in response to the mains frequency, in such a way that, without ever jeopardising the temperature of your butter, they tend to take power at times that help the grid.

Can demand-management alone provide the virtual storage that's needed? How big a sink of power are the nation's fridges? On average, a typical fridge-freezer draws about 18 W, and the number of fridges is probably

about 30 million. So the ability to switch off all the nation's fridges for a few minutes would be equivalent to 540 MW of automatic adjustable power. This is quite a lot of electrical power – more than one percent of the national total – but it's not as big as the sudden increases in demand produced when the people, united in an act of religious observance (such as watching Coronation Street, or watching England play footie against Sweden), simultaneously switch on half a million kettles. Such "TV pick-ups" can produce increases in demand of over 2000 MW. Popular soap operas such as Coronation Street and EastEnders typically generate TV pick-ups of 600–800 MW. So automatically switching off every fridge would *nearly* cover these daily blips of concerted kettle boiling.

In South Africa (where there are frequent electricity shortages), radiocontrolled demand-management systems are being installed in hundreds of thousands of homes, to control electric water heaters and air-conditioning systems.

To provide flexibility on a shorter timescale, many industrial users of electricity are on special contracts that allow the electricity-grid managers to switch off those user's demand at very short notice.

Denmark's solution

Here's how Denmark copes with the intermittency of its wind power. The Danes effectively use other countries' hydroelectric as storage facilities (and pay for this service). Almost all of Denmark's wind power is exported to its European neighbours, some of whom have hydroelectric power, which they can turn down to balance things out. The saved hydroelectric power is then sold back to the Danes (at a higher price) during the next period of low wind and high demand. Overall, Danish wind is contributing useful energy, and the system as a whole has considerable security thanks to the capacity of the hydro system.

Could Britain adopt the Danish solution? We would need direct large-capacity connections to countries with lots of turn-off-and-on-able hydroelectric capacity; or a big connection to a Europe-wide electricity grid.

Norway has 27.5 GW of hydroelectric capacity. Sweden has roughly 16 GW. And Iceland has 1.8 GW. A 1.2 GW high-voltage DC interconnector to Norway was mooted in 2003, but not built. A connection to the Netherlands – the BritNed interconnector, with a capacity of 1 GW – will be built in 2010.

A solution with two grids

Put wind power and other intermittent sources onto a *second* electricity grid, used to power systems that don't require reliable power, such as electric vehicle battery-charging. For over 25 years (since 1982), the Scottish island of Fair Isle (population 70, area 5.6 km²) has had *two* electricity net-

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com



works that distribute power from two wind turbines and, if necessary, a diesel-powered electricity generator. Standard electricity service is provided on one network, and electric heating is delivered by a second set of cables. The electric heating is mainly served by excess electricity from the wind-turbines that would otherwise have had to be dumped. Remote frequency-sensitive programmable relays control individual water heaters and storage heaters in the individual buildings of the community. In fact there's up to six frequency channels per household, so the system emulates seven networks. Fair Isle also successfully trialled a kinetic energy storage system (a flywheel) to store energy during fluctuations of wind strength on a time-scale of 20 seconds.

Electrical vehicles as generators

Vehicle-to-grid power. If 30 million electric vehicles were willing, in times of national electricity shortage, to run their chargers in reverse and put power into the grid, then, at 2 kW per vehicle, we'd have a potential power source of 60 GW – similar to the capacity of all the power stations in the country. Even if only one third of the vehicles were connected and available at one time, they'd still amount to a potential source of 20 GW of power. If each of those vehicles were willing, in emergencies, to share 2 kWh of energy – corresponding to perhaps 20% of its storage capacity – then the total energy provided by the fleet would be 20 GWh – twice as much as the energy in the Dinorwig pumped storage facility.

Other storage technologies

There's a lot of ways of storing energy, and lots of criteria by which storage solutions are judged. Figure ?? shows three of the most important: energy density (how much energy is stored per unit mass of storage system); efficiency (how much energy you get back per unit energy put in); and lifetime (how many cycles of energy storage can be delivered before the system needs refurbishing). Other important criteria are: the maximum rate at which energy can be pumped into or out of the storage system, often expressed as a power per unit mass; the duration for which energy stays stored in the system; and of course the cost of the system.

flamable fuels typically provide around $10\,\mathrm{MJ/kg}$ while batteries yield less than $0.5\,\mathrm{MJ/kg}.$

Flywheels

A flywheel system designed for energy storage in a racing car can store 400 kJ (0.1 kWh) of energy and weighs 24 kg. That's an energy density of 4.6 Whper kg. http://www.flybridsystems.com/F1System.html

PRODUCTION CONSUMPTION
Wind: 4.1
Diesel: 1.8
Heating: 2.5
Other: 2.9

Figure 26.13. Electrical production and consumption on Fair Isle, 1995–96. All numbers are in kWh/d per person. Production exceeds consumption because 0.6 kWh/d per person were dumped.



Figure 26.16. One of the two flywheels at the fusion research facility in Culham, under construction. It weighs 800 t. Spinning at 225 revolutions per minute, it can store 1000 kWh, and its energy density is about 1 Wh per kg. Photo: EFDA-JET. www.jet.efda.org.

fuel	calorific value		
	(kWh/kg)	(MJ/l)	
propane	13.8	25.4	
petrol	13.0	34.7	
diesel oil (DERV)	12.7	37.9	
kerosene	12.8	37	
heating oil	12.8	37.3	
ethanol	8.2	23.4	
methanol	5.5	18.0	
bioethanol		21.6	
coal	8.0		
firewood	4.4		
hydrogen	39.0		
natural gas	14.85	0.04	

(a)

Table 26.14. (a) Calorific values (energy densities per unit mass and per unit volume) of some fuels (in kWh per kg and MJ per litre). (b) Energy density of some batteries (in Wh per kg). 1 kWh = 1000 Wh.

battery type	energy density (Wh/kg)	lifetime (cycles)
nickel-cadmium	45-80	1500
NiMH	60-120	300-500
lead-acid	30-50	200-300
lithium-ion	110-160	300-500
lithium-ion-polyme	r 100–130	300-500
reusable alkaline	80	50

(b)

100000 100000 hydrogen Chydrogen fuel cell hydrogen fuel cell propane Energy density (Wh/kg) 10000 10000 petrol ethanol, coal methanol 1000 1000 firewood lithium ion flywheel lithium ion oflywheel alkaline Ni-MHONi-Cd 100 100 lead acid vanadium lead acido air⊙ 10 10 supercapacitor supercapacitor o pumped storage air/oilo pumped storage 1 10 100 1000 10000100000 0 0.2 0.4 0.6 8.0 Cycles Efficiency (a) (b)

Figure 26.15. Some properties of storage systems and fuels. (a) Energy density (on a logarithmic scale) versus lifetime (number of cycles). (b) Energy density versus efficiency. The energy densities don't include the masses of the energy systems' containers, except in the case of "air" (compressed air storage). Taking into account the weight of a cryogenic tank for holding hydrogen, the energy density of hydrogen is reduced to roughly 2400 Wh per kg.

(c) David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

Supercapacitors

Supercapacitors are used for storage of small amounts of electrical energy (up to 1kWh) where many cycles of operation are required, and charging must be completed quickly. For example, supercapacitors are favoured over batteries for regenerative braking in vehicles that do many stops and starts. You can buy supercapacitors with an energy density of 6Wh/kg.

An American company, EEStor, claims to be able to make much better supercapacitors, using barium titanate, with an energy density of 280 Wh/kg.

Vanadium flow batteries

VRB power systems www.vrbpower.com have provided a 12 MWh energy storage system for the Sorne Hill windfarm in Ireland (current capacity "32 MW," increasing to "39 MW"). (VRB stands for vanadium redox battery.) [ktd7a] This storage system is a big "flow battery," a vanadium-based redox regenerative fuel cell, with a couple of tanks full of vanadium in different chemical states. This storage system can smooth the output of its windfarm on a time-scale of minutes, but the longest time for which it could deliver one third of the capacity (during a lull in the wind) is one hour. The same company installed a 1.1 MWh system on Tasmania. It can deliver 200 kW for four hours, 300 kW for 5 minutes and 400 kW for 10 seconds.

A 1.5 MWh vanadium system costing \$480 000 occupies 70 m² with a mass of 107 tonnes. The vanadium redox battery has a life of more than 10 000 cycles. It can be charged at the same rate that it is discharged (in contrast to lead-acid batteries which must be charged 5 times as slowly). [627ced] Its efficiency is 70–75%, round-trip. The volume required is about 1 m³ for 20 kWh using 2-molar vanadium in sulphuric acid. (That's 0.02 kWh/kg or 72 kJ/kg.)

So to store 10 GWh would require $500\,000\,\text{m}^3$ (170 swimming pools) – for example, tanks 2 m high covering a floor area of $500\,\text{m} \times 500\,\text{m}$.

Scaling up the vanadium technology to the scale of pumped storage systems – 10 or 20 GWh – might have a noticeable effect on the world vanadium market, but it is probably feasible. Current worldwide production of vanadium is 40 000 tonnes per year [5fas17]. A 10 GWh system, assuming 1-molar vanadium solution, would contain 36 000 tonnes of vanadium – one year's worth of current production. Vanadium is currently produced as a by-product of other processes, and the total world vanadium resource is estimated to be 63 million tonnes.

"Economical" solutions

In the present world which doesn't put any cost on carbon pollution, the financial bar that a storage system must beat is an ugly alternative: storage can be emulated by simply putting up an extra gas-fired power station to

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

meet extra demand, and shedding any excess electrical power by throwing it away in heaters.

Seasonal fluctuations

The fluctuations of supply and demand that have the longest timescale are seasonal. The most important fluctuation is that of building-heating, which goes up every winter. Current UK natural gas demand varies throughout the year, from a typical average of $36\,\mathrm{kWh/d}$ per person in July and August to an average of $72\,\mathrm{kWh/d}$ per person in December to February, with extremes of $30-80\,\mathrm{kWh/d/p}$.

Some renewables also have yearly fluctuations – solar power is stronger in summer and wind power is weaker.

How to ride through these very-long-timescale fluctuations? Electric vehicles and pumped storage are not going to help store the sort of quantities required. A useful technology will surely be long-term thermal storage. A big rock or a big vat of water can store a winter's worth of heat for a building.

more here

Notes

page no.

- 202 The total output of the wind fleet of the Republic of Ireland. Data from eirgrid.com [2hxf6c].
 - "Loss of wind causes Texas power grid emergency". [2199ht] Actually, my reading of this news article is that this event, albeit unusual, was an example of normal power grid operation. The grid has industrial customers whose supply is interruptible, in the event of a mismatch between supply and demand. Wind output dropped by 1.4 GW at the same time that Texans' demand increased by 4.4 GW, causing exactly such a mismatch between supply and demand. The interruptible supplies were interrupted. Everything worked as intended.
 - Another example, where better power-system planning would have helped: "Spain wind power hits record, cut ordered". [3x2kvv] Spain's average electricity consumption is 31 GW. On Tuesday March 4th 2008, its wind generators were delivering 10 GW. "Spain's power market has become particularly sensitive to fluctuations in wind."
 - Supporters of wind energy play down this problem: "Don't worry individual wind farms may be intermittent, but taken together, the sum of all wind farms is much less intermittent." For an example, see the website yes2wind.com, which, on its page "debunking the myth that wind power isn't reliable" asserts that "the variation in output from wind farms distributed around the country is scarcely noticeable." http://www.yes2wind.com/intermittency_debunk.html
- © David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

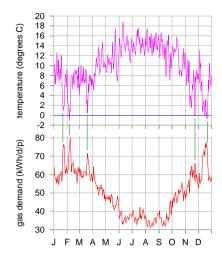


Figure 26.17. Gas demand in Britain during 2007. The upper graph shows the temperature.

- ... wind is intermittent, even if we add up lots of turbines covering a whole country. The UK is a bit larger than Ireland, but the same problem holds there too. Oswald et al. [2008]
- 206 *Dinorwig's pumped-storage efficiency is 75%*. Figure 26.18 shows data. Further information about Dinorwig and the alternate sites for pumped storage: Baines et al. [1983, 1986].
- 207 *Table 26.8, Alternative sites for pumped storage facilities.* The proposed upper reservoir for Bowydd was Llyn Newydd, grid reference SH 722 470; for Croesor: Llyn Cwm-y-Foel, SH 653 466.
- 211 Fridges can be modified to nudge their internal thermostats up and down ... in response to the mains frequency. [2n3pmb] Further links: Dynamic Demand http://www.dynamicdemand.co.uk/; http://www.responsiveload.com/; and http://www.rltec.com/.
- 212 In South Africa . . . demand-management systems are being installed. [2k8h4o]
 - For over 25 years (since 1982), Fair Isle has had two electricity networks. http://www.fairisle.org.uk/FIECo/
 Wind speeds are between 3 m/s and 16 m/s most of the time; 7 m/s is the most probable speed.

214 Figure 26.15.

Storage efficiencies.

Lithium-Ion Batteries: 88% efficient. Source: http://www.national.com/appinfo/power/files/swcap_eet.pdf

Lead-Acid Batteries: 85-95%. Source: http://www.windsun.com/Batteries/Battery_FAQ.htm

Compressed air storage: 18% efficient. Source: Lemofouet and Rufer [2005], Lemofouet-Gatsi [2006]. See also [Denholm et al., 2005]. Air/oil: hydraulic accumulators, as used for regenerative braking in trucks, are compressed-air storage devices that can be 90% efficient round-trip and allow 70% of kinetic energy to be captured Sources: Lemofouet-Gatsi [2006], [5cp27j].

- Table 26.14. Sources: Xtronics http://xtronics.com/reference/energy_density.htm; Battery University http://www.batteryuniversity.com/partone-3.htm; wikipedia http://en.wikipedia.org/wiki/Flywheel_energy_storage.

The latest batteries with highest energy density are lithium-sulphur and lithium-sulphide batteries, which have an energy density of 300 Wh/kg.

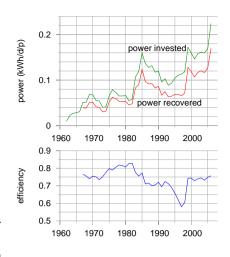


Figure 26.18. Efficiency of the four pumped storage systems of Britain.

27 Five energy plans for Britain

If we are to get off our current fossil fuel addiction we need a plan for radical action. And the plan needs to add up. The plan also needs a political and financial roadmap. Politics and economics are not part of this book's brief. So here I will simply discuss what the technical side of a plan that adds up might look like.

There are many plans that add up. In this chapter I will describe five. Please don't take any of the plans I present as "the author's recommended solution." My sole recommendation is this:

Make sure your policies include a plan that adds up!

Each plan has a consumption side and a production side: we have to specify how much power our country will be consuming, and how that power is to be produced. To avoid the plan's taking many pages, I deal with a cartoon of our country, in which we consume power in just three forms: transport, heating, and electricity. This is a drastic simplification, omitting industry, farming, food, imports, and so forth. But I hope it's a helpful simplification, allowing us to compare and contrast alternative plans in one minute. Eventually we'll need more detailed plans, but today, we are so far away from our destination, I think that a simple cartoon is the best way to capture the issues.

I'll present a few plans which I believe are technically feasible plans for the UK in 2050. All will share the same consumption side. I emphasize again, this doesn't mean that I think this is the correct plan for consumption, or the only plan. I just want to avoid overwhelming you with a proliferation of plans. On the production side, I will describe a range of plans using different mixes of renewables, "clean coal," and nuclear power.

The current situation

The current situation in our cartoon country is this: Transport uses 40 kWh/d per person. (That's transporting both humans and stuff.) Most of that energy is currently consumed as petrol, diesel, or kerosene. Heating of air and water uses 40 kWh/d per person. Much of that is provided by natural gas. Delivered electricity amounts to 18 kWh/d/p and uses fuel (mainly coal, gas, and nuclear) with an energy content of 45 kWh/d per person. The remaining 27 kWh/d/p is going up cooling towers (25 kWh/d/p) and lost in the wires of the distribution network (2 kWh/d/p). The total energy input to this present-day cartoon country is 125 kWh/d per person.

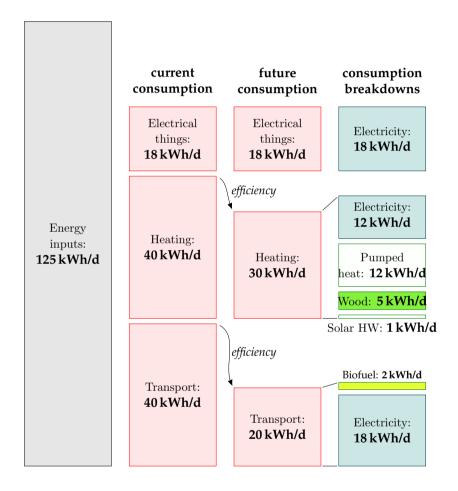


Figure 27.1. Current consumption per person in "cartoon Britain 2008" (left two columns), and a future consumption plan, along with a possible breakdown of fuels (right two columns). This plan requires that electricity supply be increased from 18 to 48 kWh/d/p of electricity.

Common features of all five plans

In my future cartoon country, the energy consumption is reduced by using more efficient technology for transport and heating.

In the five plans for the future, **transport** is largely electrified. Electric engines are more efficient than petrol engines, so the energy required for transport is reduced. Public transport (also largely electrified) will be better integrated, better personalized, and better patronized. There will be a few essential vehicles that can't be easily electrified, and for those we will make our own liquid fuels (for example biodiesel or biomethanol or cellulosic bioethanol). The energy for transport is 18 kWh/d/p of electricity and 2 kWh/d/p of liquid fuels. The electric vehicles' batteries will serve as an energy storage facility, helping to cope with fluctuations of electricity supply and demand. The area required for the biofuel production would be about 12% of the UK (500 m² per person), assuming that biofuel production comes from 1%-efficient plants and that conversion of plant to fuel is 33% efficient. Alternatively, the biofuels could be imported if we could persuade other countries to devote the required (Wales-sized) area of agricultural land to biofuels for us.

In all five plans, the energy consumption of **heating** is reduced by improving the insulation of all buildings, and improving the control of temperature (through thermostats, education, and the promotion of sweaterwearing by sexy personalities). New buildings (all those built from 2010 onwards) are really well insulated and require almost no space heating. Old buildings (which will still dominate in 2050) are mainly heated by airsource heat pumps and ground-source heat pumps. Some water heating is delivered by solar panels (2.5 square metres on every house), some by heat pumps, and some by electricity. Some buildings located near to managed forests and energy-crop plantations are heated by biomass. The power required for heating is thus reduced from $40 \, \text{kWh/d/p}$ to $12 \, \text{kWh/d/p}$ of electricity, $2 \, \text{kWh/d/p}$ of solar hot water, and $5 \, \text{kWh/d/p}$ of wood.

The wood for making heat (or possibly combined heat and power) comes from nearby forests and energy crops (perhaps miscanthus grass, willow, or poplar) covering a land area of 6 million hectares, or $1000\,\mathrm{m}^2$ per person; this would correspond to 35% of the UK's agricultural land, which has an area of $2800\,\mathrm{m}^2$ per person. The energy crops would be grown mainly on the lower-grade land, leaving the higher-grade land for food-farming. $1000\,\mathrm{m}^2$ of energy crops will yield 1 oven dry ton per year, which has an energy content of about $10\,\mathrm{GJ}$ per year, or $7.6\,\mathrm{kWh/d}$; of this energy, about 33% is lost in the process of heat production and delivery. The final heat delivered is $5\,\mathrm{kWh/d}$ per person.

In these plans, I assume the current demand for **electricity** for gadgets, light, and so forth is maintained. So we still require $18\,\text{kWh(e)/d/p}$ of electricity. Yes, lighting efficiency will be improved by a switch to LEDs for most lighting, but we'll have increased the number of gadgets in our



Figure 27.2. A solar water heater providing hot water for a family in Michigan. The system's pump is powered by the small photovoltaic panel on the left.

lives, for example video-conferencing systems to help us travel less, and new gadgets to ensure the blessings of economic growth.

So the total consumption of electricity under this plan goes up (because of the 18 kWh/d/p for electric transport and the 12 kWh/d/p for heat pumps) to 48 kWh/d/p (or 120 GW per UK). This is nearly a tripling of UK electricity consumption. Where's that energy to come from?

Let's describe some alternatives. Not all of these alternatives are "sustainable" as defined in this book; but they are all low-carbon plans.

Producing lots of electricity - the components

To make lots of electricity, our plan will use some amount of onshore and offshore wind; some solar photovoltaics; possibly some solar power bought from countries with deserts; waste incineration (including refuse and agricultural waste); hydroelectricity (the same amount as we get today); perhaps wave power; tidal barrages, tidal lagoons, and tidal stream power; perhaps nuclear power; and perhaps some "clean fossil fuel," that is, coal burnt in power stations that do carbon capture and storage. Each plan will aim for a total electricity production of 50 kWh/d/p on average – I got this figure by rounding up the 48 kWh/d/p of assumed average demand, allowing for some loss in the distribution network.

Some of the plans that follow will import power from other countries. For comparison, it may be helpful to know how much of our current power is imported today. The answer is that, in 2006, the UK imported $28\,\mathrm{kWh/d/p}$ of fuel – 23% of its primary consumption. These imports are dominated by coal $(18\,\mathrm{kWh/d/p})$, crude oil $(5\,\mathrm{kWh/d/p})$, and natural gas $(6\,\mathrm{kWh/d/p})$. Nuclear fuel (uranium) is not usually counted as an import since it's easily stored.

In all five plans I will assume that we scale up municipal waste incineration so that almost all waste is incinerated or recycled rather than landfilled. Incinerating 1 kg per day per person of waste yields roughly 0.5 kWh/d per person of electricity. I'll assume that a similar amount of agricultural waste is also incinerated, yielding 0.6 kWh/d. Incinerating this waste would require roughly 3 GW of waste-to-energy capacity, a ten-fold increase over the incinerating power stations of 2008. London (7 million people) would have twelve 30 MW waste-to-energy plants like SELCHP in South London. Birmingham (1 million people) would have two of them. Every town of 200 000 people would have a 10 MW waste-to-energy plant. One good side-effect of this waste incineration plan is that it eliminates future methane emissions from landfill sites.

In all five plans, hydroelectricity contributes 0.2 kWh/d, the same as today.

Electric vehicles are used as a dynamically-adjustable load on the electricity network. The average power required to charge the electric vehicles is $45\,\mathrm{GW}$ ($18\,\mathrm{kWh/d/p}$). So fluctuations in renewables such as solar and

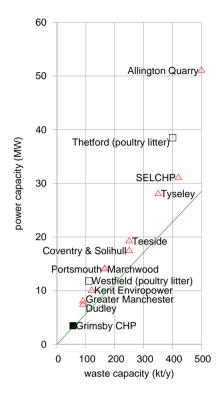


Figure 27.3. Waste-to-energy facilities in Britain. The line shows the average power production assuming 1 kg of waste \rightarrow 0.5 kWh of electricity.

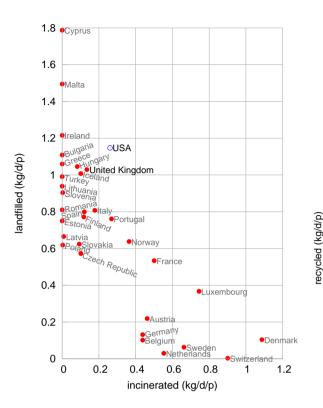
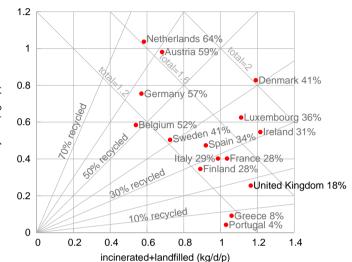


Figure 27.4. Left: Municipal solid waste put into landfill, versus amount incinerated, in kg per day per person, by country. Right: Amount of waste recycled versus amount landfilled or incinerated. Percentage of waste recycled is given beside each country's name.



wind can be balanced this load, as long as the fluctuations are not too big or lengthy.

Daily swings in electricity demand are going to be bigger because of the replacement of gas for cooking and heating by electricity (see figure 26.17). To ensure that surges in demand of 10 GW lasting up to 5 hours can be covered, all the plans would build five new pumped storage facilities like Dinorwig (or upgrade hydroelectric facilities to provide pumped storage). 50 GWh of storage is equal to five Dinorwigs, each with a capacity of 2 GW. Some of the plans that follow will require extra pumped storage beyond this.

Producing lots of electricity - plan D

Plan D is the "domestic diversity" plan, in which we use a lot of every possible source of electricity, and depend relatively little on energy supply from other countries.

Here's where plan D gets its 50 kWh/d/p of electricity from. Wind: 8 kWh/d/p (20 GW average; 66 GW peak) (plus about 400 GWh of associated pumped storage facilities). Solar PV: 3 kWh/d/p. Waste incineration: 1.3 kWh/d/p. Hydroelectricity: 0.2 kWh/d/p. Wave: 2 kWh/d/p. Tide:

(c) David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

plan D Clean coal: 16 kWh/d Nuclear: 16 kWh/d Tide: 3.7 Wave: 2 Hydro: **0.2** Waste: 1.1 Pumped heat: 12 Wood: 5kWh/d Solar HW: 1 Biofuels: PV: **3 kWh/d**

X7:... 1. 0 1-XA71

 $3.7 \,\text{kWh/d/p}$. Nuclear: $16 \,\text{kWh/d/p}$ ($40 \,\text{GW}$). Clean coal: $16 \,\text{kWh/d/p}$ ($40 \,\text{GW}$).

The figure for wind corresponds to a 30-fold increase in wind power over the installed power in 2008. Britain would have nearly three times as much wind hardware as Germany has now. Installing this windpower over a period of 10 years would require roughly 50 jack-up barges.

To get 3 kWh/d/p from solar photovoltaics requires 6 m² of 20%-efficient panels per person. Most south-facing roofs would have to be completed covered with panels; alternatively, it might be more economical, and cause less distress to the League for the Preservation of Buildings, to plant many of this panels in the countryside in the traditional Bavarian manner (figure 6.7, 43).solar farm

The waste incineration corresponds to $1 \, \text{kg}$ per day per person of domestic waste (yielding $0.5 \, \text{kWh/d}$) and a similar amount of agricultural waste yielding $0.6 \, \text{kWh/d}$; the hydroelectricity is $0.2 \, \text{kWh/d}$, the same amount as we get from hydro today.

The wave power requires 7500 Pelamis deep-sea wave devices occupying 500 km of Atlantic coastline (see the map on p77).

The tide power comes from 5 GW of tidal stream installations, a 2 GW Severn barrage, and 2.5 GW of tidal lagoons, which can serve as pumped storage systems too.

The nuclear power ($40\,\mathrm{GW}$) is a roughly four-fold increase of the 2007 nuclear fleet. If we had $16\,\mathrm{kWh/d/p}$ of nuclear power, we'd lie in between Belgium, Finland, France and Sweden, in terms of per-capita production: Belgium and Finland produce roughly $12\,\mathrm{kWh/d/p}$; France and Sweden produce $19\,\mathrm{kWh/d/p}$ and $20\,\mathrm{kWh/d/p}$.

The clean coal (40 GW) corresponds to taking the current fleet of coal stations, which deliver about 30 GW, retrofitting carbon capture systems to them, which would reduce their output to 22 GW, then building another 18 GW of new clean-coal stations. This level of coal power requires an energy input of about 53 kWh/d/p of coal, which is a little bigger than our current rate of burning of all fossil fuels, and well above the level we estimated as being "sustainable" in Chapter 23. This rate of consumption of coal is roughly three times the current rate of coal imports (18 kWh/d/p). If we didn't reopen UK coal mines, this plan would have 32% of UK electricity depending on imported coal. Reopened UK coal mines could deliver an energy input of about 8 kWh/d/p, so either way, the UK would not be self-sufficient for coal.

Do any features of this plan strike you as unreasonable or objectionable? If so, perhaps one of the next four plans is more to your liking.

In all the plans that follow, the electricity contributions of hydroelectricity and waste incineration are going to remain unchanged, so I won't mention them again.

Producing lots of electricity – plan N

Plan N is the "NIMBY" plan, for people who don't like industrializing the British countryside with renewable energy facilities, and who don't want new nuclear power stations either. Let's reveal the plan in stages.

First, we turn down all the renewable knobs from their very high settings in plan D to: wind: $2 \, kWh/d/p$ (5 GW average); solar PV: $0 \, kWh/d/p$; wave: $0 \, kWh/d/p$; tide: $1 \, kWh/d/p$.

We've just lost ourselves $14 \, \text{kWh/d/p}$ (35 GW per UK) by turning down the renewables knob. (Don't misunderstand! Wind is still hugely increased over its 2008 levels – it's increased eight-fold, to be precise.)

In the NIMBY plan, nuclear power's contribution is reduced to $10\,\mathrm{kWh/d/p}$ (25 GW). – a reduction by 15 GW compared to plan D, but still a substantial increase over today's levels. 25 GW of nuclear power could, I think, be squeezed onto the existing nuclear sites. I left the clean-coal contribution unchanged at $16\,\mathrm{kWh/d/p}$ ($40\,\mathrm{GW}$).

Where are we going to get an extra 50 GW from? The NIMBY says, "not in my back yard, but in someone else's." Thus the NIMBY plan pays other countries for imports of solar power from their deserts to the tune of 20 kWh per day per person (50 GW).

This plan requires the creation of five blobs each the size of London (44 km in diameter) in the transmediterranean desert, filled with solar power stations. It also requires power transmission systems to get the power up to the UK. Today's high voltage electricity connection from France can deliver up to 2 GW of power. So this plan requires a twenty-five-fold increase in the capacity of the electricity connection from the continent. (Or an equivalent power-transport solution – perhaps ships filled with methanol plying their way from desert shores.)

Having less wind power, plan N doesn't need to build in Britain the extra pumped-storage facilities mentioned in plan D, but given its dependence on sunshine, it still requires storage systems to be built somewhere along the line to store energy from the fluctuating sun. Molten salt storage systems at the solar power stations are one option. Tapping into pumped storage systems in the Alps might also be an option. Converting the electricity to a storable fuel such as methanol is another option, though conversions entail losses and thus require more solar power stations.

This plan gets 32%+40%=72% of the UK's electricity from other countries.

Producing lots of electricity - plan L

Some people say "we don't want nuclear power!" How can we satisfy them? Perhaps it should be the job of this anti-nuclear bunch to persuade the NIMBY bunch that they do want renewable energy in our back yard after all.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

plan N

Solar in deserts: 20 kWh/d

Clean coal: 16 kWh/d

Nuclear: 10 kWh/d

Tide: 1 kWh/d

 $\begin{array}{l} \text{H}\underline{\text{ydro: } 0.2\,kWh/d} \\ \text{Waste: } 1.1\,kWh/d \end{array}$

Pumped heat: 12 kWh/d

Wood: 5 kWh/d
Solar HW: 1 kWh/d
Biofuels: 2 kWh/d
Wind: 2 kWh/d

plan L

Solar in deserts: 16 kWh/d

Clean coal: 16 kWh/d

Tide: **3.7**Wave: **2**

Hydro: **0.2**

Waste: **1.1**

Pumped heat: 12

Wood: 5

Solar HW: 1

Biofuels: 2 PV: 3

Wind: 8

We can create a nuclear-free plan by taking plan D, keeping all those renewables in our back yard, and doing a straight swap of nuclear for desert power.

Wind: 8 kWh/d/p (20 GW average) (plus about 400 GWh of associated pumped storage facilities). Solar PV: 3 kWh/d/p. Wave: 2 kWh/d/p. Tide: 3.7 kWh/d/p. Clean coal: 16 kWh/d/p (40 GW). Solar power in deserts: 16 kWh/d/p (40 GW average power).

This plan imports 64% of UK electricity from other countries.

I call this "plan L" because it aligns fairly well with the policies of the Liberal Democrats – at least it did when I first wrote this chapter in mid-2007; recently, they've been talking about "real energy independence for the UK," and have announced a zero-carbon policy, under which Britain would be a net energy exporter; their policy does not detail how these targets would be met.

Producing lots of electricity - plan G

Some people say "we don't want nuclear power, and we don't want coal!" It sounds a reasonable goal, but we need a plan to deliver it.

I call this plan "plan G," because I guess the Green Party don't want nuclear or coal, though I think not all Greens would like the rest of the plan. Greenpeace, I know, *love* wind, so plan G is dedicated to them too, because it has *lots* of wind.

I make plan G by starting again from plan D, nudging up the wave contribution by 1 kWh/d and bumping up wind power fourfold (relative to plan D) to 32 kWh/d/p, so that wind delivers 64% of all the electricity. This is a 120-fold increase of British wind power over today's levels. Under this plan, *world* wind power in 2007 is multiplied by four, with all of the increase being placed on or around the British Isles.

The immense dependence of plan G on renewables, especially wind, creates difficulties for our main method of balancing supply and demand, namely adjusting the charging rate of millions of rechargeable batteries for transport. So in plan G we have to include substantial additional pumped-storage facilities, capable of balancing out the fluctuations in wind on a timescale of days. Pumped-storage facilities equal to four hundred Dinorwigs can completely replace wind for a national lull lasting 2 days. Roughly one hundred of Britain's major lakes and lochs would be required for the associated pumped-storage systems.

Wind: $32 \, \text{kWh/d/p}$ (80 GW average) (plus about $4000 \, \text{GWh}$ of associated pumped-storage facilities). Solar PV: $3 \, \text{kWh/d/p}$. Wave: $3 \, \text{kWh/d/p}$. Tide: $3.7 \, \text{kWh/d/p}$. Solar power in deserts: $7 \, \text{kWh/d/p}$ (17 GW).

This plan gets 14% of its electricity from other countries.

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

plan G

Solar in deserts: 7

Tide: **3.7**

Wave: 3

Hydro: **0.2**

Waste: 1.1

Pumped heat: 12

Wood: 5

Solar HW: 1

Biofuels: 2
PV: 3

Wind: **32**

plan E

Nuclear: 44 kWh/d

Tide: **0.7**

Hydro: **0.2**

Waste: **1.1**

Pumped heat: 12

Wood: 5

Solar HW: 1

Biofuels: 2

Wind: 4

Producing lots of electricity – plan E

E stands for "economics." On a level economic playing field with a strong price signal preventing the emission of CO₂, we don't get a diverse solution, we get an economically optimal solution that delivers the required power at the lowest cost. And when "clean coal" and nuclear go head to head on price, it's nuclear that wins. (The capital cost of regular dirty coal power stations is £1 billion per GW, about the same as nuclear; but the capital cost of clean-coal power, including carbon capture and storage, is roughly £2 billion per GW.) Solar power in other people's deserts loses to nuclear power when we take into account the cost of the required 2000-km-long transmission lines (though van Voorthuysen [2008] reckons that with Nobel-prize-worthy developments in solar-powered production of chemical fuels, solar power in deserts would be the economic equal of nuclear power). Offshore wind also loses to nuclear, but I've assumed that onshore wind costs about the same as nuclear. My final plan is a rough guess for what would happen in a liberated energy market with a strong carbon price.

Wind: 4 kWh/d/p (10 GW average). Solar PV: 0 kWh/d/p. Wave: 0 kWh/d/p. Tide: 0.7 kWh/d/p. Nuclear: 44 kWh/d/p (110 GW).

This plan has a ten-fold increase in our nuclear power over 2007 levels. 110 GW is roughly double France's nuclear fleet. I included a little tide because I believe a well-designed tidal lagoon facility can compete with nuclear power.

In this plan, Britain has no energy imports (except for the uranium, which, as we said before, doesn't count).

Figure 27.5 shows all five plans.

How these plans relate to carbon-sucking and air travel

In a future world where carbon pollution is priced appropriately, we will be interested in any power scheme that can at low-cost put extra carbon down a hole in the ground. Such carbon-neutralization schemes might permit us to continue flying at 2004 levels (while oil lasts). In 2004, average UK emissions of CO_2 from flying were about 0.5t per year per person. Accounting for the full greenhouse impact of flying, perhaps the effective emissions were about $1 \, t \, CO_2^{(e)}$ per year per person. In all five of these plans I assumed that 25% of the UK was devoted to the production of energy crops which were then used for heating or for combined heat and power. If instead we directed all these crops to power-plants with carbon capture and storage, the "clean coal" plants that featured in three of the plans, then the amount of extra CO_2 captured would be about 1 t of CO_2 per year. If the municipal and agricultural waste incinerators were located at clean-coal plants too so that they could share the same chimney, perhaps the total captured could be increased to $2 \, t \, CO_2$ per year per person. This

⁽c) David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

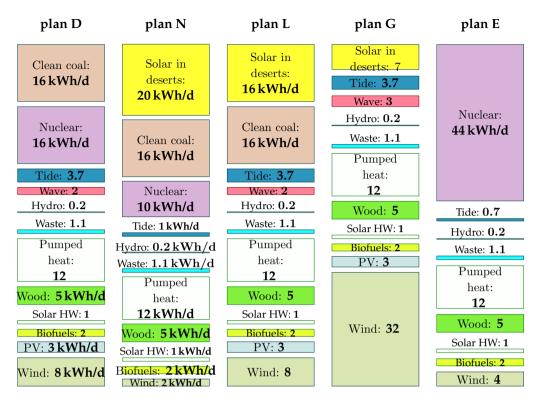


Figure 27.5. All five plans.

arrangement would have additional costs: the biomass and waste might have to be transported further; the carbon-capture process would require a significant fraction of the energy from the crops; and the lost building-heating would have to be replaced by more air-source heat pumps. But, if carbon-neutrality is our aim, it would be worth planning ahead by seeking to locate new clean-coal plants with waste incinerators in regions close to potential biomass plantations.

"All these plans are absurd!"

If you don't like these plans, I'm not surprised. I agree that there is something unpalatable about every one of them. Feel free to make another plan that is more to your liking. But make sure it adds up!

Perhaps you will conclude that a viable plan has to involve less power consumption per capita. I might agree with that, but it's a difficult policy to sell – recall Tony Blair's response (p246) when someone suggested he should fly overseas for holidays less!

Alternatively, you may conclude that we have too high a population density, and that a viable plan requires fewer people. Again, a difficult policy to sell.

TBC

I need to talk about growth and figure 18.6.

Notes and further reading

page no.

- **??** *Incinerating 1 kg of waste yields roughly 0.5 kWh of electricity.* The calorific value of municipal solid waste is about 2.6 kWh per kg; power stations burning waste produce electricity with an efficiency of about 20%. Source: SELCHP tour guide.
- 222 Figure 27.4. Data from Eurostat, www.epa.gov, and www.esrcsocietytoday. ac.uk/ESRCInfoCentre/.
- 225 The policies of the Liberal Democrats. See www.libdems.org.uk: [5os7dy], [yrw2oo].
- 222 Current UK natural gas demand varies throughout the year, from typical average of 90 GW in July and August to average of 180 GW in December to February, with extremes of 75–200 GW (figure ??, p??). There is a good correlation with temperature: 90 GW is always used no matter how high the temperature. From temperature 20 °C downwards demand increases linearly from 90 GW at 20 °C to 200 GW at 0 °C.

28 Putting costs in perspective

A plan on a map

Let me try to make clear the scale of the previous chapter's plans by showing you a map of Britain bearing a sixth plan. This sixth plan lies roughly in the middle of the first five.

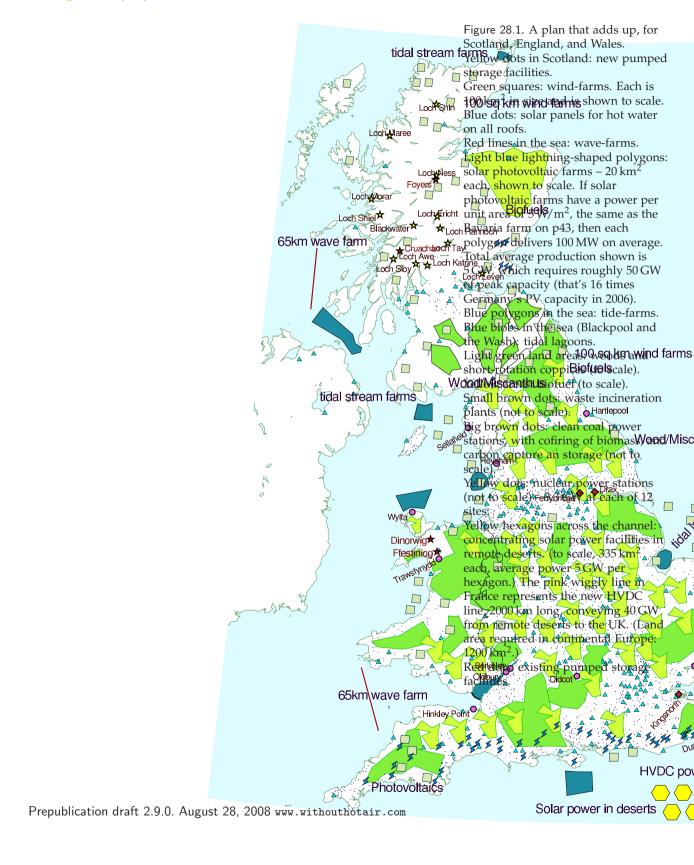
More explanatory notes to come here. TBC.

Let's look at this plan in a bit more detail to assess its costs: its land area costs, and its financial costs.

For simplicity, the financial costs are estimated using today's prices for comparable facilities, many of which are early prototypes. We can expect many of the prices to drop significantly.

Solar in deserts: 16 kWh/d Clean coal: 3 Nuclear: 16 kWh/d Tide: **3.7** Wave: **0.3** Hydro: 0.2 Waste: **1.1** Pumped heat: 12 Wood: 5 Solar HW: 1 Biofuels: 2 PV: **2**

Wind: 8



52 onshore wind- farms, each 100 square km in size.	Capacity: 0.67 GW per windfarm. Total capacity 35 GW.	Rough cost: £27b. (Based on the projected cost of Lewis windfarm, £500 million for 650 MW.)	£450 per person.	Average power delivered: 4.2 kWh/d/p.
29 offshore wind- farms, each 100 square km in size.	Capacity: 1 GW per windfarm. Total capacity 29 GW.	Rough cost: £33b, plus £3b capital investment in jack-up barges. (Based on the cost of Kentish Flats.)	£650 per person.	Average power delivered: 3.5 kWh/d/p.
1000 km ² of photovoltaic farms	Capacity: 48 GW	Rough cost: £190b (Based on Solarpark in Mühlhausen, Bavaria)	£3200 per person.	2kWh/d/p
Solar hot water panels: 1 m ² of roof per person. (60 km ² total)	£1200 per person	1kWh/d/p		
Concentrating solar power in deserts: 2700 km ² . Average power output: 40 GW.	Rough cost: £500b	£8300 per person	16 kWh/d/p	
Land in Europe for 1600 km of HVDC power lines with 50 GW capacity: 1200 km ²	Rough cost: £1b (assuming land costs £7500 per ha in Europe)	£15 per person		
2000 km of HVDC power lines with 50 GW capacity: Biofuels: 30 000 km ² Wood/Miscanthus: 31 000 km ²	£1b (based on German Aerospace Center estimates)	£15 per person	2kWh/d/p 5kWh/d/p	
Waste incinerators: 100 new 30 MW incinerators	£8.5 billion	£140 per person	based on SELCHP, which cost £85 mil- lion	

I'd like to emphasize that I am not advocating this particular plan – it includes several features that I, as dictator of Britain, would not select. I've deliberately included all available technologies, so that you can try out your own plans with other mixes.

For example, if you say 'photovoltaics are going to be too expensive, I'd like a plan with more wave power instead', you can see how to do it: you need to increase the wave-farms eight-fold.

If you don't like the wind-farms' locations, feel free to move them (but where to?). Bear in mind that putting more of them offshore will increase costs.

[©] David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

If you'd like fewer windfarms, no problem – just specify which of the other technologies you'd like instead.

Perhaps you think that this plan (and all five plans in the previous chapter) devotes unreasonably large areas to biofuels. Fine: you may therefore conclude that the demand for liquid fuels for transport must be reduced below the 2 kWh per day per person that this plan assumed; or that liquid fuels must be created in some other way.

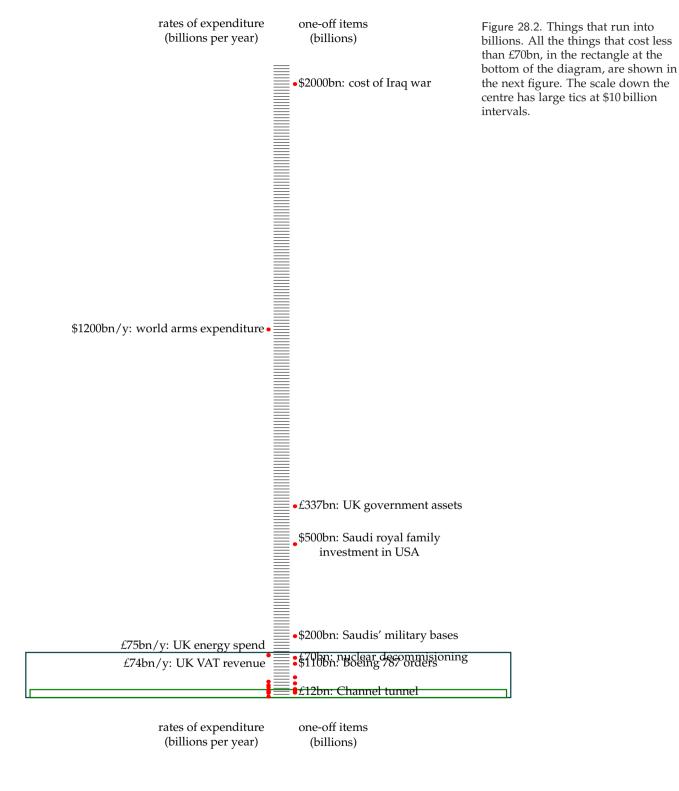
Cost of switching from fossil fuels to renewables

Every wind farm costs a few million pounds to build and delivers a few megawatts. As a very rough ballpark figure in 2007, installing one watt of power costs one pound; one kilowatt costs one thousand pounds; a megawatt of wind costs a million; a gigawatt of nuclear costs a billion or perhaps two. Other renewables are more expensive. We (Britain) currently consume a primary power of roughly 300 GW, most of which is fossil fuel. So we can anticipate that a major switching from fossil fuel to renewables is going to require roughly 300 GW of renewables and thus have a cost in the ballpark of £300 billions. A government report leaked by the Guardian in August 2007 agrees: it estimates that achieving "20% by 2020" (that is, 20% of all energy from renewables, which would require an increase in renewable power of 80 GW) could cost "up to £22 billion" (which would average out to £1.7 billion per year). This estimate is actually significantly smaller than the rule of thumb I just mentioned, which would have suggested that 80 GW would cost £80 billion. The authors of the leaked report seem to view £22 billion as an "unreasonable" cost, preferring a target of 9% renewables, which would cost approximately £4 billion (£0.3 billion per year). (Another reason they give for disliking the "20% by 2020" target is that the resulting greenhouse gas savings "risk making the EU emissions trading scheme redundant." Terrifying thought!)

Billions are big numbers and hard to get a feel for. To try to help put the cost of kicking fossil fuels in perspective, this chapter discusses other things that also come in billions of pounds, or in billions per year. I'll also express many of these expenditures "per person", dividing the total by an appropriate population.

Perhaps the most relevant quantity to compare with is the money we *already* spend on energy every year. In the UK, the money spent on energy by final users is £75 billion per year, and the total market value of all energy consumed is £130 billion per year. So the idea of spending £1.7 billion per year on investment in future energy infrastructure isn't at all unreasonable – it is less than 3% of our current expenditure on energy!

Another good comparison to make is with our annual expenditure on insurance: some of the investments we need to make offer an uncertain return – just like insurance. UK individuals and businesses spend £90bn per year on insurance.



© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

rates of expenditure Figure 28.3. Things that run into (billions) (billions per year) billions. (Detail.) £75bn/y: UK energy spend £74bn/y: UK VAT revenue •£70bn: nuclear decommisioning •£64.5bn: rail investment plan - \$110bn: Boeing 787 orders •\$66bn: assets of Gates Foundation £28bn/y: UK charities' income • \$46bn/y: War on drugs • •£25bn: replacing Trident \$40bn/y: Exxon profits • \$33bn/y: perfume and makeup • •£15bn: identity cards for all £13bn/y: Shell profits •£12bn: Channel tunnel •£6.7bn: ITER fusion project £5bn/y: UK arms exports £4.3bn: Heathrow Terminal 5 £3.2bn: Langeled gas pipeline £1.9bn: widening M1 motorway £2.5bn/y: Tesco profits £2|5bn/y: Government monitoring government• rates of expenditure one-off items (billions per year) (billions)

one-off items

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

Other things that cost a billion

Subsidies

US subsidy for corn-based ethanol: \$2 billion per year [2kz3hk]. (\$7 per year per person in the USA.)

£1 billion: amount "earned" in windfall profits by the UK's most-polluting industries from the first year of the European carbon trading scheme [3717fr]. (£17 per person in the UK.)

£56 billion over 25 years: cost of decommissioning the UK's nuclear power stations. (That's the 2004 figure; in 2008 it was up to £73 billion. http://news.bbc.co.uk/1/hi/uk/7215688.stm (£1200 per person.)

Transport

\$1.2 billion: President Bush's Hydrogen Fuel Initiative announced in the 2003 State of the Union Address. (\$4 per person in the USA.)

£1.4billion: The UK government gave Virgin trains a £1.4billion subsidy over five years to run the London-to-Glasgow service and help offset high track charges. (£23 per person in the UK.)

£4.3 billion: cost of London Heathrow Airport's Terminal 5. (£72 per person in the UK.)

£8.6 billion: cost of upgrading the west-coast mainline [2qtr71]. (£140 per person in the UK.)

£64.5 billion – UK government's rail investment plan announced January 2002. (Half from the public purse, half from private investors.) [21q4j8]. (£1100 per person in the UK.)

£15–20b/y: estimated cost to UK industry of traffic congestion. (£250–330 per year per person in the UK.)

\$3b/y: annual spending by the eleven teams participating in Formula One racing.

110b: as of 7/7/7, 47 customers worldwide have ordered 677 Boeing 787 airplanes worth more than 110 billion.

Subsidies and tax-breaks

The UK air transport industry receives over £9 billion per year in tax breaks because of tax-free fuel, VAT-free tickets, and profits from duty-free sales [2uraxb]. (£150 per year per person in the UK.)

Tax cut for drivers: At the 2002 Budget, the Chancellor cut road fuel duty by around £1 billion a year. (£17 per year per person in the UK.)

Road-building

£1.9 billion: The cost of widening the M1 through the East Midlands (from junction 21 to 30), estimated at £700 million in the multi modal study

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

Final Report (December 2001), has risen to £1.9 billion upon entry into the Targeted Programme of Improvements (April 2004) [yu8em5]. (£32 per person in the UK.)

Government investment in renewable-energy-related research and development

In 2002–3, the UK Government's commitment to renewable-energy-related R&D was £12.2 million. (Source: House of Lords report.) (£0.20 per person in the UK.)

Global expenditure on climate research: \$2 billion.

Energy

The money spent on energy by the final users in the UK in 2004 was £75 billion per year (£1250 per person), which is about 6% of the UK's gross domestic product. Dividing the money spent by the energy delivered, the average cost paid per kWh was 2.7p.

Philanthropy

The Gatsby Trust's Settlor (David Sainsbury) has declared his ambition to give away at least £1 billion in his lifetime. (The Gatsby Charitable Foundation. Annual Report and Accounts 2006, page 3.)

\$66 billion – assets of the Gates Foundation [y1x4xq].

The endowment of the Mohammed Bin Rashid Al Maktoum foundation (www.mbrfoundation.ae) is \$10 billion.

The annual income of UK charities is £28 billion.

Special occasions

Cost of Athens 2004 Olympics: €9 billion [2nznsz].

Cost of the London 2012 Olympics: £2.4 billion; no, I'm sorry, £5 billion [3x2cr4]; or perhaps £9 billion [2dd4mz]. (£150 per person in the UK.)

Business as usual

£2.5b/y: Tesco's profits (announced 2007). (£42 per year per person in the UK.)

£10.2 b/y: spent by British people on food that they buy but do not eat. (£170 per year per person in the UK.)

£11b/y (\$22b): BP's profits (2006).

£13b/y (\$25b): Royal Dutch Shell's profits (2006). Most of Shell's profits come from finding and extracting oil, and then selling it on to the markets. \$40b/y. Exxon's profits (2006).

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

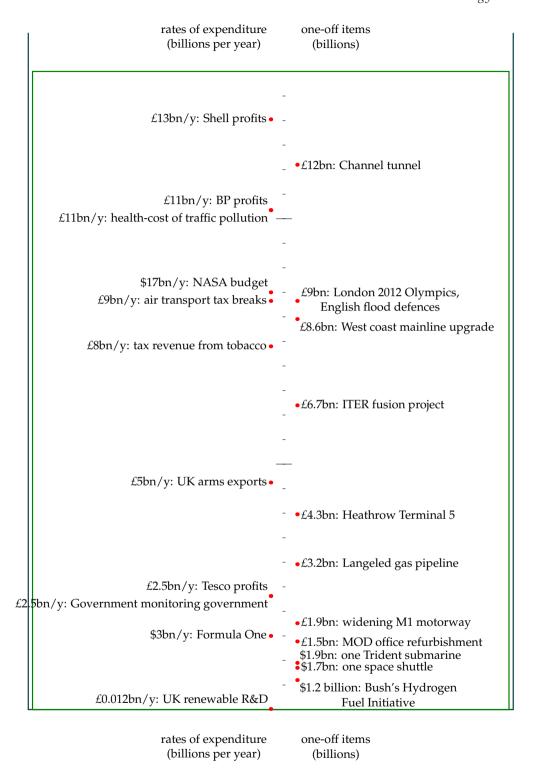


Figure 28.4. Things that run into billions. (Detail of detail.) The smallest item displayed (£0.012b/y) is the UK government's annual investment in © David JreneWaskayn Programme, Louis and Low Carbon Buildings Programme, £0.018b/y shared between wind, biomass, solar hot water/PV, ground-source heat pumps, micro-hydro and micro CHP.

\$33b/y. World expenditure on perfumes and makeup.

\$700bn per year: USA's expenditure on foreign oil (2008). (\$2300 per year per person in the USA.)

Government business as usual

£2.5b/y: cost of central government's monitoring of local government. (£42 per year per person in the UK.)

£1.5b: cost of refurbishment of Ministry of Defence offices in Whitehall. (Private Eye No. 1176, 19th January 2007, page 5.) (£25 per person in the UK.)

£1.4b: cost of new headquarters for Home Office in Marsham Street. (Private Eye No. 1176, 19th January 2007, page 5.) (£23 per person in the UK.)

£8.5 billion: cost of Allenby/Connaught redevelopment of army barracks in Aldershot and Salisbury Plain. (£140 per person in the UK.)

£15 billion – cost of introducing UK identity card scheme [7v1xp]. (£250 per person in the UK.)

£1.8 billion. Central government departments spent almost £2 billion on consultants during 2006. [2qhyw2] (£30 per person in the UK.)

Government assets

The UK government owns assets worth £337 billion. [2hddq9] (£5600 per person in the UK.)

Planning for the future

£9 billion – cost of flood defences required to protect England against 40 cm sea-level rises [324zyk]. (£150 per person in the UK.)

£3.2 billion: cost of the Langeled pipeline, which ships gas from Norwegian producers to Britain. The pipeline's capacity is 20 billion m³ per year, corresponding to a power of 25 GW(thermal). The pipeline is 1200 km long and used about one million tonnes of steel and one million tonnes of concrete [2nfp2d] [39g2wz] [3ac8sj]. (£53 per person in the UK.)

Tobacco taxes and subsidies

£11b/y: annual cost of the impact of traffic pollution on health. (£180 per year per person in the UK.)

£1.5b/y: annual cost to National Health Service of treating smoking-related diseases. (£25 per year per person in the UK.)

£8b/y: annual revenue from tobacco taxes in the UK [y7kg26]. (£130 per year per person in the UK.) The European Union spends almost €1 billion a year subsidising tobacco farming. http://www.ash.org.uk/

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

International investments

\$1.4 billion: money received in investments and contracts by the House of Bush from the House of Saud [8t7rd].

\$500 billion: Saudi royal family's investment in USA [2f3nar]. (\$1700 per person in the USA.)

Space

\$1.7 billion: Cost of one space shuttle. (\$6 per person in the USA.) \$17 billion: NASA's budget (2007) http://www.nasa.gov/about/budget/, [2gajp8]. (\$60 per person in the USA.)

Military

UK's arms exports are £5 billion per year (£83 per year per person in the UK), of which £2.5 billion go to the Middle East, and £1 billion go to Saudi Arabia. Source – Observer, 3 December 2006.

£1 billion: payments by British arms manufacturer BAE Systems to Saudi arms-deal-arranger Prince Bandar bin Sultan (relating to the Al Yamamah warplane deal in 1985, worth £43 billion.) Source: BBC News Thu 7/6/07.

Two new aircraft carriers will cost £3.8 billion. http://news.bbc.co.uk/ 1/low/scotland/6914788.stm (£63 per person in the UK.)

The Trident submarine costs about \$1.9 billion apiece (not including warheads) http://www.brook.edu/fp/projects/nucwcost/trident.htm. Replacing Trident would cost £10–25 billion [ysncks]. (£170–420 per person in the UK.)

\$46b/y: Annual cost of the USA's "War on drugs." [r9fcf] (\$150 per year per person in the USA.)

\$63 billion: American donation of "military aid" (i.e., weapons) to the Middle East over the next 10 years – roughly half to Israel, and half to Arab states. [2vq59t] (\$210 per person in the USA.)

\$200 billion: Saudi expenditure on new military bases from 1979 to 1989. [2f3nar]. (\$7600 per person in Saudia Arabia.)

World expenditure on arms: \$1.2 trillion per year (2005 estimate) [ym46a9]. (\$200 per year per person in the world.)

[99bpt] Iraq war could cost US over \$2 trillion, says Nobel prize-winning economist Joseph Stiglitz. (\$7000 per person in America.)

UK spending on wars in Iraq and Afghanistan: £8 billion.

According to the Stern review, the global cost of averting dangerous climate change (if we act now) is \$440 billion per year (\$440 per year per person, if shared equally between the 1 billion richest people). In 2005, the US government alone spent \$480 billion on wars and preparation for wars. The total military expenditure of the fifteen biggest military-spending countries was \$840 billion.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com



The cost of not making nuclear weapons

Today, the US Department of Energy's budget allocates at least \$4.5 billion per year to "stockpile stewardship" activities to maintain the nuclear stockpile *without* nuclear testing and *without* large-scale production of new weapons. (\$15 per year per person in America.)

Other projects

Channel tunnel. £12 billion. (50 km long) The average depth is 150 feet (45 m) underneath the seabed.

ITER project (fusion) £6.7 billion.

Notes and further reading

- ?? A government report leaked by the Guardian... The Guardian report, 13th August 2007, said [do me] "Government officials have secretly briefed ministers that Britain has no hope of getting remotely near the new European Union renewable energy target that Tony Blair signed up to in the spring and have suggested that they find ways of wriggling out of it." The leaked document is at [do me]
- 239 perfume... Source: Worldwatch Institute http://www.worldwatch.org/
 press/news/2004/01/07/
- 240 wars and preparation for wars www.conscienceonline.org.uk

UK R+D spend on renewables (2004–5): 39 million pounds via the research councils and 26 million from the DTI capital grant fund and \$20 million (for renewables) plus \$3.4 million for clean coal. Grant program for offshore wind (2005–2010): £107 million to support the creation of 1 GW of installed capacity.

29 What to do now

What we should do depends in part on our motivation. Recall that on p5 we discussed three motivations for getting off fossil fuels. Let's assume that we have the climate-change motivation.

We are not on track to a zero-carbon future. Long-term investment is not happening. Carbon sequestration companies are not thriving, even though the advice from climate experts and economic experts alike is that sucking carbon dioxide from thin air will very probably be necessary to avoid dangerous climate change. Carbon is not even being captured at any coal power stations.

Why not?

The principal problem is that carbon pollution is not priced correctly. And there is no confidence that it's going to be priced correctly in the future. When I say correctly, I mean that the price of carbon dioxide should be big enough such that every running coal power station has got carbon capture technology fitted to it.

Solving climate change is a complex topic, but in a single crude brush-stroke, here is the solution: the price of carbon dioxide must be such that people *stop burning coal without capture*. Most of the solution is captured in this one brush-stroke because, in the long term, coal is the big fossil fuel. Trying to reduce emissions from oil and gas is of secondary importance because supplies of both oil and gas are expected to decline over the next 50 years.

So what do politicians need to do? They need to ensure that all coal power stations have carbon capture fitted. I think the simplest way to achieve this goal is to pass a law that says that - from 2020, say - all coal power stations must use carbon capture. However, most democratic politicians seem to think that the way to close a stable door is to create a market in permits to leave doors open. So, if we conform to the dogma that climate change should be solved through markets, what's the market-based way to ensure we achieve our simple goal - all coal power stations to have carbon capture? Well, we can faff around with carbon trading - trading of permits to emit carbon and of certificates of carbon-capture, with onetonne carbon-capture certificates being convertible into one-tonne carbonemission permits. But the coal station owners will act only if they are convinced that the price of carbon is going to be high enough for long enough that their carbon-capturing facility will pay for itself. Experts say that a long-term guaranteed carbon price of something like \$100 per ton of CO₂ will do the trick.

So politicians need to modify the market so that investors have complete confidence that the price of carbon will always be at least \$100 per ton of CO₂. One way to do this would be to issue carbon pollution permits in an auction with a fixed minimum price. Another way would be for

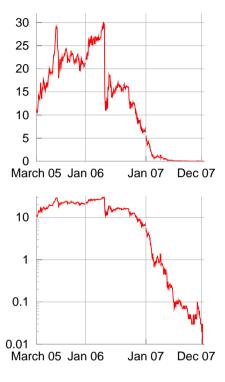


Figure 29.1. A fat lot of good that did! The price, in euro, of one ton of CO₂ under the first period of the European emissions trading scheme. Source: www.eex.com.

29 — What to do now 243

governments to underwrite investment in carbon capture by guaranteeing that they will redeem captured-carbon certificates for \$100 per ton of CO₂, whatever happens to the market in carbon-emission permits.

I still think it would be wisest to close the stable door directly, rather than fiddling with an international market that is intended to encourage stable door-closing.

Greening the tax system

"We need to profoundly revise all of our taxes and charges. The aim is to tax pollution - notably fossil fuels - more, and tax work less."

Nicolas Sarkozy

http://www.greenfiscalcommission.org.uk/

Green Fiscal Commission. "The Commission was publicly launched on 14 November 2007 and over the next year and half we will be looking in detail at the whole range of issues surrounding green taxes and environmental tax reform (ETR). The Commission's work will cover four broad areas:

- How green taxes/ ETR works.
- The environmental, economic and social implications of ETR.
- Attitudes to green taxes and ETR.
- Communication of our findings.

The focus of the Commission's work is greening the UK tax system – that is moving taxes from 'goods' like labour, to 'bads' like environmental damage. The key to a green tax shift is that it is revenue neutral – tax cuts on 'goods' must be balanced by equivalent tax increases on 'bads'.

The Commission does not have a view on what level of overall taxation is appropriate but considers that a significant shift from taxing 'goods' to 'bads' could make a important contribution to the cost-effective resolution of environmental problems.

Idea: instead of income tax, tax consumption – allows bigger multiplier on green taxes.

Even: just tax carbon, get rid of VAT and corporation taxes. (Though probably it would be a higher priority to eliminate taxes on working rather than to eliminate VAT.)

Environmental taxes are roughly 3% of GDP.

See UNITAX for example http://www.rui.co.uk/indirect/page3.html It's an Energy tax; accompanied by (to avoid regressive effects of energy taxes) a universal Basic Income. Similarly, he advocates ULAD (unified land area duty).

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

UNITAX applies a duty on all primary energy at the first point of use in any given national economy (or in any trading group of nations). All other taxes can be phased out. http://ourworld.compuserve.com/homepages/farel_bradbury/ UNITAX is based on Statutory Primary Energy Content (SPEC) of cross-frontier billings for goods and services. All exports receive a rebate based on SPEC so that indigenous industry is at no disadvantage from high primary costs.

Policies

Need to make repair, refurbishment, and recycling tax-advantageous compared with simply buying new. For example: 'no VAT on repair work'.

http://news.bbc.co.uk/1/low/business/7151862.stm EU regulations: Carmakers would have to cut average emissions of CO2 from new passenger cars sold in the EU from about 160 grams per kilometre to an average 130 grams per kilometre in 2012.

Carbon trading and taxes

Grubb and Newbery [2008] discuss the merits of taxes versus tradable quotas, arguing in favour of a stable carbon price (which would be delivered by a carbon tax); and they discuss what needs to be done to the EU emissions trading scheme to fix it.

"current instruments will not deliver an adequate investment response"

What sort of carbon price is needed

Get content from carbon.tex

And put costs in perspective

Include 'the last thing we should talk about'?

Individual lifestyle change

"a bit impractical actually"

Unless we act now, not some time distant but now, these consequences, disastrous as they are, will be irreversible. So there is nothing more serious, more urgent or more demanding of leadership.

Tony Blair, 30th October 2006

a bit impractical actually

Tony Blair,

two months later, responding to the suggestion that he should *show* leadership by not flying to Barbados for holidays.

(c) David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

29 — What to do now 245

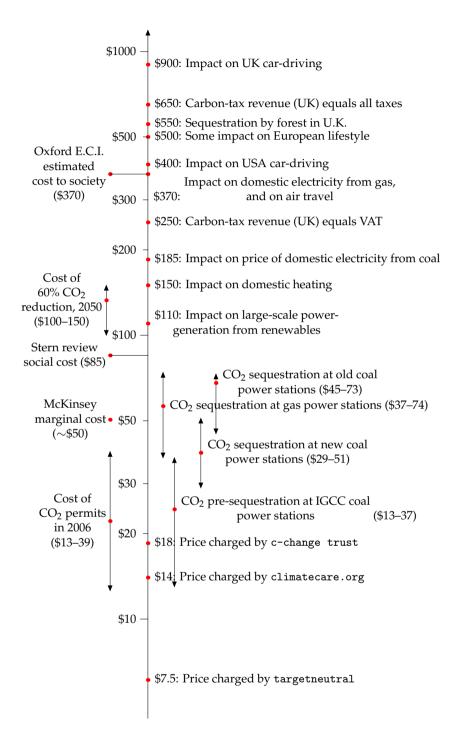


Figure 29.2. What price would CO₂ need to have in order to drive society to make significant changes in CO₂ pollution?

The diagram shows carbon dioxide costs (per tonne) at which particular actions will become economical, or particular behaviours will be economically impacted.

As the cost rises through \$20–70 per tonne, CO₂ would become sufficiently costly that it would be economical to add carbon sequestration to new and old power stations.

A price of \$110 per tonne would transform large-scale renewable electricity-generation projects that currently cost 3p per kWh more than gas from pipedreams into financially viable ventures. For example, the proposed Severn barrage would produce tidal power with a cost of 6p per kWh, which is 3.3p above a typical selling price of 2.7p per kWh; if each 1000 kWh from the barrage avoided one ton of CO₂ pollution at a value of £60 per ton, the Severn barrage would more than pay for itself.

At \$150 per tonne, domestic users of gas would notice the cost of carbon in their heating bills.

At \$370, carbon pollution would cost enough to reduce people's inclination to fly.

At \$500 per tonne, average Europeans who didn't change their lifestyle might spend 12% of income on the carbon costs of driving, flying, and heating their homes with gas. And at \$900 per tonne, the carbon cost of driving would be noticeable.

Britain's energy policy just doesn't stack up. It won't deliver security. It won't deliver on our commitments on climate change. It falls short of what the world's poorest countries need.

Lord Patten of Barnes, Chair of Oxford University task force on energy and climate change, Monday 4th June 2007.

http://news.bbc.co.uk/1/low/sci/tech/6970730.stm "Brits 'addicted' to cheap flights."

It's like converting a peacetime economy to a wartime economy.

Efficiency

Action

People sometimes ask me "What should *I* do?" This table indicates eight simple personal actions I'd recommend, and a *very* rough indication of the savings associated with each action.

Simple action	Possible saving
Put on a wooly jumper and turn down your heating's thermostat (to 15 or 17 °C, say). Put individual thermostats on all radiators. Make sure the heating's off when no-one's at home. Do the same at work.	20 kWh/d
Read all your meters (gas, electricity, water) every week, and identify easy changes to reduce consumption (e.g., switching things off). Compare competitively with a friend. Read the meters at your place of work too, creating a perpetual live energy audit.	4 kWh/d
Stop flying.	35 kWh/d
Drive less, drive slower, drive more gently, car-pool, use an electric car, join a car club, cycle, walk, use trains and buses.	20 kWh/d
Keep using old gadgets (e.g. computers); don't replace them early.	4kWh/d
Change lights to fluorescent or LED.	4 kWh/d
Don't buy clutter. Avoid packaging.	20 kWh/d
Eat vegetarian, six days out of seven	10 kWh/d

[©] David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

Whereas the above actions are easy to implement, these next ones take a bit of planning, determination, and money.

Major action	Possible saving
Eliminate draughts.	5 kWh/d
Double glazing.	10 kWh/d
Improve wall, roof, and floor insulation.	10 kWh/d
Solar hot water panels.	8 kWh/d
Photovoltaic panels.	5 kWh/d
Knock down old building and replace by new.	35 kWh/d
Replace fossil-fuel heating by ground-source or air-	10 kWh/d
source heat pumps	

Runners-up: simple actions with small savings.

Action		possible saving
Wash laundry at 30 °C. Stop using a tumble-dryer; use a clothes-line airing cupboard.	or	1.1 kWh/d 0.5 kWh/d

Notes and further reading

page no.

246 "a bit impractical actually" The full transcript of the interview with Tony Blair (January 9 2007) is here [2ykfgw]. Here are some more quotes from it.

Interviewer: "have you thought of perhaps not flying to Barbados for a holiday and not using all those air miles?"

Tony Blair: "I would frankly, be reluctant to give up my holidays abroad." Interviewer: "It would send out a clear message though wouldn't it, if we didn't see that great big air journey off to the sunshine? ... – a holiday closer to home?"

Tony Blair: "Yeah – but I personally think these things are a bit impractical actually to expect people to do that. I think that what we need to do is to look at how you make air travel more energy efficient, how you develop the new fuels that will allow us to burn less energy and emit less. How – for example – in the new frames for the aircraft, they are far more energy efficient.

"I know everyone always – people probably think the Prime Minister shouldn't go on holiday at all, but I think if what we do in this area is set people unrealistic targets, you know if we say to people we're going to cancel all the cheap air travel ... You know, I'm still waiting for the first politician who's actually running for office who's going to come out and say it – and they're not."

The other quote: "Unless we act now, not some time distant but now, these consequences, disastrous as they are, will be irreversible. So there is nothing more serious, more urgent or more demanding of leadership." is Tony Blair speaking at the launch of the Stern review, 30 October 2006 [2nsvx2]. See also [yxq5xk] for further comment.

EU Wed 23/1/08. Revenues resulting from the ETS will accrue to Member States and should be used to help the EU to adjust to an environment friendly economy by supporting innovation in areas such as renewables, carbon capture and storage and R&D. Part of the revenues should also go towards helping developing countries adapt to climate change. The Commission estimates that the revenues from the auctioning could amount to 50 billion annually by 2020.

What's needed

For long-term reduction of carbon emissions, the single most important global action is to introduce carbon capture technology everywhere where coal is used. This would happen if carbon pollution had an appropriate price.

radical fiscal reform
normative economics
political economics
get rid of taxes that penalize work and saving
get rid of deadweight costs of tax
demand-responsive road transport services are not

demand-responsive road transport services are not permitted at present. Running a bus trip because it is needed is against the law.

Society lifestyle change

Instead of planning wind farms all over Britain, would it not be better government policy to encourage people to use less electricity? Why don't they impose a massive levy on electric toothbrushes, razors, fan heaters, spin driers, and all the gadgets given out this Christmas?

Janet Street-Porter

Ideas. "Let the market handle it. Put a cap on global carbon emissions, and allow emissions credits to be traded."

Are there actions that a market solution will not promote? A market approach may fail if consumers sometimes choose irrationally, or if the person choosing what to buy doesn't pay all the costs associated with their choice.

Here are some examples.

29 — What to do now 249

The admission barrier

Imagine that carbon taxes are sufficiently high that a new super-duper low-carbon gizmo would cost 5% less than its long-standing high-carbon rival, the Dino-gizmo, *if* it were mass-produced in the same quantities. Thanks to clever technology, the Eco-gizmo's carbon emissions are a fantastic 90% lower than the Dino-gizmo's. It's clear that it would be good for society if everyone bought Eco-gizmos now. But at the moment, sales of the new Eco-gizmo are low, so the per-unit economic costs are higher than the Dino-gizmo's. Only a few tree-huggers and lab coats will buy the Eco-Gizmo, and Eco-Gizmo Inc. will quite likely go out of business.

Perhaps government interventions are necessary to oil the transition and give innovation a chance. Support for research and development? Taxincentives favouring the new product (like the tax-incentives that oiled the transition from leaded to unleaded petrol)?

Small cost differences

Imagine that Eco-Gizmo Inc. makes it from tadpole to frog, and that carbon taxes are sufficiently high that an Eco-gizmo indeed costs 5% less than its long-standing high-carbon rival from Dino-appliances, Inc. Surely the carbon taxes will now do their job, and all consumers will buy the lowcarbon gizmo? Ha! First, many consumers don't care too much about a 5% price difference. Image is everything. Second, if they feel at all threatened by the Eco-gizmo, Dino-appliances, Inc. will relaunch their Dino-gizmo, emphasizing that it's more patriotic, announcing that it's now available in green, and showing cool people sticking with the old faithful Dino-gizmo. "Real men buy Dino-gizmos." If this doesn't work, Dino will issue pressreleases saying scientists haven't ruled out the possibility that long-term use of the Eco-gizmo might cause cancer, highlighting the case of an old lady who was tripped up by an Eco-gizmo, or suggesting that Eco-gizmos harm the lesser spotted fruit bat. Fear, Uncertainty, Doubt. As a backup plan, Dino-appliances could always buy up the Eco-gizmo company. The winning product will have nothing to do with energy saving if the economic incentive to the consumer is only 5%.

Government solutions? Perhaps *extra* carbon taxes and energy taxes should be applied to consumer goods? Critics might worry that such tinkering with the market might lead to sub-optimal products succeeding. Perhaps government should simply ban the sales of the Dino-gizmo (just as government banned sales of leaded-petrol cars)?

Larry and Tina

Imagine that Larry the landlord rents out a flat to Tina the tenant. Larry is responsible for maintaining the flat and providing the appliances in it, and Tina pays the monthly heating and electricity bills. Here's the problem:

Larry feels no incentive to invest in modifications to the flat that would reduce Tina's bills. He could install more-efficient lightbulbs, and plug in a more economical fridge; these eco-friendly appliances would pay back their extra up-front cost over their long life; but it's Tina who would benefit, not Larry. Similarly, Larry feels little incentive to improve the flat's insulation or install double-glazing, especially when he takes into account the risk that Tina's boyfriend Wayne might smash one of the windows when drunk. In principle, in a perfect market, Larry and Tina would both make the "right" decisions: Larry would install all the energy-saving features, and would charge Tina a slightly higher monthly rent; Tina would recognize that the modern and well-appointed flat would be cheaper to live in and thus be happy to pay; Larry would demand an increased deposit in case of breakage of the expensive new windows; and Tina would respond rationally and banish Wayne. However, I don't think that Larry and Tina can ever deliver a perfect market. Tina is poor, so has difficulty paying large deposits. Larry strongly wishes to rent out the flat, so Tina mistrusts his assurances about the property's low energy bills, suspecting Larry of exaggeration.

It seems to me that some sort of intervention is required, to get Larry and Tina to do the right thing – for example, government could legislate a huge tax on inefficient lightbulbs; they could ban from sale all fridges that do not meet economy benchmarks; they could require all flats to meet high standards of insulation; or they could introduce a system of mandatory independent flat assessment, so that Tina could read about the flat's energy profile before renting.

Acting as if the only cost of car-driving is the petrol. Not factoring in road tax, parking charges, insurance, maintenance, and depreciation of the car.

Buying a car in a way that ignores the lifetime emissions associated with the car.

Company car. Car provided by employer.

Other society resources that are not influenced by markets

The free market isn't responsible for building roads, dedicated bus lanes, car parks, or cycle paths. But road-building and the provision of car parks and cycle paths have a significant impact on people's transport choices. Local and national governments are responsible for the crucial decisions after which energy taxes will have an effect.

Similarly, planning laws, which determine *where* homes and workplaces may be created and *how densely* houses may be packed into land have an overwhelming influence on people's future travelling behaviour. If a new town is created that has no rail station, it is unlikely that the residents

29 — What to do now 251

of that town will make long-distance journeys by rail. If housing and workplaces are more than a few miles apart, many people will insist that they have no choice but to drive to work.

Things that last 100 years

Most investors have a ten-year horizon: they want to get their money back in ten years, with interest. They thus feel little incentive to make things whose value persists for fifty or one hundred years.

Other topics

Waste incineration

Energy tax

Ensure energy use in production of goods is kept track of by some mechanism. Easiest to just use the financial market and tax energy at source. Might be more educational to have energy consumption tracked (like sales tax, value-added-tax) and added on at the shop.

[Give energy credits to everyone on a per-capita basis, i.e. a universal wage.]

Recycled materials need to be promoted. Energy tax would help.

Carbon tax

The Economist recommends a carbon tax as the primary mechanism for government support of clean energy sources. "Nuclear power's new age," The Economist, September 8th 2007.

The Conservative Party's Quality of Life Policy Group also recommends increasing environmental taxes and reducing other taxes. – "a shift from pay as earn to pay as you burn."

"Green taxes and emissions trading need not raise the overall tax burden. The principle of environmental tax reform (ETR) – whereby the revenue base is shifted away from taxes on work towards taxes on carbon and other pollutants – is a logical progression of fiscal policy. Like the market for individual products, the current tax system harks back to a time when environmental costs were not recognized. Attaching a price to environmental damage opens a door to reducing taxes on employment of capital."

"new green taxes should be replacement taxes," "shifting the tax base from 'goods' such as employment and capital, to 'bads' like pollution."

"We cannot delay while every country uses another as an excuse not to take action."

The Royal Commission also recommended that the UK should introduce a carbon tax. "It should apply upstream and cover all sectors."

Climate bonds: http://www.igreens.org.uk/climate_stability_bonds.htm 'Upstream cap and trade': http://kyoto2.org

Get rid of VAT

Either get rid of value-added tax altogether, or at least get rid of it for green services such as repair work. At present it's much cheaper to buy a new microwave, DVD player, or vacuum cleaner than to get a malfunctioning one fixed.

Committing to a low-carbon economy "will involve transcending party politics and building a cross-party consensus on a radical but realistic long-term framework for emissions reductions. In the UK, all three main political parties have already committed themselves to cutting emissions by at least 60 per cent by 2050, and a draft Climate Change Bill, the first of its kind in the world, has cross-party support."

"The scale and depth of the change which will be needed will not be easy to achieve. It will require true leadership from government."

Tax jet fuel like other fuel, or more

Building regulations

Mandate energy-efficient construction; integrated solar panels in southfacing walls, roofs, and windows; solar electricity if economical; solar water heating otherwise; electricity-powered ground-source heat pumps instead of gas-powered central heating; thick massive walls to reduce the need for summer air-conditioning. Fit electric heat pumps to buildings. (Using air as the external heat source.)

Somehow, the consumer needs to perceive the energy content of their choices

For example, holiday-makers need to feel an incentive not to roar around on jet-skis – what horrible paradise-disturbing stink-tubs! – and instead get their thrills from, say, hang-gliding, mountain-climbing, cycling, or sailing.

(Need evidence that recreation consumes a lot of energy before this rant.)

(Jet-skis use about 500 kWh per 100 km.)







Figure 29.3. "Green Dragon" – a human-powered roller coaster in North Wales. Riders walk up the hill twice and descend twice: the first descent is on a sedate inclined-plane railway which uses the riders' weight to bring the main roller coaster to the top; walking up again, they are rewarded with their second, high-speed, high-g ride.

29 — What to do now 253

Car production regulations

Once an inefficient thing is bought, it's too late. It's essential that inefficient things should not be manufactured in the first place; or, that the consumer, when buying, should feel influenced not to buy inefficient things.

Big up-front tax on cars whose efficiency is poor. (Better to have an up-front tax as well as big fuel tax because (a) a big fuel tax is only linear; we can get a bigger disincentive for gas-guzzlers by making the up-front tax steeper than linear. (b) People pay more attention to an up-front tax; it will influence their purchase decision much more.)

Packaging

Right to return packaging to vendor, who must then recycle it. – Not because the packaging itself has much embodied energy, but rather because of the extra transport costs for moving around lavishly packaged stuff.

Regulations making a difference

An airline has been flying an empty passenger plane in order to keep hold of its landing slots. "British Mediterranean Airways round-trip flights between London's Heathrow and Cardiff International have been taking off six days a week since October." The company wanted to keep the slot so that it could use them for profit in the summer [25e5rv].

Information to the user

http://news.bbc.co.uk/1/hi/sci/tech/6550361.stm

Politics, legislation

Economic incentives are not enough to bring about lifestyle change. Consumers aren't aware of all the costs – and even if they were aware of the total cost, they wouldn't respond to it. Mr. Flaccid, who's suceptible to "hard" advertisements (now removed) like the one on p??, doesn't choose a planet-wrecking car on economic grounds.

Indeed many brands are "reassuringly expensive." Consumer choice is not determined solely by price signals. Many consumers care more about image and perception and some deliberately buy expensive.

Criticism of actions so far

From the House of Lords Science and Technology Committee "Renewable Energy: Practicalities" (4th report of session 2003–04).

"The Government are implementing their renewables programme by means of the Renewables Obligation (RO). This sets rising "targets" for the amount of renewable electricity to be generated each year (currently reaching as far ahead as 2015), and forms the basis for a complex and subtle market-driven set of incentives to generators. The incentive in any one year is high until around 70 percent of the Government's "target" for renewables generation in that year has been attained, and then declines rapidly. We believe that this mechanism will in fact ensure that the Government's targets are not attained, even though offshore wind enjoys additional capital grants.

The Renewables Obligation, although described as "technology-blind" discriminates strongly in favour of generation technologies that can be brought to market within the next year or so, because the uncertainty surrounding the future value of the RO incentives means that investors look for an early return on their investment. Only wind can produce this early return. If the Government wish to achieve their renewable target of 10 percent by 2010, or to diversify the national renewable portfolio, and there are good reasons to do so, the RO will need modification in the near future.

We found almost no one outside Government who believed that the White Paper targets were likely to be achieved. This was partly for practical reasons – planning consents, availability of labour and equipment and so on – and partly as a direct consequence of the RO method of support. We judge that by 2010 the United Kingdom may have achieved 6-7 percent renewable generation.

We deplore the minimal amounts that the Government have committed to renewable-energy-related R&D (£12.2 million in 2002-03). . . . If resources other than wind are to be exploited in the United Kingdom this has to change.

We could not avoid the conclusion that the Government are not taking energy problems sufficiently seriously."

Ensuring continuity of supply: "We were told simply that market forces would solve the problem. We are not convinced and urge the Government to give these matters further consideration."

The absence of scientific understanding often leads to superficial decision-making. The 2003 energy white paper was a good example of that. I would not like publicly to call it amateurish but it did not tackle the problem in a realistic way.

Sir David King, former Chief Scientist

Our windswept island has more than enough wind, wave and tidal power potential to meet all of our energy needs many times over.

greenpeace

serving on the government's Renewables Advisory Board ... felt like

29 — What to do now 255

November 2000	"primary units" (the first 22 kWh/d) "secondary units" (the rest)	1.35 p/kWh 1.93 p/kWh
January 2007	the first 12 kWh/d the rest	5.25 p/kWh 2.94 p/kWh

Table 29.4. Domestic gas charges for British Gas customers in Cambridge, including tax.

watching several dozen episodes of Yes Minister in slow motion. I do not think this government has ever been serious about renewables

Jeremy Leggett, founder of Solarcentury

From OFGEM

In "Cutting the green customer confusion – next steps" (Appendices) from www.ofgem.gov.uk.

"There is mounting evidence that while the RO has been effective at *reducing carbon emissions* that other schemes or policies could have delivered the same (or greater) emissions reductions at lower costs. In 2006/07, the cost of carbon abatement through the RO was in the range £65-140/tCO2 depending on the fuel that is assumed to be displaced. In contrast the cost of abatement in the UK Emissions Trading Scheme is around £18/tCO2.

"There is also increasing evidence that there are more efficient and effective policy tools which can be used to encourage the *deployment of new renewables*. The European Commission compared the costs and associated effectiveness of "feed-in tariffs" to support renewables implemented in Europe with corresponding quota schemes, such as the RO. The analysis showed that the RO was the most expensive and least efficient method of support. However, it is also clear that the RO scheme's effectiveness has been hampered by the delays in planning for wind farms and transmission lines."

Variable pricing and rationing

People sometimes talk about rationing resources – for example, distributing limited "carbon emission permits" to every member of the public. Rationing can be viewed as a special case of a pricing policy that says the price you pay for fossil fuel should vary with the amount you purchase. Such pricing policies are not new. Table 29.4 shows the prices charged by British gas. A charging system that makes the first x units cheaper and subsequent units more expensive should have a somewhat similar effect to a rationing system.

"We should invest in artificial intelligence and nanotechnology; come 2080, nanorobots will be able to solve the CO_2 problem by sucking CO_2 out of thin air."

False. This is a really bad idea because, as explained in Chapter $\ref{condition}$ (p??), sucking CO_2 out of thin air has an inescapable energy cost. The energy cost of capturing CO_2 and concentrating it for storage somewhere is in fact similar to the energy released by burning the fossil fuel in the first place.

Chargers

The myth that won't die

The BBC is still banging the phone-charger drum in 2007: "turn off your TV, unplug your mobile charger and switch off lights when you leave a room" (Monday, 14 May 2007, http://news.bbc.co.uk/1/hi/uk/6653687.stm).

And on 6th June 2007, the Mayor of London launched "DIY planet repairs," a public information campaign calling on citizens to "unplug, switch off and turn down." Under the heading "Unplug," we are advised

If every London household unplugged their mobile phone chargers when not in use, we could save $31\,000$ tonnes of CO_2 and £7.75m per year.

Let's think about these numbers. London's population is about 7 million. So what this poster is really saying is that if you unplug your charger, you're saving

$$\frac{31\,000}{7\,\text{million}} = 0.004\,\text{tonnes CO}_2$$
 per year per person.

We should compare this quantity with the typical CO₂ pollution per person, which is about 10 tonnes per year. So what the Mayor is recommending is:

"Do your bit! Make a difference! Unplug the evil phone chargers, and reduce your CO_2 pollution by less than one twentieth of one per cent!"

The total of all the Mayor's recommendations, incidentally, comes to $1.6\,\mathrm{million}$ tonnes of CO_2 per year. [(Wash Low) 98,000 tonnes of CO_2 per year. (Standby Switch Off) 465,000 tonnes. (Switch Off Your Lights) 93,000 tonnes. (Unplug) 31,000 tonnes. (Turn down thermostat one degree) 837,000 tonnes. (Only Boil What You Need when making tea) 62,000 tonnes.] Which is 0.23 tonnes per year per Londoner. A 2% reduction. Go for it, London!

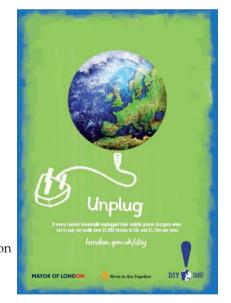


Figure 29.5. Advertisement from the 'DIY planet repairs' campaign. The text reads '**Unplug**. If every London household unplugged their mobile-phone chargers when not in use, we could save 31,000 tonnes of CO₂ and £7.75m per year'. london.gov.uk/diy/

29 — What to do now 257

On 4th July 2007, the BBC continued to promote the 'phone chargers are huge' myth: their article reports that the newest mobile phone chargers waste much less energy than their older cousins, but nevertheless, according to an expert 'a huge amount of energy was still being wasted if people were not unplugging their chargers when they were not being used'.[2wegkm]

This is a terrible abuse of the word 'huge'!

Quotes and links

Green with energy

There are many easy ways to reduce the amount of energy you use and cut fuel consumption, writes Hilary Osborne

Monday August 21, 2006

Turn off the lights

And the TV. And your mobile phone charger. These are all quick and easy ways to save energy. According to the Energy Saving Trust, if all UK households turned appliances off rather than putting them on standby it would save the energy produced by two-and-a-half 700 megawatt power stations each year.

Unplugging mobile phone chargers could save consumers £60m a year and cut CO₂ emissions by 250 000 tonnes, the Energy Saving Trust says.

60m pounds per UK is 0.03 kWh per day each. Which is 2 hundredths of 1 percent.

30 Energy plans for Europe, America, and the World

This chapter needs sorting out!

Here we discuss energy plans for Europe, for North America, and for the world. Nature magazine managed to do the whole world in 8 pages [Schiermeier et al., 2008] so why not?

The bottom line:

Europe can't live on its own renewables. So Europe needs nuclear power, or solar in other people's deserts, or both.

America's *non-solar* renewables aren't enough for America. So America needs nuclear power, or solar in its own deserts, or both.

Redoing the calculations for Europe

Can Europe live on renewables?

According to TRANS-CSP_Full_Report_Final.pdf, The European renewable energy potential is about $40\,000$ PJ/y – that is, $60\,\text{kWh/d}$ per person. Their figure 2-12 breaks down into roughly 1/4 geothermal, 1/5 CSP, 1/5 Solar thermal 1/8 biomass, 1/15 PV, 1/8 wind, 1/15 hydro.

Once you take the argument from UK self-sufficiency to the EU level, aren't things much more favourable? Lower population density and more hydro, solar etc.?

Yes, there's more hydro (in Scandanavia and Central Europe) and more solar (in Southern countries), and the population density is a little lower than the UK. But most of Europe has *less* wind, wave, and tide.

Calculation to follow.

Wind: the heart of continental europe has lower typical windspeeds than the British Isles – in much of Italy, for example, windspeeds are below $4\,\text{m/s}$. Let's guess than one fifth of Europe has big enough wind-speeds for economical windfarms, having a power density of $2\,\text{W/m}^2$, and then assume that we fill 10% of those regions with windfarms. The area of the European Union is roughly $9\,000\,\text{m}^2$ per person. So wind gives

$$0.2 \times 10\% \times 9000 \,\text{m}^2 \times 2 \,\text{W/m}^2 = 360 \,\text{W}$$
 per person

which is 9 kWh/d per person.

Hydro: Worldwide, hydroelectricity already contributes about 1.4 kWh/d/person. For many countries, hydro has significant potential.

hydroelectric production in europe totals 590 TWh/y, or 67 GW; shared between 500 million, that's 3.2 kWh/d per person. This production is dominated by Norway, France, Sweden, Italy, Austria, and Switzerland. I understand that there's little scope for further expansion of hydro in Europe. Let's imagine a 50% increase, giving 5 kWh/d per person.

Wave: Taking the whole atlantic coastline (about 4000 km) and multiplying by an assumed average production rate of 10 kW/m, we get **2 kWh/d per person**.

Tide: tripling the estimated total resource around the British Isles (14 kWh/d per person) to allow for French, Irish and Norwegian tidal resources, then sharing between a population of 500 million, we get **5 kWh/d per person**. (Too much!)

Solar PV and thermal panels: most places are sunnier than the UK, so panels would deliver more power in continental europe. $12\,\mathrm{m}^2$ of roof-mounted photovoltaic panels would deliver about $8\,\mathrm{kWh/d}$ in all places south of the UK. Similarly, $12\,\mathrm{m}^2$ of water-heating panels could deliver $20\,\mathrm{kWh/d}$ of low-grade thermal heat.

Total so far: $9+5+2+5+8 = 29 \,\text{kWh/d}$ per person. The only resources not mentioned so far are geothermal, and large-scale solar farming (with either mirrors, panels, or biomass).

Assuming an average raw power of sunshine of $90 \, \text{W/m}^2$, and that 30% of the land can be used for biomass, with 1% efficient plants – not obviously feasible! – the power arriving in the form of carbohydrate would be $60 \, \text{kWh/d}$ per person. If (with a miracle of bioengineering) this power could be processed into useful form with an efficiency of 66%, we'd end up with $40 \, \text{kWh/d/p}$.

Alternatively, use the same area $(2700 \, \text{m}^2 \, \text{per person})$ for solar PV farming, with a power density of $5 \, \text{W/m}^2$, and we'd get $320 \, \text{kWh/d/p}$. Solar PV farming would, therefore, add up to something substantial, if its cost could be got down.

Total Europe energy consumption in 2002: 1 082 mtoe. (Of which 306 industry, 338 transport, 438 other.)

Electricity: 1690 TWh/y (55% of total electricity) (and 928 PJ of heat) provided by classic thermal power stations. Nuclear 32%. Hydro 10%.

Redoing the calculations for the whole world

Do everything except solar first.

Hydro

"The IHA and the IEA estimate the world's total technical feasible hydro potential at 14 000 TWh/year (6.4 kWh/d per person), of which about 8000 TWh/year (3.6 kWh/d per person) is currently considered economically feasible for development. Most of the potential for development is in Africa, Asia and Latin America." http://www.ieahydro.org/faq.htm

Wind

It is estimated that 3% of the energy from the Sun that hits the earth is converted into wind energy.

Greenpeace and European Wind Energy Association say: Total available resources worldwide are estimated at 53 000 TWh. That's 24 kWh/d per person. That's onshore technically recoverable resource.

Some people think this figure is comforting: "It is clear that the world's wind resources are unlikely ever to be a limiting factor in the utilization of wind power for electricity production." But I'd ask, "is 24 kWh/d per person enough for what people *want*?"

Wind. $2\,\mathrm{W/m^2}$ flat ground at $v=6\,\mathrm{m/s}$. Unfortunately most of the world's land has smaller wind speeds. Exceptional spots: central states of the USA (Kansas, Oklahoma); Saskatchewan, Canada; Southern extremeties of Argentina and Chile; Northeast Autralia; Northeast and Northwest China; Northwest Sudan; Southwest South Africa; Somalia; Iran and Afghanistan. Offshore: everywhere offshore north of 30° or south of 30° is good. America offshore study: winds above $7.5\,\mathrm{m/s}$ and depth $<21\,\mathrm{m}$: area on whole East Coast is about $5000\,\mathrm{km^2}$ near Cape Cod and $15000\,\mathrm{km^2}$ down as far as North Carolina. At $3\,\mathrm{MW/km^2}$, that would offer $60\,\mathrm{GW}$. Eastern US continental shelf estimated wind power: $400\,\mathrm{GW}$. They cite a NREL report (on page 4) giving $95\,\mathrm{GW}$ estimate for using 1/3 of the area of $<30\,\mathrm{m}$ waters. They then estimate an additional $386\,\mathrm{GW}$ in deeper waters. They examine a $1.5\,\mathrm{TWh/y}$ ($170\,\mathrm{MW}$) proposal by Cape Wind Associates ($130'3.6\,\mathrm{MW'}$ machines in $62\,\mathrm{km^2}$ of Nantucket Sound.) ($2.8\,\mathrm{MW/km^2}$)

Tide

The average dissipated power globally due to tides is equal to 4 TW (Munk 1997, Egbert & Ray 2000). Kowalik [2004] He estimates that of this, 40–80 GW is tappable.

Other places in the world on the same scale as the Severn: Argentina: San José and Golfo Nuevo (two sites); Australia: Walcott Inlet; Cobequid, Canada; India: Gulf of Khambat; USA: Turnagain Arm and Knik Arm; Russia: Tugur.

USA & Canada: Bay of Fundy.

Ten times as big as the Severn: Russia: Penzhinsk (190 TWh/y, 22 GW!).

Wind again

USA wind document:

Wind energy, which produces virtually no CO₂ emissions, has been long recognized as an abundant potential source of electric power. A detailed analysis by the Department of Energy's Pacific Northwest Labora-

tory in 1991 estimated the energy potential of the U.S. wind resource at 10.8 trillion kilowatt-hours (kWh) annually, or more than three times total current U.S. electricity consumption.

Elliott et al. [1991] http://www.awea.org/policy/ccwp.html

Class 5 means power density is $400 \,\mathrm{W/m^2}$ at $30 \,\mathrm{m}$ above ground; average windspeed $7 \,\mathrm{m/s}$. About 0.6% of land area is in class 5. (Mainly in North Dakota, Wyoming and Montana.)

Taking in class 3 as well (power density 300-400 W/m² at 50 m), wind speed 6.4 m/s (5.1–5.6 m/s at 10 m), the area is 13% of the contiguous USA. Could generate over 100 quads (fossil fuel equivalent) of electricity. [570 TWh(e), 65 GW]. (I think this means raw fuel thermal energy.) With land-use restrictions, down to 47 quads.

The area for the land-use restrictions scenario is 435 thousand square kilometres.

Note they are assuming the delivered power is 1–2 W/m² in regions of class 3–6.

They converted from kWh into primary energy equivalent using 10235 btu per kWh.

total electricity consumed in 1990 was 2705 billion kWh.

ANSWER: USA, annual: 16735 TWh if no land exclusion; 4628 TWh if maximum land exclusion.

That's 1911 GW or 528 GW respectively.

Or 42 kWh/d per person (300 million people).

(153 kWh/d per person if no land exclusion).

American capacity factor: $1468\,\mathrm{MW}$ of capacity generated $2.42\,\mathrm{TWh/y}$. That's 19%.

Wave

Global coastal wave power resource estimated to be 3000 GW.

Highest wave energies are observed in the North Pacific, eastern Atlantic and southern coastlines of Australia, New Zealand, South America and Africa. Annual averages exceed 10 kW/m in nearly all areas.

For an estimate of the world coastline, use the data I used to find how many people live near sealevel. The world area within $100 \, \text{km}$ of the coast is $27.6 \, \text{million km}^2$ (20%). So the effective length of coastline is $276 \, 000 \, \text{km}$.

Multiply by 10 MW/km, get 2,760 GW.

OK, so wave power is 3000 GW, which is 0.5 kW per person, or 12 kWh/d per person if perfectly harvested.

Assuming 10% harvesting, and 50%-efficient conversion to electricity, that's 0.5 kWh/d per person.

According to some investment advisors / snake-oil salesmen, the global potential of wave power is "35 816 TW." My estimate, I remind you, was 3 TW. That is also "26 297 TWh per year". I bet the snake-oil merchants have got confused between TW and TWh/y.

Geothermal

We already estimated the world sustainable geothermal resource on p104. It's at most 10 kWh per day per person of electricity, assuming a population density of 43 people per square km (the world population density), assuming perfect heat pumps, and assuming that drilling is free; plus an equal amount of thermal power as a by-product.

In 1995, the exploitation of geothermal power was estimated to amount to on average about 4GW total, worldwide. Which is 0.01kWh/d per person.

People sometimes talk of Iceland supplying Europe's energy. The renewable reserves of Iceland (hydro and geothermal together) are estimated to be 50 000 GWh/y. That's just 5.7 GW.

Solar

Solar PV

- refer to solar.tex for projections of solar PV cost. The BP solar document says 3 TW(peak) of solar PV would reduce carbon emissions by 1 Gt C. This is said to be a plausible amount of PV in 2040.

This table was copied into solarnotes.tex:

Biomass

Arable land: 13%; permanent crops: 5%; sum = 18%. Total land area is 150 million km². All arable and crop land: 27 million km². ($4500\,\text{m}^2$ each if shared between 6 billion.) Take over all this land, and produce power at $0.5\,\text{W/m}^2$ flat ground or $0.5\,\text{MW/km}^2$: 13.5 TW. (Ignoring the energy input required.) $54\,\text{kWh/d}$ each.

"The annual global primary production of biomatter totals 220 billion oven dry tons, or 4,500 EJ. The theoretically harvestable bioenergy potential is estimated to be 2,900 EJ, of which 270 EJ could be considered technically available on a sustainable basis (Hall and Rosillo-Calle, 1998)." Rogner [2000] discuss land requirements. "Assuming a 45 percent conversion efficiency to electricity and yields of 15 oven dry tons a hectare per year, 2 square kilometres of plantation would be needed per megawatt of electricity of installed capacity running 4,000 hours a year." That is $0.23 \, \mathrm{W(e)/m^2}$. Later the same reference suggests 446 EJ per year from biomass, much of it in Latin America.

Sheffield	28%
Edinburgh	30%
Manchester	31%
Cork	32%
London	34%
Cologne	35%
Copenhagen	38%
Munich	38%
Paris	39%
Berlin	42%
Wellington, NZ	43%
Seattle	46%
Toronto	46%
Detroit, MI	54%
Winnipeg	55%
Beijing 2403	55%
Sydney 2446	56%
Pula, Croatia	57%
Nice, France	58%
Boston, MA	58%
Bangkok, Thailand	60%
Chicago	60%
New York	61%
Lisbon, Portugal	61%
Kingston, Jamaica	62%
San Antonio	62%
Seville, Spain	66%
Nairobi, Kenya	68%
Johannesburg, SA	71%
Tel Aviv	74%
Los Angeles	77%
Upington, SA	91%
Yuma, AZ	93%
Sahara Desert	98%

Table 30.1. World sunniness figures. [3doaeg]

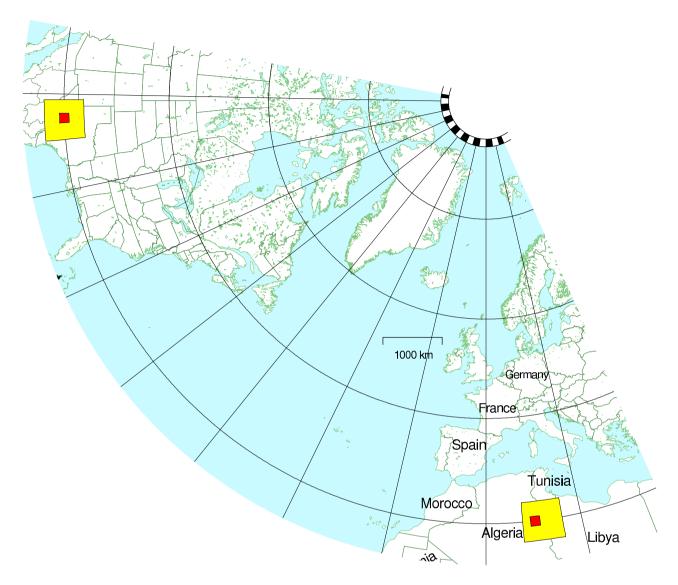


Figure 30.2. The celebrated little square strikes again. The 600 km by 600 km square in North America, completely filled with concentrating solar power, would provide enough power to give 500 million people the average American's consumption of 250 kWh/d.

This map also shows the square of size $600\,\mathrm{km}$ by $600\,\mathrm{km}$ in Africa, which we met earlier.

The area of one square is the same as the area of Germany, and 16 times the area of Wales. Or, to translate into American, it's a little bigger than the area of Arizona, and 16 times the area of New Jersey. Within each big square is a smaller 145 km by 145 km square showing the area required in the Sahara – one New Jersey – to supply 30 million people with 250 kWh per day per person.

31 The last thing we should talk about

Capturing carbon dioxide from thin air is the last thing we should talk about.

When I say this, I am deliberately expressing a double meaning. First, I think the energy requirements for carbon capture from thin air are so enormous, it seems almost absurd to talk about it. But second, I do think we should talk about it, contemplate how best to do it, and fund research into how to do it better, because capturing carbon from thin air may turn out to be our last line of defense, if humanity fails to take the cheaper and more sensible options that may still be available.

Pumping carbon out of the ground is big bucks. In the future, assuming that inadequate action is taken now, pumping carbon *into* the ground is going to be big bucks.

What's the best way to suck CO₂ from thin air?

By the laws of physics, Energy cost ≥ 0.2 kWh per kg of CO₂. So I'll be amazed if the cost is ever reduced below 0.6 kWh per kg.

Looking at the literature, Energy cost $3.3\,\mathrm{kWh}$ per kg. Plausible cost: \$140 per ton of CO_2 .

Lackner's secret technology

Wallace Broecker has been promoting the idea that 'artificial trees are the way to solve global warming'. Pushed for details, he says that 'brilliant physicist Klaus Lackner has invented a method to capture CO2 from thin air, and it doesn't require very much energy'. Broecker imagines that the world will carry on burning fossil fuels at much the same rate as it does now, and 60 million CO₂-scrubbers (each the size of an up-ended shipping container) will vacuum up the CO₂.

I think it's a very good idea to discuss capturing CO_2 from thin air, but I feel there is a problem with the way this carbon scrubbing technology is being discussed. The problem is energy: how much energy does Lackner's CO_2 -capture method require. 'Not very much'? Come on, we need numbers, not adjectives.

Here are some of the numbers required for a coherent conversation about carbon capture. Grabbing CO₂ from thin air and concentrating it into liquid CO₂ requires energy. The laws of physics say that the energy required must be at least 0.2 kWh per kg of CO₂. What does Lackner's process require? In June 2007 Lackner told me that his lab was achieving 1.3 kWh per kg. Since then, I'm sure further improvements have been made, though I haven't seen numbers published. Let's imagine that further improvements could get the energy cost down to 0.7 kWh per kg of CO₂.

Now, let's assume that we wish to neutralize a typical European's CO₂ output of 11 tons per year, which is 30 kg per day per person. The energy



required, assuming an exchange rate of $0.7 \, \text{kWh}$ per kg of CO_2 , is $21 \, \text{kWh}$ per day per person. For comparison, British electricity consumption is roughly $17 \, \text{kWh}$ per day per person.

So as a ballpark figure, the Broecker/Lackner plan requires an amount of energy equal to current electricity production.

When I call carbon capture from thin air 'the last thing we should talk about', I don't mean that we shouldn't talk about it. I definitely think we should talk about it, in detail, to help drive us towards more radical action now, to reduce the need to create these mega-vacuum-cleaners.

And if the cost of running the mega-vacuum-cleaners can be brought down, brilliant, let's make them. But no amount of research and development can get round the laws of physics, which say that grabbing CO₂ from thin air and concentrating it into liquid CO₂ requires at least 0.2 kWh per kg of CO₂.

What about trees?

Trees are carbon capturing systems; they suck CO₂ out of thin air, and they don't violate any laws of physics. They capture carbon using energy obtained from sunlight. The fossil fuels that we burn were originally created by this process. So, the suggestion is, how about trying to do the opposite of fossil fuel burning? How about creating wood and burying it in a hole in the ground, while, next door, humanity continues digging up fossil wood and setting fire to it? From the minutes of the Select Committee on Science and Technology, the best plants in Europe capture carbon at a rate of roughly 10 tons of dry wood per hectare per year. Or in equivalent CO₂ terms, that's about 15 tons of CO₂ captured per hectare per year. So the area of forest per person required to fix a European output of 11 tons of CO₂ per year is 7500 square metres per person. (And then you'd have to find somewhere to permanently store 7.5 tons of wood per year!) Taking Britain as an example European country, this required area, 7500 square metres per person, is twice the area of Britain.

Sources for numbers

Unavoidable energy requirement to compress CO_2 from 0.03% to 100% at atmospheric pressure is $kT \ln 100/0.03$ per molecule, which is 0.13 kWh per kg. (Ideal energy cost.) The ideal energy cost of compression of CO_2 to 110 bar (a standard pressure mentioned for geological storage) is 0.067 kWh/kg. So the total ideal cost of CO_2 capture and compression is 0.2 kWh/kg. Practical methods will always cost more than the ideal. According to the IPCC special report on carbon capture and storage, the practical cost of the second step, compression of CO_2 to 110 bar, is 0.11 kWh per kg. (0.4 GJ per t CO_2 ; 18 kJ per mole CO_2 ; 7 kT per molecule.)

Even if CO₂ could be *captured* for free, the *compression* cost to compress

one European's CO₂ output of 30 kg per day would be 3.3 kWh/d per person – a 20% increase in electricity production.

What's going to happen

At some point in the future, a coalition of the willing will agree to clean up everyone's mess.

Notes and further reading

At \$90/barrel, the oil industry turns overs \$2.5 trillion/y. Each barrel = $0.4 \, tCO_2$, so at \$90/barrel, people already pay \$225 to emit 1 ton CO_2 . (Of course, they are really paying for chemicals and energy, not for the right to emit.)

```
1700 kWh per barrel, so oil costs 5.4 c per kWh. 0.03% CO_2 \longrightarrow Pure \ CO_2 \longrightarrow Liquid \ CO_2 Keith et al. [2005]
```

33 Gt per year sequestration from thin air, at \$100 per ton: \$3.3 trillion per year Additional power required: 12 TW (cf world consumption = 15 TW today)

Technologies Amines? CaOH? Trees? Algae? Pumping water up from mid-ocean?

Dumping CO₂ in the deep ocean

Source: Williams [2000]. "DEEP OCEAN SEQUESTRATION OF ANTHRO-POGENIC CARBON DIOXIDE. The ocean, containing 40,000 gigatons of carbon (relative to 750 GtC in the atmosphere), represents the largest potential sink for anthropogenic CO₂; disposing in the ocean of an amount of CO₂ that would otherwise lead to a doubling of the atmosphere's content would thus increase the ocean concentration by less than 2 percent. On a 1,000-year time scale, more than 90 percent of today's anthro-pogenic emissions will be transferred to the oceans through a slow, natural process. The basic idea of ocean sequestration of CO₂ is to inject CO₂ directly into the deep ocean to accelerate this process and reduce both peak atmospheric CO₂ concentrations and their rate of increase. For a large fraction of injected CO₂ to remain in the ocean, injection must be at great depths. A consensus is developing that the best near-term strategy would be to discharge CO₂ at depths of 1000–1500 metres, which can be done with existing technology."

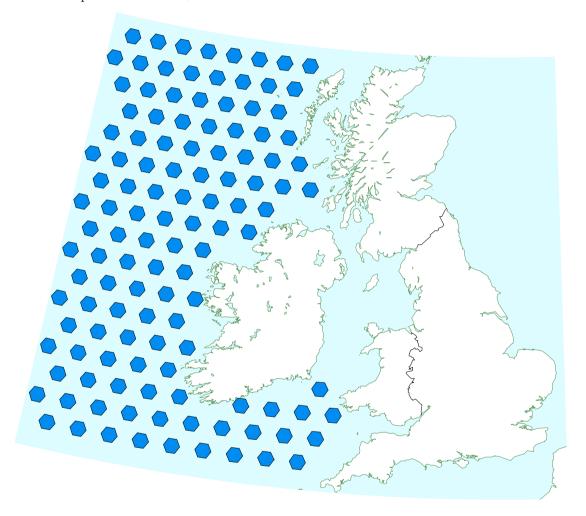
Ocean nourishment

"Extensive ocean nourishment will change both the physical and biological nature of the ocean. Increased photosynthesis in the upper ocean will

weakly change the solar absorption. A benefit of ocean nourishment is that it will enhance the fish stocks which have been seriously depleted in the last fifty years. Unlike intense agriculture, ocean nourishment, by supporting the base of the food chain, aims not to disrupt the biodiversity of the ocean."

Judd et al. [2008] claim about $30\,\mathrm{km} \times 30\,\mathrm{km}$ of ocean can be nourished (by pumping urea fertilizer) to take up $5\,\mathrm{Mt}\,\mathrm{CO}_2/\mathrm{y}$. UK carbon emissions are about $600\,\mathrm{Mt}\,\mathrm{CO}_2/\mathrm{y}$. So complete neutralization of UK carbon emissions would require 120 such areas in the ocean.

This map shows 120 areas, each 900 km².



"Commentators can be predicted to oppose manipulations of the ocean, focussing on the uncertainties rather than on the potential benefits. They will be playing to the public's fear of the unknown. People are ready to passively accept an escalation of an established practice (e.g., dumping CO_2 in the atmosphere) while being wary of innovations that might

improve their future well being. They have an uneven aversion to risk."

The Ocean Nourishment process is suitable to areas of the ocean deficient in nitrogen. That includes most of the North Atlantic. The risks of ocean nourishment are discussed in Jones [2008].

The reason I find ocean nourishment interesting is that, in contrast to geological carbon storage, it's a technology that might be implemented even if the international community doesn't agree on a high value for cleaning up carbon pollution; fishermen might implement ocean nourishment purely in order to catch more fish.

Greenfinger.

Acknowledgments

For leading me into environmentalism, I thank Robert MacKay, Gale Ryba, and Mary Archer.

For decades of intense conversation on every detail, thank you to Matthew Bramley, Mike Cates, and Tim Jervis.

For good ideas, for inspiration, for suggesting good turns of phrase, for helpful criticism, for encouragement, I thank the following people, all of whom have shaped this book. John Hopfield, Sanjoy Mahajan, Iain Murray, Ian Fells, Tony Benn, Chris Bishop, Peter Dayan, Zoubin Ghahramani, Kimber Gross, Peter Hodgson, Jeremy Lefroy, Robert MacKay, William Nuttall, Mike Sheppard, Ed Snelson, Quentin Stafford-Fraser, Prashant Vaze, Mark Warner, Seb Wills, Phil Cowans, Bart Ullstein, Helen de Mattos, Daniel Corbett, Greg McMullen, Alan Blackwell, Richard Hills, Philip Sargent, Denis Mollison, Volker Heine, Olivia Morris, Marcus Frean, Erik Winfree, Carvl Walter, Martin Hellman, Per Sillrén, Trevor Whittaker, Daniel Nocera, Jon Gibbins, Nick Butler, Sally Daultrey, Richard Friend, Guido Bombi, Alessandro Pastore, John Peacock, Carl Rasmussen, Phil C. Stuart, Adrian Wrigley, Jonathan Kimmitt, Henry Jabbour, Ian Bryden, Andrew Green, Montu Saxena, Chris Pickard, Kele Baker, Davin Yap, Martijn van Veen, Sylvia Frean, Janet Lefroy, John Hinch, James Jackson, Stephen Salter, Derek Bendall, Deep Throat, Thomas Hsu, Geoffrey Hinton, Radford Neal, Sam Roweis, John Winn, Simon Cran-McGreehin, Jackie Ford, Lord Wilson of Tillyorn, Dan Kammen, Harry Bhadeshia, Colin Humphreys, Adam Kalinowski, Anahita New, Jonathan Zwart, John Edwards, Danny Harvey, David Howarth, Andrew Read, Jenny Smithers, William Connolley, Ariane Kossack, Sylvie Marchand, Phil Hobbs, David Stern, Ryan Woodard, Noel Thompson, Matthew Turner, Frank Stajano, Stephen Stretton, Terry Barker, Jonathan Köhler, Peter Pope, Aleks Jakulin, Charles Lee, Dave Andrews, Dick Glick, Paul Robertson, Jürg Matter, Alan and Ruth Foster, David Archer, Philip Sterne, Oliver Stegle, Markus Kuhn, Keith Vertanen, Anthony Rood, Pilgrim Beart, Ellen Nisbet, Bob Flint, David Ward, Pietro Perona, Andrew Urquhart, Michael McIntyre, Andrew Blake, Anson Cheung, Daniel Wolpert, Rachel Warren, Peter Tallack, Philipp Hennig, Christian Steinrücken, Tamara Broderick, Demosthenis Pafitis, David Newbery, Annee Blott, Henry Leveson-Gower, John Colbert, Philip Dawid, Mary Waltham, Philip Slater, Christopher Hobbs, Margaret Hobbs, Paul Chambers, Michael Schlup, Fiona Harvey, Jeremy Nicholson, Ian Gardner, Sir John Sulston, Michael Fairbank, Menna Clatworthy, Gabor Csanyi, Stephen Bull, Jonathan Yates, Michael Sutherland, Michael Payne, Simon Learmount, John Riley, Lord John Browne, Cameron Freer, Parker Jones, Andrew Stobart, Peter Ravine, Anna Jones, Peter Brindle, Eoin Pierce, Willy Brown, Graham Treloar, Robin Smale, Dieter Helm, Gordon Taylor, Saul Griffith, David Cebonne, Simon Mercer, Alan Storkey, Giles Hodgson, Amos Storkey, Chris Williams, Tristan Collins, Darran Messem, Simon Singh, Gos Micklem, Peter Guthrie, Shin-Ichi Maeda, Candida Whitmill, Beatrix Schlarb-Ridley, Fabien Petitcolas, Sandy Polak, Dino Seppi, Tadashi Tokieda, Lisa Willis, Paul Weall, Hugh Hunt, Jon Fairbairn, Miloš Kojašević, Andrew Howe, Ian Leslie, Andrew Rice, Miles Hember, Hugo Willson, Win Rampen, Nigel Goddard, Richard Dietrich, Gareth Gretton, David Sterratt, Jamie Turner, Alistair Morfey, Rob Jones, Paul McKeigue, Rick Jefferys, Robin S Berlingo, Frank Kelly, Michael Kelly, Anne Miller, Malcolm Mackley, Tony Juniper, Peter Milloy, Cathy Kunkel, Tony Dye, Rob Jones, Garry Whatford, Francis Meyer, Wha-Jin Han, Brendan McNamara, Michael Laughton, Dermot McDonnell, John McCone, Andreas Kay, John McIntyre, Denis Bonnelle, Ned Ekins-Daukes, John Daglish, Jawed Karim, Tom Yates, Lucas Kruijswijk, Sheldon Greenwell, Charles Copeland, Georg Heidenreich, Colin Dunn, Steve Foale, Leo Smith, Mark McAndrew, Bengt Gustafsson, Roger Pharo, David Calderwood, Graham Pendlebury, Brian Collins, Paul Hasley, Martin Dowling, Martin Whiteland, Andrew Janca, Keith Henson, Valerie MacKay, Dewi Williams, Nick Barnes, Niall Mansfield, Graham Smith, Wade Amos, Sven Weier, Richard McMahon, Andrew Wallace, Corinne Meakins, Eoin O'Carroll, Iain McClatchie, Alexander Ac, Mark Suthers, Gustav Grob, Ibrahim Dincer, Ian Jones, Adnan Midilli, Chul Park, David Gelder, Damon Hart-Davis, George Wallis, Philipp Spöth, James Wimberley, Richard Madeley, Jeremy Leggett, Michael Meacher, Dan Kelley, Tony Ward-Holmes, Charles Barton, James Wimberley, Jay Mucha, Johan Simu, Stuart Lawrence, Nathaniel Taylor, Dickon Pinner, Michael Davey, Michael Riedel, William Stoett, Jon Hilton, Mike Armstrong, Tony Hamilton, Joe Burlington, David Howey, Jim Brough, Mark Lynas, . Thank you all.

For help with finding climate change data, I thank Emily Shuckburgh. I'm very grateful to Kele Baker for gathering the electric car data in figure 20.21. I also thank David Sterratt for research contributions, and Niall Mansfield and Jonathan Zwart for excellent editorial advice.

The errors that remain are of course my own.

I am especially indebted to Seb Wills, Phil Cowans, Oliver Stegle, Patrick Welche, and Carl Scheffler for keeping my computers working.

I thank the African Institute for Mathematical Sciences, Cape Town, and the Isaac Newton Institute for Mathematical Sciences, Cambridge, for hospitality.

The data source for figures showing greenhouse gas emissions was the Climate Analysis Indicators Tool (CAIT) Version 4.0. (Washington, DC: World Resources Institute, 2007). Many thanks to the Digital Technology Group, Computer Laboratory, Cambridge and Heriot–Watt University Physics Department for providing weather data online. I am grateful to Jersey Water and Guernsey Electricity for tours of their facilities.

Thank you to Gilby Productions for providing the TinyURL service. TinyURL is a trademark of Gilby Productions. Thank you to Eric Johnston and Satellite Signals Limited for providing a nice interface for maps [www.satsig.net].

Thank you to David Stern for the author portrait, to Becky Smith for artwork, and to Claire Jervis for the black-and-white photos on pages iii, 33, 161, 102, 348, 120, and 308. For other photos, thanks too to Robert MacKay, Marcus Frean, Rosie Ward, Harry Bhadeshia, Catherine Huang, Yaan de Carlan, Pippa Swannell, Corinne Le Quéré, David Faiman, Tim Jervis, and anonymous contributors to Wikipedia. I am grateful to the office of the Mayor of London for providing copies of advertisements.

The artwork on page 264 is "Maid in London" by Banksy http://www.banksy.co.uk/; and on page 53, "Sunflowers" also by Banksy. Thank you, Banksy!

This book is written in LATEX on the ubuntu GNU/Linux operating system using free software. The figures were drawn with gnuplot and metapost. Many of the maps were created with Paul Wessel and Walter Smith's gmt. Thank you also to Martin Weinelt and OMC. Thank you to Donald Knuth, Leslie Lamport, Richard Stallman, Linus Torvalds, and all those who contribute to free software.

Finally I owe the biggest debt of gratitude to the Gatsby Charitable Foundation, who supported me and my research group before, during, and after the writing of this book.

Part III Technical chapters

A Cars II

We estimated that a car driven 100 km uses about 80 kWh of energy.

Where does this energy go? How does it depend on properties of the car? Could we make cars that are 100 times more efficient? Let's make a simple cartoon of car-driving, to describe where the energy goes. The energy in a typical fossil-fuel car goes to four main destinations, all of which we will now explore:

- 1. speeding up then slowing down using the brakes
- 2. air resistance
- 3. rolling resistance
- 4. heat 75% of the energy is thrown away as heat, because the energy-conversion chain is inefficient.

Initially our cartoon will ignore rolling resistance; we'll add this effect in later in the chapter.

Assume the driver accelerates rapidly up to a cruising speed v, and maintains that speed for a distance d, which is the distance between traffic lights or stop signs or congestion events. At this point, he slams on the brakes and turns all his kinetic energy into heat in the brakes (this vehicle doesn't have fancy regenerative braking). Once he's able to move again, he accelerates back up to his cruising speed, v. This acceleration gives the car kinetic energy; braking throws that kinetic energy away.

Energy goes not only into the brakes: while the car is moving, it makes air swirl around. A car leaves behind it a tube of swirling air, moving at a speed similar to v. Which of these two forms of energy is the bigger: kinetic energy of the swirling air, or heat in the brakes? Let's work it out.

• The car speeds up and slows down once in each duration d/v. The rate at which energy pours into the brakes is:

$$\frac{\text{kinetic energy}}{\text{time between braking events}} = \frac{\frac{1}{2}m_{\text{c}}v^2}{d/v} = \frac{\frac{1}{2}m_{\text{c}}v^3}{d}, \quad (A.1)$$

where m_c is the mass of the car.





Figure A.1. A Peugot 206 has a drag coefficient of 0.33. Photo by Christopher Batt.

The key formula for most of the calculations in this book is:

kinetic energy =
$$\frac{1}{2}mv^2$$
.

For example, a car of mass m=1000 kg moving at 100 km per hour or v=28 m/s has an energy of

$$\frac{1}{2}mv^2 = 390\,000\,\mathrm{J} \simeq 0.1\,\mathrm{kWh}.$$

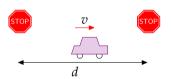


Figure A.2. Our cartoon: a car moves at speed v between stops separated by a distance d.

Figure A.3. A car moving at speed v creates behind it a tube of swirling air; the cross-sectional area of the tube is similar to the frontal area of the car, and the speed at which air in the tube swirls is roughly v.

A — Cars II 273

• The tube of air created in a time t has a volume Avt, where A is the cross-sectional area of the tube, which is similar to the area of the front view of the car. (For a streamlined car, A is usually a little smaller than the frontal area $A_{\rm car}$, and the ratio of the tube's effective cross-sectional area to the car area is called the drag coefficient $c_{\rm d}$. Throughout the following equations, A means the effective area of the car, $c_{\rm d}A_{\rm car}$.) The tube has mass $m_{\rm air} = \rho Avt$ (where ρ is the density of air) and swirls at speed v, so its kinetic energy is:

$$\frac{1}{2}m_{\rm air}v^2 = \frac{1}{2}\rho Avt\,v^2,$$

and the rate of generation of kinetic energy in swirling air is

$$\frac{\frac{1}{2}\rho Avtv^2}{t} = \frac{1}{2}\rho Av^3.$$

So the total rate of energy production by the car is:

power going into brakes + power going into swirling air =
$$\frac{1}{2}m_c v^3/d$$
 + $\frac{1}{2}\rho A v^3$.

Both forms of energy dissipation scale as v^3 . So this cartoon predicts that a driver who halves his speed v makes his power consumption 8 times smaller. If he ends up driving the same total distance, his journey will take twice as long, and the total energy consumed by his journey will be four times smaller.

Which of the two forms of energy dissipation – brakes or air-swirling – is the bigger? It depends on the ratio of

$$(m_{\rm c}/d)/(\rho A)$$
.

If this ratio is much bigger than 1, then more power is going into brakes; if it is smaller, more power is going into swirling air. Rearranging this ratio, it is bigger than 1 if

$$m_{\rm c} > \rho Ad$$
.

Now, Ad is the volume of the tube of air swept out from one stop sign to the next. And ρAd is the mass of that tube of air. So we have a very simple situation: energy dissipation is dominated by kinetic-energy-being-dumped-into-the-brakes if the mass of the car is *bigger* than the mass of the tube of air from one stop sign to the next; and energy dissipation is dominated by making-air-swirl if the mass of the car is *smaller* (figure A.4).

Let's work out the special distance d^* between stop signs, below which the dissipation is braking-dominated and above which it is air-swirling dominated (also known as drag-dominated). If the frontal area of the car is:

$$A_{\rm car} = 2 \,\mathrm{m}\,\mathrm{wide} \times 1.5 \,\mathrm{m}\,\mathrm{high} = 3 \,\mathrm{m}^2$$

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

I'm using this formula:

 $mass = density \times volume$

The symbol ρ ("rho") denotes the density.

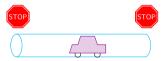


Figure A.4. To know whether energy consumption is braking-dominated or air-swirling-dominated, we compare the mass of the car with the mass of the tube of air between stop-signs.



Figure A.5. Power consumed by a car is proportional to its cross-sectional area, during motorway driving, and to its mass, during town driving. Guess which gets better mileage – the VW on the left, or the spaceship?

and the drag coefficient is $c_d = 1/3$ and its mass is $m_c = 1000$ kg then the special distance is:

$$d^* = \frac{m_c}{\rho c_d A_{car}} = \frac{1000 \text{ kg}}{1.3 \text{ kg/m}^3 \times \frac{1}{3} \times 3 \text{ m}^2} = 750 \text{ m}.$$

So "city-driving" is dominated by kinetic energy and braking if the distance between stops is less than 750 m. Under these conditions, it's a good idea, if you want to save energy:

- 1. to reduce the mass of your car;
- 2. to get a car with regenerative brakes (which roughly halve the energy lost in braking see Chapter 20); and
- 3. to drive more slowly.

When the stops are significantly more than 750 m apart, energy dissipation is drag-dominated. Under these conditions, it doesn't much matter what your car weighs. Energy dissipation will be much the same whether the car contains one person or six. Energy dissipation can be reduced:

- 1. by reducing the car's drag coefficient;
- 2. by reducing its cross-sectional area; or
- 3. by driving more slowly.

The actual energy consumption of the car will be the energy dissipation estimated above, cranked up by a factor related to the inefficiency of the engine and the transmission. Typical petrol engines are about 25% efficient, so of the chemical energy that a car guzzles, three quarters is wasted in making the car's engine and radiator hot, and just one quarter goes into 'useful' energy:

total power of car
$$\simeq 4\left[\frac{1}{2}m_{\rm c}v^3/d + \frac{1}{2}\rho Av^3\right]$$
.

Let's check this theory of cars by plugging in plausible numbers for motorway driving. Let $v=70\,\mathrm{miles}\,\mathrm{per}\,\mathrm{hour}=110\,\mathrm{km/h}=31\,\mathrm{m/s}$ and $A=c_\mathrm{d}A_\mathrm{car}=1\,\mathrm{m}^2$. The power is estimated to be roughly

$$4 \times \frac{1}{2} \rho A v^3 = 2 \times 1.3 \,\text{kg/m}^3 \times 1 \,\text{m}^2 \times (31 \,\text{m/s})^3 = 80 \,\text{kW}.$$

If you drive the car at this speed for one hour every day, then you travel 110 km and use 80 kWh of energy per day. If you drove at half this speed for two hours per day instead, you would travel the same distance and use up 20 kWh of energy. This simple theory seems consistent with the mileage figures for cars quoted in Chapter 3. Moreover, the theory gives

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

at $110 \,\mathrm{km/h} \stackrel{\longleftrightarrow}{\leftrightarrow} 80 \,\mathrm{kWh/(100 \,km)}$ Bicycle at $21 \,\mathrm{km/h} \stackrel{\longleftrightarrow}{\leftrightarrow} 2.4 \,\mathrm{kWh/(100 \,km)}$

Planes at 900 km/h

A380 27 kWh/100 seat-km

Table A.6. Facts worth remembering: car energy consumption.

insight into how the energy consumed by your car could be reduced. The theory has a couple of flaws which we'll explore in a moment.

Could we make a new car that consumes 100 times less energy and still goes at 70 mph? **No**. Not if the car has the same shape. On the motorway at 70 mph, the energy is going mainly into making air swirl. Changing the materials the car is made from makes no difference to that. A miraculous improvement to the fossil-fuel engine could perhaps boost its efficiency from 25% to 50%, bringing the energy consumption of a fossil-fuelled car down to roughly 40 kWh per 100 km.

Electric vehicles have some wins: while the weight of the energy store, per kWh stored, is bigger than that of petrol, the weight of an electric engine can be smaller. And the energy-chain in an electric car is much more efficient: electric motors can be 90% efficient.

Storage: energy content of petrol: 12.5 kWh/kg of which roughly 25% gets turned into useful work, so the useful energy density is 3.7 kWh/kg. Lithium-ion polymer (LiPo) rechargeable cells: storage capacity is 0.15 kWh/kg (1/25 of net petrol) and these cells can deliver their energy at a maximum rate of 1000 W per kg.

Engine power: a 4-stroke petrol aero-engine power rating delivers roughly 0.75 kW/kg. The best electric motors have an efficiency of 90% and a power rating of 6 kW/kg. A 75 kW electric motor saves 85 kg in weight.

We'll come back to electric cars in more detail towards the end of this chapter.

Bicycles and the scaling trick

Here's a fun question: what's the energy consumption of a bicycle, in kWh per 100 km? Pushing yourself along on a bicycle requires energy for the same reason as a car: you're making air swirl around. Now, we could do all the calculations from scratch, replacing car-numbers by bike-numbers. But there's a simple trick we can use to get the answer for the bike from the answer for the car. The energy consumed by a car, per distance travelled, is the power-consumption associated with air-swirling,

$$4 \times \frac{1}{2} \rho A v^3$$
,

divided by the speed, v; that is,

energy per distance
$$= 4 \times \frac{1}{2} \rho A v^2$$
.

The "4" came from engine inefficiency; ρ is the density of air; the area A is the effective frontal area of a car; and v is its speed.

Now, we can compare a bicycle with a car by dividing $4 \times \frac{1}{2}\rho Av^2$ for the bicycle by $4 \times \frac{1}{2}\rho Av^2$ for the car. All the fractions and ρ s cancel, if

CARS Honda Insight 0.25 Prius 0.26 Renault 25 0.28 Honda Civic (2006) 0.31 VW Polo GTi 0.32 Peugeot 206 0.33 Ford Sierra 0.34 Audi TT 0.35 Honda Civic (2001) 0.36 Citroën 2CV 0.51 Cyclist 0.9 Long-distance coach 0.425 PLANES Cessna Cessna 0.027 Learjet 0.022 Boeing 747 0.031	Drag coefficients	
Prius 0.26 Renault 25 0.28 Honda Civic (2006) 0.31 VW Polo GTi 0.32 Peugeot 206 0.33 Ford Sierra 0.34 Audi TT 0.35 Honda Civic (2001) 0.36 Citroën 2CV 0.51 Cyclist 0.9 Long-distance coach 0.425 PLANES Cessna 0.027 Learjet 0.022	Cars	
Renault 25 0.28 Honda Civic (2006) 0.31 VW Polo GTi 0.32 Peugeot 206 0.33 Ford Sierra 0.34 Audi TT 0.35 Honda Civic (2001) 0.36 Citroën 2CV 0.51 Cyclist 0.9 Long-distance coach 0.425 PLANES Cessna 0.027 Learjet 0.022	Honda Insight	0.25
Honda Civic (2006) 0.31 VW Polo GTi 0.32 Peugeot 206 0.33 Ford Sierra 0.34 Audi TT 0.35 Honda Civic (2001) 0.36 Citroën 2CV 0.51 Cyclist 0.9 Long-distance coach 0.425 PLANES Cessna 0.027 Learjet 0.022	Prius	0.26
VW Polo GTi 0.32 Peugeot 206 0.33 Ford Sierra 0.34 Audi TT 0.35 Honda Civic (2001) 0.36 Citroën 2CV 0.51 Cyclist 0.9 Long-distance coach 0.425 PLANES Cessna 0.027 Learjet 0.022	Renault 25	0.28
Peugeot 206 0.33 Ford Sierra 0.34 Audi TT 0.35 Honda Civic (2001) 0.36 Citroën 2CV 0.51 Cyclist 0.9 Long-distance coach 0.425 PLANES Cessna 0.027 Learjet 0.022	Honda Civic (2006)	0.31
Ford Sierra 0.34 Audi TT 0.35 Honda Civic (2001) 0.36 Citroën 2CV 0.51 Cyclist 0.9 Long-distance coach 0.425 PLANES 0.027 Learjet 0.022	VW Polo GTi	0.32
Audi TT 0.35 Honda Civic (2001) 0.36 Citroën 2CV 0.51 Cyclist 0.9 Long-distance coach 0.425 PLANES 0.027 Cessna 0.022 Learjet 0.022	Peugeot 206	0.33
Honda Civic (2001) 0.36 Citroën 2CV 0.51 Cyclist 0.9 Long-distance coach 0.425 PLANES Cessna 0.027 Learjet 0.022	Ford Sierra	0.34
Citroën 2CV 0.51 Cyclist 0.9 Long-distance coach 0.425 PLANES Cessna 0.027 Learjet 0.022	Audi TT	0.35
Cyclist 0.9 Long-distance coach 0.425 PLANES Cessna 0.027 Learjet 0.022	Honda Civic (2001)	0.36
Long-distance coach 0.425 PLANES Cessna 0.027 Learjet 0.022	Citroën 2CV	0.51
PLANES Cessna 0.027 Learjet 0.022	Cyclist	0.9
Cessna 0.027 Learjet 0.022	Long-distance coach	0.425
Learjet 0.022	Planes	
	Cessna	0.027
Boeing 747 0.031	Learjet	0.022
	Boeing 747	0.031

Drag-areas (m ²)		
Land Rover Discovery	1.6	
Volvo 740	0.81	
Typical car	0.8	
Honda Civic	0.68	
VW Polo GTi	0.65	
Honda Insight	0.47	

Table A.7. Drag coefficients and drag areas.

wheel	$C_{\rm rr}$
train (steel on steel)	0.002
bicycle tyre	0.005
truck rubber tyres	0.007
car rubber tyres	0.010

Table A.8. Rolling resistance – The rolling resistance is equal to the weight multiplied by the coefficient of rolling resistance, $C_{\rm rr}$. The rolling resistance includes the force due to wheel flex, friction losses in the wheel bearings, shaking and vibration of both the roadbed and the vehicle (including energy absorbed by the vehicle's shock absorbers), and sliding of the wheels on the road or rail. The coefficient varies with the quality of the road, with the material the wheel is made from, and with temperature. The numbers given here assume smooth roads. [2bhu35]

the efficiency of the carbon-powered bicyclist's engine is similar to the efficiency of the carbon-powered car engine (which it is). The ratio is:

$$\frac{\text{energy per distance of bike}}{\text{energy per distance of car}} = \frac{c_{\rm d}^{\rm bike} A_{\rm bike} v_{\rm bike}^2}{c_{\rm d}^{\rm car} A_{\rm car} v_{\rm car}^2}.$$

The trick we are using is called 'scaling'. If we know how energy consumption scales with speed and area, then we can predict energy consumption of objects with completely different speeds and areas. Specifically, let's assume that the area ratio is

$$\frac{A_{\text{bike}}}{A_{\text{car}}} = \frac{1}{4}.$$

(Four cyclists can sit shoulder to shoulder in the width of one car.) Let's assume the bike is not very well streamlined:

$$\frac{c_{\rm d}^{\rm bike}}{c_{\rm d}^{\rm car}} = \frac{1}{1/3}$$

And let's assume the speed of the bike is 21 km/h (13 miles per hour), so

$$\frac{v_{\text{bike}}}{v_{\text{car}}} = \frac{1}{5}.$$

Then

$$\frac{\text{energy-per-distance of bike}}{\text{energy-per-distance of car}} = \left(\frac{c_{\text{d}}^{\text{bike}}}{c_{\text{d}}^{\text{car}}} \frac{A_{\text{bike}}}{A_{\text{car}}}\right) \left(\frac{v_{\text{bike}}}{v_{\text{car}}}\right)^{2}$$

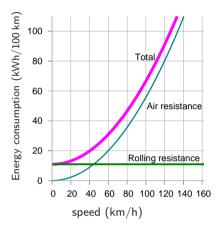
$$= \left(\frac{3}{4}\right) \times \left(\frac{1}{5}\right)^{2}$$

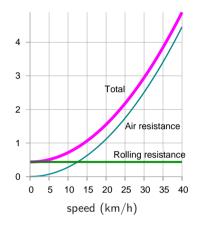
$$= \frac{3}{100}$$

So a cyclist at 21 km/h consumes about 30 times less energy per kilometre than a lone car-driver on the motorway – about **2.4 kWh per 100 km**.

If you would like a vehicle whose fuel efficiency is thirty times better than a car's, it's simple: ride a well-streamlined bike.

A — Cars II 277





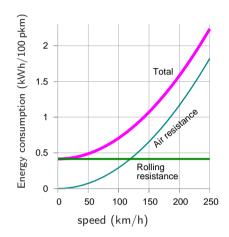


Figure A.9. Simple theory of car fuel consumption (energy per distance). Vertical axis is fuel consumption in kWh per $100 \,\mathrm{km}$. Assuming that the car's engine uses energy with an efficiency of 0.25, whatever the speed; that the drag-area of the car is $1 \,\mathrm{m}^2$; that the car's mass is $1000 \,\mathrm{kg}$, and that $C_{\mathrm{rr}} = 0.01$, the air resistance has an energy demand that grows as the square of the speed, and the rolling resistance makes a constant energy demand, whatever the speed.

Figure A.10. Simple theory of bike fuel consumption (energy per distance). Vertical axis is fuel consumption in kWh per 100 km. Assumption: the bike's engine (that's you!) uses energy with an efficiency of 0.25, whatever the speed; the drag-area of the cyclist is 0.5 m^2 ; that the cyclist+bike's mass is 80 kg; and $C_{\text{rr}} = 0.005$.

Figure A.11. Simple theory of train energy consumption, *per passenger*, for an eight-carriage train carrying 584 passengers. Horizontal axis is speed in km/h. Vertical axis is energy consumption in kWh per 100 p-km. Assumptions: the train's engine uses energy with an efficiency of 0.90; the drag-area of the train is $11\,\mathrm{m}^2$; its mass is $400\,000\,\mathrm{kg}$, and $C_{\mathrm{rr}}=0.002$.

Queries

What about rolling resistance?

Some things we've completely ignored so far are the energy consumed in the tyres and bearings of the car, the energy that goes into the noise of wheels against asphalt, the energy that goes into grinding rubber off the tyres, and the energy that vehicles put into shaking the ground. Collectively, these forms of energy consumption are called *rolling resistance*. The standard model of rolling resistance asserts that the force of rolling resistance is simply proportional to the weight of the vehicle, independent of the speed. The constant of proportionality is called the coefficient of rolling resistance, $C_{\rm rr}$. Table A.8 gives some typical values.

The coefficient of rolling resistance for a car is about 0.01. The effect of rolling resistance is just like perpetually driving up a hill with a slope of one in a hundred. If set moving, a car will roll at steady speed down a hill with a slope of one in a hundred. So rolling friction is about 100 newtons per ton, independent of speed. You can confirm this by pushing a typical one-ton car along a flat road. Once you've got it moving, you'll find you can keep it moving with one hand. So at a speed of 31 m/s (70 mph), the power required to overcome rolling resistance, for a one-ton vehicle, is

force
$$\times$$
 velocity = $(100 \text{ newtons}) \times (31 \text{ m/s}) = 3100 \text{ W}$;

which, allowing for an engine efficiency of 25%, requires 12 kW of engine power; whereas the power required to overcome drag was estimated on p274 to be 80 kW. So, at high speed, about 15% of the power is required for rolling resistance.

Figure A.9 shows the theory of fuel consumption (energy per unit distance) as a function of steady speed, when we add together the formulae for air resistance and rolling resistance.

The speed at which a car's rolling resistance is equal to air resistance is given by

$$C_{\rm rr}m_{\rm c}g=\frac{1}{2}\rho c_{\rm d}Av^2,$$

that is,

$$v = \sqrt{2 \frac{C_{\rm rr} m_{\rm c} g}{\rho c_{\rm d} A}} = 7 \,\mathrm{m/s} = 16 \,\mathrm{miles} \;\mathrm{per} \;\mathrm{hour}$$

At 32 mph, one fifth of the power is required for rolling resistance. At 48 mph, one tenth.

Bicycles

For a bicycle (m = 90 kg, $A = 0.75 \text{ m}^2$), the transition from rolling-resistance-dominated cycling to air-resistance-dominated cycling takes place at a speed of about 12 km/h. At a speed of 20 km/h, cycling costs about 1.6 kWh per 100 km.

A — Cars II 279

Trains

For an eight-carriage train as depicted in figure 20.4 ($m = 400\,000\,\text{kg}$, $A = 11\,\text{m}^2$), the speed above which air resistance is greater than rolling resistance is:

$$v = 33 \,\mathrm{m/s} = 74 \,\mathrm{miles}$$
 per hour.

For a single-carriage train ($m = 50\,000$ kg, $A = 11\,\text{m}^2$), the speed above which air resistance is greater than rolling resistance is:

$$v = 12 \,\mathrm{m/s} = 26 \,\mathrm{miles}$$
 per hour.

Dependence of power on speed

When I say that halving your driving speed should reduce fuel consumption (in miles per gallon) to one quarter of current levels, some people feel sceptical. They have a point: most cars' engines have an optimum revolution rate, and the choice of gears of the car determines a range of speeds at which the optimum engine efficiency can be delivered. My tacit assumption that the engine's efficiency is the same at all speeds and all loads led to the conclusion that it's always good (in terms of miles per gallon) to travel slower; but if the engine's efficiency drops off at low speeds, then the most fuel-efficient speed might be large. For a BMW 318ti, for example, the optimum speed is about 60 km/h (figure A.12). If my suggested experiment of halving the car's speed takes the car out of this designed range of speeds, the consumption might not fall by as much as four-fold. But if society were to decide that car speeds should be reduced, there is nothing to stop engines and gears being redesigned so that the peak engine efficiency was found at the right speed. As further evidence that the power a car requires really does increase as the cube of speed, figure A.13 shows the engine power versus the top speeds of a range of cars. The line shows the relationship "power proportional to v^3 ."

What about the energy-cost of making the car?

Good question! The creation of steel uses about 6000 kWh per ton of steel. The energy cost of making the raw materials for a one ton car is thus equivalent to about 3000 km of driving; an appreciable cost, but probably only 1% of the lifetime energy-cost of the car's fuel.

Electric cars: is range a problem?

People often say that the range of electric cars is not big enough. Electric car advocates say 'no problem, we can just put in more batteries' – and that's true, but we need to work out what effect the extra batteries have on the energy consumption. The answer depends sensitively on what energy

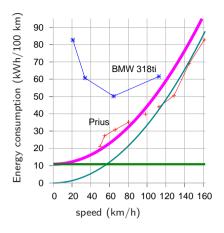


Figure A.12. Current cars' fuel consumptions do not vary as speed squared. Vertical axis: Energy consumption in kWh per 100 km. Horizontal axis: Speed in km/h. Prius data from B.Z. Wilson; BMW data from Phil C. Stuart. The smooth curve shows what a speed-squared curve would look like, assuming a drag-area of 0.6 m².

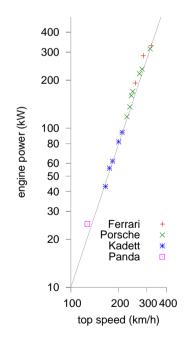


Figure A.13. Powers of cars (kW) versus their top speeds (km/h). The power increases as the third power of the speed. To go twice as fast requires eight times as much engine power. From Tennekes [1997].

density we assume the batteries deliver: for an energy density of 40 Wh/kg (typical of lead-acid batteries), we'll see that it's hard to push the range beyond 200 or 300 km; but for an energy density of 120 Wh/kg (typical of various lithium-based batteries), a range of 500 km is easily achievable.

So, let's work out what our cartoon says about the range of an electric car. Let's assume that the mass of the car and occupants is 740 kg, without any batteries. In due course we'll add 100 kg, 200 kg, 500 kg, or perhaps 1000 kg of batteries. Let's assume a typical speed of 50 km/h (30 mph); a drag-area of 0.8 m²; a rolling resistance of 0.01; a distance between stops of 500 m; an engine efficiency of 85%; and that during stops and starts, regenerative braking recovers half of the kinetic energy of the car. Charging up the car from the mains is assumed to be 85% efficient. Figure A.14 shows the transport cost of the car versus its range, as we vary the amount of battery on board. The upper curve shows the result for a battery whose energy density is 40 Wh/kg (old-style lead-acid batteries). The range is limited by a wall at about 500 km. To get close to this maximum range, we have to take along comically large batteries: for a range of 400 km, for example, 2000 kg of batteries are required, and the transport cost is above 25 kWh per 100 km. If we are content with a range of 180 km, however, we can get by with 500 kg of batteries. Things get much better when we switch to lighter lithium-ion batteries. At an energy density of 120 Wh/kg, electric cars with 500 kg of batteries can easily deliver a range of 500 km. The transport cost is predicted to be about 13 kWh per 100 km.

It thus seems to me that the range problem has been solved by the advent of modern batteries. It would be nice to have even better batteries, but an energy density of 120 Wh per kg is already good enough, as long as we're happy for the batteries in a car to weigh up to 500 kg. In practice I imagine most people would be content to have a range of 300 km, which can be delivered by 250 kg of batteries. If these batteries were divided into ten 25 kg chunks, separately unpluggable, then a car user could keep just four of the ten chunks on board when he's doing regular commuting (100 kg gives a range of 140 km); and collect an extra six chunks from a battery-recharging station when he wants to make longer-range trips. During long-range trips, he would exchange his batteries for a fresh set at a battery-exchange station every 300 km or so.

Notes

page no.

274 Typical petrol engines are about 25% efficient. Encarta [6by8x] says "The efficiencies of good modern Otto-cycle engines range between 20 and 25 percent". The petrol engine of a Toyota Prius, famously one of the most efficient car engines, uses the Atkinson cycle instead of the Otto cycle; it has a peak power output of 52 kW and has an efficiency of 34% when delivering 10 kW [348whs]. The most efficient diesel engine in the

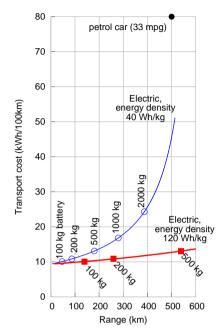


Figure A.14. Theory of electric car range (horizontal axis) and transport cost (vertical axis) as a function of battery mass, for two battery technologies. A car with 500 kg of old batteries, with an energy density of 40 Wh per kg, has a range of 180 km. With the same weight of modern batteries, delivering 120 Wh per kg, an electric car can have a range of more than 500 km. Both cars would have an energy cost of about 13 kWh per 100 km. These numbers allow for a battery charging efficiency of 85%.

- world is52%-efficient, but it's not suitable for cars as it weighs 2300 tons: the Wartsila-Sulzer RTA96-C turbocharged two-stroke diesel engine is intended for container ships and has a power output of 80 MW.
- 274 Regenerative brakes roughly halve the energy lost in braking. Source: E4tech [2007].
- 277 The bike's engine uses energy with an efficiency of 0.25. This and the other assumptions about cycling are confirmed by di Prampero et al. [1979]. The drag-area of a cyclist in racing posture is $c_d A = 0.3 \,\mathrm{m}^2$. The rolling resistance of a cyclist on a high-quality racing cycle (total weight 73 kg) is 3.2 N.
- prius/. BMW data from Phil C. Stuart. http://www.randomuseless. info/318ti/economy.html.

Further reading: Gabrielli and von Kármán [1950].

Figure A.15. The Wartsila-Sulzer RTA96-C 14-cylinder engine. 27 m 279 Figure A.12 Prius data from B.Z. Wilson http://home.hiwaay.net/~bzwilson/ong and 13.5 m high.



http://www.wartsila.com/

B Wind II

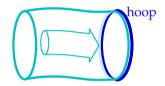
The physics of wind power

To estimate the energy available from wind, we'll need one formula: if an object with mass m moves at speed v then its kinetic energy is

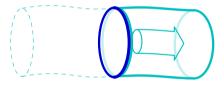
$$\frac{1}{2}mv^2$$
.

To estimate the energy in wind, let's imagine holding up a hoop with an area of one square metre, facing the wind whose speed is v. Consider the mass of air that passes through that hoop in one second. Here's a picture of that mass of air just before it passes through the hoop:

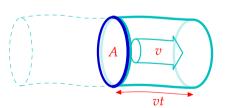




And here's a picture of the same mass of air one second later:



The mass of this piece of air is the product of its density ρ , its area A, and its length, which is v times t, where t is one second.



The kinetic energy of this piece of air is

$$\frac{1}{2}mv^2 = \frac{1}{2}\rho Avt \, v^2 = \frac{1}{2}\rho Atv^3. \tag{B.1}$$

So the power of the wind, for an area A – that is, the kinetic energy passing across that area per unit time – is

$$\frac{\frac{1}{2}mv^2}{t} = \frac{1}{2}\rho A v^3.$$
 (B.2)

I'm using this formula again:

 $mass = density \times volume$

B — Wind II 283

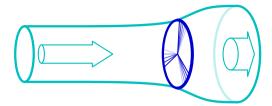


Figure B.3. Flow of air past a windmill. The air is slowed down and splayed out by the windmill.

This formula may look familiar – we derived an identical expression on p273 when we were discussing the power requirement of a moving car.

What's a typical wind speed? On a windy day, a cyclist really notices the wind direction; if the wind is behind you, you can go much faster than normal; the speed of such a wind is comparable to the typical speed of the cyclist, which is, let's say, 21 km per hour (13 miles per hour, or 6 metres per second). In Cambridge, the wind is only occasionally this big. Nevertheless, let's use this as a typical British figure (and bear in mind that we may need to revise our estimates).

The density of air is about 1.3 kg per m³. (I usually round this to 1 kg per m³, which is easier to remember, although I haven't done so here.) Then the typical power of the wind per square metre of hoop is

$$\frac{1}{2}\rho v^3 = \frac{1}{2}1.3 \,\text{kg/m}^3 \times (6 \,\text{m/s})^3 = 140 \,\text{W/m}^2. \tag{B.3}$$

Not all of this energy can be extracted by a windmill. The windmill slows the air down quite a lot, but it has to leave the air with *some* kinetic energy, otherwise that slowed-down air would get in the way. Figure B.3 is a cartoon of the actual flow past a windmill. The maximum fraction of the incoming energy that can be extracted by a disc-like windmill was worked out by a German physicist called Albert Betz in 1919. If the departing wind speed is one third of the arriving wind speed, the power extracted is 16/27 of the total power in the wind. 16/27 is 0.59. In practice let's guess that a windmill might be 50% efficient. In fact, real windmills are designed with particular wind speeds in mind; if the wind speed is significantly greater than the turbine's ideal speed, it has to be switched off.

As an example, let's assume a diameter of d = 25 m, and a hub height of 32 m, which is roughly the size of the lone windmill above the city of Wellington, New Zealand (figure B.4). The power of a single windmill is

efficiency factor \times power per unit area \times area

$$= \frac{1}{2} \times \frac{1}{2} \rho v^3 \times \frac{\pi}{4} d^2 \tag{B.4}$$

$$= \frac{1}{2} \times 140 \,\text{W/m}^2 \times \frac{\text{g}}{4} (25 \,\text{m})^2 \tag{B.5}$$

$$= 34 \, \text{kW}.$$
 (B.6)

Indeed, when I visited this windmill on a very breezy day, its meter showed it was generating 60 kW.

miles/ hour	km/h	m/s	Beaufort scale
2.2	3.6	1	force 1
7	11	3	force 2
11	18	5	force 3
13	21	6	force 4
16	25	7	10100 4
22	36	10	force 5
29	47	13	force 6
36	31	16	force 7
42	68	19	force 8

Figure B.2. Speeds.

To estimate how much power we can get from wind, we need to decide how big our windmills are going to be, and how close together we can pack them.

How densely could such windmills be packed? Too close and the upwind ones will cast wind-shadows on the downwind ones. Experts say that windmills can't be spaced closer than 5 times their diameter without losing significant power. At this spacing, the power that windmills can generate per unit land area is

$$\frac{\text{power per windmill (B.4)}}{\text{land area per windmill}} = \frac{\frac{1}{2}\rho v^3 \frac{\pi}{8} d^2}{(5d)^2}$$
(B.7)

$$= \frac{\pi}{200} \frac{1}{2} \rho v^3 \tag{B.8}$$

$$= 0.016 \times 140 \,\text{W/m}^2 \tag{B.9}$$

$$= 2.2 \,\mathrm{W/m^2}.$$
 (B.10)

This number is worth remembering: a wind-farm with a wind speed of 6 m/s produces a power of 2 W per m² of land area. Notice that our answer does not depend on the diameter of the windmill. The *ds* cancelled because bigger windmills have to be spaced further apart. Bigger windmills might be a good idea in order to catch bigger windspeeds that exist higher up (the taller a windmill is, the bigger the wind speed it encounters), or because of economies of scale, but those are the only reasons for preferring big windmills.

This calculation depended sensitively on our estimate of the windspeed. Is 6 m/s plausible as a long-term typical windspeed in windy parts of Britain? Figures 4.1 and 4.2 showed windspeeds in Cambridge and Cairngorm. Figure B.7 shows the mean winter and summer windspeeds in eight more locations around Britain. I fear 6 m/s was an overestimate of the typical speed in most of Britain! If we replace 6 m/s by Bedford's 4 m/s as our estimated windspeed, we must revise our estimate down, multiplying it by $(4/6)^3 \simeq 0.3$. (Remember, wind power scales as windspeed cubed.)

On the other hand, to estimate the typical power, we shouldn't take the mean wind speed and cube it; rather, we should find the mean cube of the windspeed. The average of the cube is bigger than the cube of the average. But if we start getting into these details, things get even more complicated, because real wind turbines don't actually deliver a power proportional to wind-speed cubed. Rather, they typically have just a range of wind-speeds within which the ideal behaviour holds; at higher or lower speeds real wind turbines deliver less than the ideal power.

Queries



Figure B.4. The Brooklyn windmill above Wellington, New Zealand, with people providing a scale at the base. On a breezy day, this windmill was producing 60 kW, (1400 kWh per day). Photo by Philip Banks.

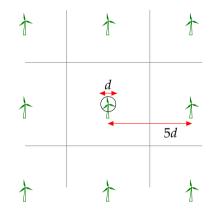


Figure B.5. Wind-farm layout.

Power per un	IT AREA
wind-farm (speed 6 m/s)	2 W/m ²

Table B.6. Facts worth remembering: wind-farms.

B — Wind II 285

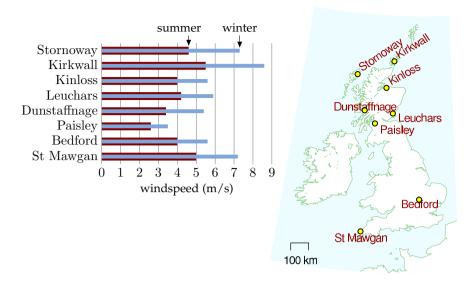


Figure B.7. Average summer windspeed (dark bar) and average winter windspeed (light bar) in eight locations around Britain. Speeds were measured at the standard weather-man's height of 10 metres. Averages are over the period 1971–2000.

What about micro-generation? If you plop one of those mini-turbines on your own roof, what energy can you expect it to deliver?

Assuming a windspeed of 6 m/s, which, as I said before, is *above* the average for most parts of Britain; and assuming a diameter of 1 m, the power delivered would be 50 W. That's 1.3 kWh per day – not very much. (See also p70.)

This estimate agrees with the figures for the D400 StealthGen, famously purchased by Conservative party leader David Cameron, which has a diameter of 1.1 m (and should thus deliver about 1.6 kWh/d at a windspeed of 6 m/s). The website www.d400.co.uk says that at windspeeds of 5.1 m/s and 7.7 m/s, this microturbine delivers 40 W and 120 W, respectively. Eclectic Energy encourages the buyer to expect the power produced to be 660 kWh per year (1.8 kWh/d). I am doubtful!

Figure B.8. An Ampair "600 W" micro-turbine. The average power generated by this micro-turbine in Leamington Spa is 0.037 kWh per day

(1.5 W).

Standard windmill properties

The typical windmill of today has a rotor diameter of around 54 metres centred at a height of 80 metres; such a machine has a 'capacity' of 1 MW. The 'capacity' or 'peak power' is the *maximum* power the windmill can generate in optimal conditions. Usually, wind turbines are designed to start running at wind speeds somewhere around 3 to 5 m/s and to stop if the wind speed reaches gale speeds of 25 m/s. The actual average power delivered is the 'capacity' multiplied by a factor that describes the fraction of the time that wind conditions are near optimal. This factor, sometimes called the "load factor" or "capacity factor," depends on the site; a typical load factor for a *good* site in the UK is 30%.

Other people's estimates of wind-farm power densities

In http://www.world-nuclear.org/policy/DTI-PIU.pdf the UK onshore wind resource is estimated using an assumed wind-farm power density of at most $9 \, \text{W/m}^2$ (capacity, not average production). If the capacity factor is 33% then the average power production would be $3 \, \text{W/m}^2$.

The London Array is an offshore wind-farm planned for the outer Thames Estuary. With its 1GW capacity, it is expected to become the world's largest offshore wind-farm. The completed wind-farm will consist of 271 wind turbines in $245\,\mathrm{km^2}$ [6086ec] and will deliver an average power of $3\,100\,\mathrm{GWh}$ per year ($350\,\mathrm{MW}$). (Cost £1.5bn.) That's a power density of $350\,\mathrm{MW}/245\,\mathrm{km^2} = 1.4\,\mathrm{W/m^2}$. This is lower than other offshore farms because, I guess, the site includes a big channel (Knock Deep) that's too deep (about $20\,\mathrm{m}$) for economical planting of turbines.

I'm more worried about what these plans [for the proposed London Array wind-farm] will do to this landscape and our way of life than I ever was about a Nazi invasion on the beach.

Bill Boggia, whose

family owns and runs several caravan parks around Graveney, where the undersea cables of the wind-farm will come ashore.



Figure B.9. The qr5.

Other shapes

Helical wind turbines – they look nice, and they work whatever the wind direction: especially useful in gusty urban environments. The qr5 from quietrevolution.co.uk is 5 m high \times 3.1 m in diameter, mounted at the top of a 9-m pole. It costs about £33 000 including installation. The turbine weighs approximately 250 kg. Its start-up speed is 4.5 m/s. If the average wind speed is $5.9 \, \text{m/s}$, it generates $10\,000 \, \text{kWh}$ per year (27 kWh/d or 1.1 kW, on average). That's $70 \, \text{W/m}^2$ of vertical area – about the same as a horizontal-axis turbine. And it has a capital cost of £30 000 per kW average power.

See ocean.tex for power density table.

See Faber [1995], p. 63.

Globally, 20 GW of wind capacity was added last year, costing about \$36 billion, according to the Global Wind Energy Council.

Variation of wind speed with height

Taller windmills see higher wind speeds. The way that wind speed increases with height is complicated and depends on the roughness of the surrounding terrain. As a ballpark figure, doubling the height typically increases wind-speed by 10% and thus increases the power of the wind by 30%.

Some standard formulae for speed v as a function of height z are:

 According to the wind shear formula from NREL [ydt7uk], the speed is a power of the height:

$$v(z) = v_{10} \left(\frac{z}{10 \,\mathrm{m}}\right)^{\alpha}$$

where v_{10} is the speed at 10 m, and a typical value of the exponent α is 0.143 or 1/7. The one-seventh law (v(z) is proportional to $z^{1/7}$) is used by Elliott et al. [1991], for example.

2. The wind shear formula from the Danish Wind Industry Association [yaoonz] is

$$v(z) = v_{\text{ref}} \frac{\log(z/z_0)}{\log(z_{\text{ref}}/z_0)},$$

where z_0 is a parameter called the roughness length, and $v_{\rm ref}$ is the speed at a reference height $z_{\rm ref}$ such as 10 m. The roughness length for typical countryside (agricultural land with some houses and sheltering hedgerows with some 500-m intervals – 'roughness class 2') is $z_0=0.1\,{\rm m}$.

In practice, these two wind shear formulae give similar numerical answers. That's not to say that they are accurate at all times however. van den Berg [2004] suggests that different wind profiles often hold at night.

Accidents

http://www.caithnesswindfarms.co.uk/ has data on wind fatalities and accidents. 45 fatalities since the 1970s, 17 in 2000–2006.

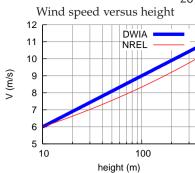
102 blade failure incidents. Pieces of blade travel 400 m.

Structural failures: 40 during 1998–2006.

Compare with nuclear, per GWy.

A set of wind turbines in Tsukuba City, Japan, so bad that they were actually importing more than they were exporting. Their installers were so embarrassed by the stationary turbines that they imported power to make them spin so that they looked like they were working! [6bkvbn]

Netherlands wind capacity factor: 22%; Germany: 19%.



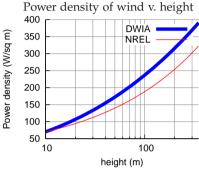


Figure B.10. Top: Two models of wind speed and wind power as a function of height. DWIA = Danish Wind Industry Association; NREL = National Renewable Energy Laboratory. For each model the speed at 10 m has been fixed to 6 m/s. For the Danish Wind model, the roughness length is set to $z_0 = 0.1$ m. Bottom: The power density is the power per unit of upright area.

Notes and further reading

page no.

- 283 The maximum fraction of the incoming energy that can be extracted by a disc-like windmill... There is a nice explanation of this on the Danish Wind Industry Association's website. [yekdaa].
- 285 Usually, wind turbines are designed to start running at wind speeds around 3 to 5 m/s. [ymfbsn].
 - a typical load factor for a good site is 30%. In 2005, the average load factor of all major UK wind-farms was 28% [ypvbvd]. The load factor varied during the year, with a low of 17% in June and July. The load factor for the best region in the country Caithness, Orkney and the Shetlands was 33%. The load factors of the two offshore wind-farms operating in 2005 were 36% for North Hoyle (off North Wales) and 29% for Scroby Sands (off Great Yarmouth). Average load factors in 2006 for ten regions were: Cornwall 25%; Mid-Wales 27%; Cambridgeshire and Norfolk 25%; Cumbria 25%; Durham 16%; Southern Scotland 28%; Orkney and Shetlands 35%; Northeast Scotland 26%; Northern Ireland 31%; Offshore 29%. [wbd8o]

Watson et al. [2002] say a minimum annual mean wind speed of 7.0 m/s is currently thought to be necessary for commercial viability of wind power. About 33% of UK land area has such speeds.



Figure B.11. A 5.5-m diameter Iskra $5\,\mathrm{kW}$ turbine [www.iskrawind.com] having its annual check-up. This turbine, located in Hertfordshire (not the windiest of locations in Britain), mounted at a height of $12\,\mathrm{m}$, has an average output of $11\,\mathrm{kWh}$ per day. A windfarm of machines with this performance, one per $30\,\mathrm{m} \times 30\,\mathrm{m}$ square, would have a power density of $0.5\,\mathrm{W/m^2}$.

C Planes II

What we need to do is to look at how you make air travel more energy efficient, how you develop the new fuels that will allow us to burn less energy and emit less.

Tony Blair

Hoping for the best is not a policy, it is a delusion.

Emily Armistead, Greenpeace

What are the fundamental limits of travel by flying? Does the physics of flight require an unavoidable use of a certain amount of energy, per ton, per kilometre flown? What's the maximum distance a 300-ton Boeing 747 can fly? What about a 1-kg bar-tailed godwit or a 100-gram Arctic tern?

Just as Chapter 3, in which we estimated consumption by cars, was followed by Chapter A, offering a model of where the energy goes in cars, this chapter fills out Chapter 5, discussing where the energy goes in planes. The only physics required is Newton's laws of motion, which I'll describe when they're needed.

This discussion will allow us to answer questions such as 'would air travel consume much less energy if we travelled in slower propellor-driven planes?' There's a lot of equations ahead: I hope you enjoy them!

How to fly

Planes (and birds) move through air, so, just like cars and trains, they experience a drag force, and much of the energy guzzled by a plane goes into pushing the plane along against this force. Additionally, unlike cars and trains, planes have to expend energy *in order to stay up*.

Planes stay up by throwing air down. When the plane pushes down on air, the air pushes up on the plane (because Newton's third law tells it to). If this upward push, which is called lift, is big enough to balance the downward weight of the plane, the plane avoids plummeting downwards.

When the plane throws air down, it gives that air kinetic energy. So creating lift requires energy. The total power required by the plane is the sum of the power required to create lift and the power required to overcome ordinary drag. (The power required to create lift is usually called 'induced drag', by the way. But I'll call it the lift power, $P_{\rm lift}$.)

The two equations we'll need, in order to work out a theory of flight, are Newton's second law:

force = rate of change of momentum,
$$(C.1)$$

and Newton's third law, which I just mentioned:

force exerted on A by B = - force exerted on B by A. (C.2)







Figure C.1. Birds: two Arctic terns, a bar-tailed godwit, and a Boeing 747.

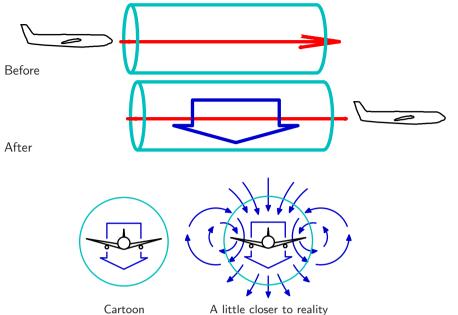


Figure C.2. A plane encounters a stationary tube of air. Once the plane has passed by, the air has been thrown downwards by the plane. The force exerted by the plane on the air to accelerate it downwards is equal and opposite to the upwards force exerted on the plane by the air.

Figure C.3. Our cartoon assumes that the plane leaves a sausage of air moving down in its wake. A realistic picture involves a more complex swirling flow. For the real thing, see figure C.4.

If you don't like equations, I can tell you the punchline now: we'll find that the power required to create lift turns out to be *equal* to the power required to overcome drag. So the requirement to 'stay up' *doubles* the power required.

Let's make a cartoon of the lift force on a plane moving at speed v. In a time t the plane moves a distance vt and leaves behind it a sausage of downward-moving air (figure C.2). We'll call the cross-sectional area of this sausage A_s . This sausage's diameter is roughly equal to the wingspan w of the plane. (Within this large sausage is a smaller sausage of swirling turbulent air with cross-sectional area similar to the frontal area of the plane's body.) Actually, the details of the air flow are much more interesting than this sausage picture: each wing tip leaves behind it a vortex, with the air between the wingtips moving down fast, and the air beyond (outside) the wingtips moving up (figures C.3 & C.4). This upward-moving air is exploited by birds flying in formation: just behind the tip of a bird's wing is a sweet little updraft. Anyway, let's get back to our sausage.

The sausage's mass is

$$m_{\text{sausage}} = \text{density} \times \text{volume} = \rho v t A_{\text{s}}.$$

Let's say the whole sausage is moving down with speed u, and figure out what u needs to be in order for the plane to experience a lift force equal to its weight mg. The downward momentum of the sausage created in time t is

$$mass \times velocity = m_{sausage}u = \rho vt A_s u.$$



Figure C.4. Air flow behind a plane. Photo by NASA Langley Research Center.

291

And by Newton's laws this must equal the momentum delivered by the plane's weight in time t, namely,

Rearranging this equation,

$$\rho vt A_{s}u = mgt$$

we can solve for the required sausage speed,

$$u = \frac{mg}{\rho v A_s}$$
.

Interesting! The sausage speed is inversely related to the plane's speed. A slow-moving plane has to throw down air harder than a fast-moving plane, because it encounters less air per unit time. That's why landing planes, travelling slowly, have to extend their flaps: so as to create a larger and steeper wing that deflects air more.

What's the energetic cost of pushing the sausage down at the required speed *u*? The power required is

$$P_{\text{lift}} = \frac{\text{kinetic energy of sausage}}{\text{time}}$$
 (C.3)
= $\frac{1}{t} \frac{1}{2} m_{\text{sausage}} u^2$ (C.4)

$$= \frac{1}{t} \frac{1}{2} m_{\text{sausage}} u^2 \tag{C.4}$$

$$= \frac{1}{2t}\rho v t A_{\rm s} \left(\frac{mg}{\rho v A_{\rm s}}\right)^2 \tag{C.5}$$

$$= \frac{1}{2} \frac{(mg)^2}{\sigma v A_c}.$$
 (C.6)

The total power required to keep the plane going is the sum of the lift power and the power required to overcome drag:

$$P_{\text{total}} = P_{\text{drag}} + P_{\text{lift}}$$
 (C.7)

$$= \frac{1}{2}c_{\rm d}\rho A_{\rm p}v^3 + \frac{1}{2}\frac{(mg)^2}{\rho v A_{\rm s}},\tag{C.8}$$

where A_p is the frontal area of the plane and c_d is its drag coefficient (as in Chapter A).

The fuel-efficiency of the plane, in the sense of energy per distance travelled, would be

$$\frac{\text{energy}}{\text{distance}}\Big|_{\text{ideal}} = \frac{P_{\text{total}}}{v} = \frac{1}{2}c_{\text{d}}\rho A_{\text{p}}v^2 + \frac{1}{2}\frac{(mg)^2}{\rho v^2 A_{\text{s}}},\tag{C.9}$$

if the plane turned its fuel energy into drag power and lift power perfectly efficiently. (Incidentally, another name for "energy per distance travelled"

is "force," and we can recognize the two terms above as the drag force $\frac{1}{2}c_{\rm d}\rho A_{\rm p}v^2$ and the lift-related force $\frac{1}{2}\frac{(mg)^2}{\rho v^2 A_{\rm s}}$. The sum is the force that specifies exactly how hard the engines have to push.)

Real jet engines have an efficiency of about $\epsilon=1/3$, so the energy-perdistance of a plane travelling at speed v is

$$\frac{\text{energy}}{\text{distance}} = \frac{1}{\epsilon} \left(\frac{1}{2} c_{\text{d}} \rho A_{\text{p}} v^2 + \frac{1}{2} \frac{(mg)^2}{\rho v^2 A_{\text{s}}} \right). \tag{C.10}$$

This fuel-efficiency is fairly complicated; but it simplifies greatly if we assume that the plane is *designed* to fly at the speed that *minimizes* the energy-per-distance. The energy-per-distance, you see, has got a sweet-spot as a function of v (figure C.5). The sum of the two quantities $\frac{1}{2}c_{\rm d}\rho A_{\rm p}v^2$ and $\frac{1}{2}\frac{(mg)^2}{\rho v^2 A_{\rm s}}$ is smallest when the two quantities are equal. This phenomenon is delightfully common in physics and engineering: two things that don't obviously *have* to be equal *are* actually equal, or equal within a factor of 2.

So, this equality principle tells us that the optimum speed for the plane is such that

$$c_{\rm d}\rho A_{\rm p} v^2 = \frac{(mg)^2}{\rho v^2 A_{\rm s}},$$
 (C.11)

i.e.,

$$\rho v_{\text{opt}}^2 = \frac{mg}{\sqrt{c_{\text{d}}A_{\text{p}}A_{\text{s}}}},\tag{C.12}$$

This defines the optimum speed if our cartoon of flight is accurate; the cartoon breaks down if the engine efficiency ϵ depends significantly on speed, or if the speed of the plane exceeds the speed of sound (330 m/s); above the speed of sound, we would need a different model of drag and lift.

Let's check our model by seeing what it predicts is the optimum speed for a 747 and for an albatross. We must take care to use the correct airdensity: if we want to estimate the optimum cruising speed for a 747 at $30\,000$ feet, we must remember that air density drops with increasing altitude z as $\exp(-mgz/kT)$, where m is the mass of nitrogen or oxygen molecules, and kT is the thermal energy (Boltzmann's constant times absolute temperature) – so the density is about 3 times smaller at that altitude.

The predicted optimal speeds (table C.6) are more accurate than we have a right to expect! The 747's optimal speed is predicted to be 540 mph, and the albatross's, 32 mph – both very close to the true cruising speeds of the two birds (560 mph and 30–55 mph respectively).

Let's explore a few more predictions of our cartoon. We can check whether the force (C.9) is compatible with the known thrust of the 747. Remembering that at the optimal speed, the two forces are equal, we just

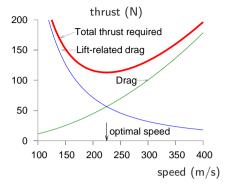


Figure C.5. The force required to keep a plane moving, as a function of its speed v, is the sum of an ordinary drag force $\frac{1}{2}c_{\rm d}\rho A_{\rm p}v^2$ – which increases with speed - and the lift-related force (also known as the induced drag) $\frac{1}{2} \frac{(mg)^2}{\rho v^2 A_s}$ – which decreases with speed. There is an ideal speed, v_{optimal} , at which the force required is minimized. The force is an energy per distance, so minimizing the force also minimizes the fuel per distance. To optimize the fuel efficiency, fly at v_{optimal} . This graph shows our cartoon's estimate of the thrust required, in newtons, for a Boeing 747 of mass 319 t, wingspan 64.4 m, drag coefficient 0.03, and frontal area 180 m², travelling in air of density $\rho = 0.41 \,\mathrm{kg/m^3}$ (the density at a height of 10 km), as a function of its speed v in m/s. Our model has an optimal speed $v_{\text{optimal}} = 220 \,\text{m/s}$ (540 mph). For a cartoon based on sausages, this is a good match to real life!

C — Planes II 293

Bird		747	Albatross
Designer		Boeing	natural selection
Mass (fully-laden)	m	363 000 kg	8 kg
Wingspan	w	64.4 m	3.3 m
Area*	A_{p}	180m^2	$0.09 \mathrm{m}^2$
Density	ρ	$0.4\mathrm{kg/m^3}$	$1.2 \mathrm{kg/m^3}$
Drag coefficient	c_{d}	0.03	0.1
Optimum speed	$v_{ m opt}$	220 m/s	14 m/s
	•	$= 540 \mathrm{mph}$	= 32 mph

Table C.6. Estimating the optimal speeds for a jumbo jet and an albatross.

* Frontal area estimated for 747 by taking cabin width (6.1 m) times estimated height of body (10 m) and adding double to allow for the frontal area of engines, wings, and tail; for albatross, frontal area of 1 square foot estimated from a photograph.

need to pick one of them and double it:

force =
$$\frac{\text{energy}}{\text{distance}}\Big|_{\text{ideal}} = \frac{1}{2}c_{\text{d}}\rho A_{\text{p}}v^2 + \frac{1}{2}\frac{(mg)^2}{\rho v^2 A_{\text{s}}}$$
 (C.13)

$$= c_{\rm d}\rho A_{\rm p} v_{\rm opt}^2 \tag{C.14}$$

$$= c_{d}\rho A_{p}v_{opt}^{2}$$
 (C.14)
$$= c_{d}\rho A_{p}\frac{mg}{\rho(c_{d}A_{p}A_{s})^{1/2}}$$
 (C.15)

$$= \left(\frac{c_{\rm d}A_{\rm p}}{A_{\rm s}}\right)^{1/2} mg. \tag{C.16}$$

Let's define the filling factor f_A to be the area ratio:

$$f_A = \frac{A_p}{A_c}. (C.17)$$

(Think of f_A as the fraction of the square occupied by the plane in figure C.7.) Then

force =
$$(c_d f_A)^{1/2} (mg)$$
. (C.18)

Interesting! Independent of the density of the fluid through which the plane flies, the required thrust (for a plane travelling at the optimal speed) is just a dimensionless constant $(c_d f_A)^{1/2}$ times the weight of the plane. This constant, by the way, is known as the drag-to-lift ratio of the plane. (The lift-to-drag ratio has a few other names: the glide number, glide ratio, aerodynamic efficiency, or finesse.)

Taking the jumbo jet's figures, $c_{\rm d} \simeq 0.03$ and $f_A \simeq 0.04$, we find the required thrust is

$$(c_d f_A)^{1/2} mg = 0.036 \, mg = 130 \, \text{kN}.$$

How does this agree with the 747's spec sheets? In fact each of the 4 engines has a maximum thrust of about 250 kN, but this maximum thrust is used only during take-off. During cruise, the thrust is much smaller:

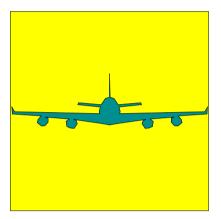


Figure C.7. Frontal view of a Boeing 747, used to estimate the frontal area $A_{\rm p}$ of the plane. The square has area $A_{\rm s}$ (the square of the wingspan).

Airbus A320	17
Boeing 767-200	19
Boeing 747-100	18
Common Tern	12
Albatross	20

Table C.8. Lift-to-drag ratios.

the thrust of a cruising 747 is 200 kN, just 50% more than our cartoon

This thrust can be used directly to deduce the transport efficiency achieved by any plane. We can work out two sorts of transport efficiency: the energy cost of moving weight around, measured in kWh per ton-kilometre; and the energy cost of moving people, measured in kWh per 100 passenger-kilometres.

Efficiency in weight terms

Thrust is a force, and a force is an energy per unit distance. The total energy used per unit distance is bigger by a factor $(1/\epsilon)$, where ϵ is the efficiency of the engine, which we'll take to be 1/3.

Here's the gross transport cost, defined to be the energy per unit weight (of the entire craft) per unit distance:

transport cost
$$=$$
 $\frac{1}{\epsilon} \frac{\text{force}}{\text{mass}}$ (C.19)

$$= \frac{1}{\epsilon} \frac{(c_{\rm d} f_A)^{1/2} mg}{m} \tag{C.20}$$

$$= \frac{1}{\epsilon} \frac{(c_{d}f_{A})^{1/2} mg}{m}$$

$$= \frac{(c_{d}f_{A})^{1/2}}{\epsilon} g$$
(C.20)
(C.21)

So the transport cost is just a dimensionless quantity (related to a plane's shape and its engine's efficiency), multiplied by g, the acceleration due to gravity. If we plug in $\epsilon = 1/3$, $c_{\rm d} = 0.03$, and $f_A \simeq 0.04$, we find the transport efficiency, according to our cartoon, is

 $0.1\,g$

or

0.3 kWh/ton-km.

Can planes be improved?

If engine efficiency can be boosted only a tiny bit by technological progress, and if the shape of the plane has already been essentially perfected, then there is little that can be done about the dimensionless quantity. The transport efficiency is close to its physical limit. The aerodynamics community say that the shape of planes could be improved a little by a switch to blended-wing bodies, and that the drag coefficient could be reduced a little by laminar flow control, a technology that reduces the growth of turbulence over a wing by sucking a little air through small perforations in the surface [Braslow, 1999]. The addition of laminar flow control to existing planes would deliver a 15% improvement in drag coefficient, and the change of shape to blended-wing bodies is predicted to improve the drag coefficient by about 18% [Green, 2006]. And equation (C.21) says that the



Figure C.9. Cessna 310N: 60 kWh per 100 passenger-km. A Cessna 310 Turbo carries 6 passengers (including 1 pilot) at a speed of 370 km/h. Photograph by Adrian Pingstone.

C — Planes II 295

transport cost is proportional to the square root of the drag coefficient, so improvements of $c_{\rm d}$ by 15% or 18% would improve transport cost by 7.5% and 9% respectively.

This transport efficiency is the efficiency of moving weight around, *including the weight of the plane itself*. To estimate the energy required to move freight by plane, per unit weight of freight, then we need to divide by the fraction that is cargo. For example, if a full 747 freighter is about 1/3 cargo, then its transport efficiency is

or roughly 1 kWh/ton-km. This is the same as the transport efficiency of a truck.

Transport efficiency in terms of bodies

Similarly, we can estimate a passenger transport-efficiency.

transport efficiency (passenger-km per litre of fuel)

= number of passengers
$$\times \frac{\text{energy per litre}}{\underline{\text{thrust}}}$$
 (C.22)

= number of passengers
$$\times \frac{\epsilon \times \text{energy per litre}}{\text{thrust}}$$
 (C.23)

$$= 400 \times \frac{1}{3} \frac{38 \,\text{MJ/litre}}{200\,000 \,\text{N}} \tag{C.24}$$

which is a bit more efficient than a typical single-occupant car (12 km per litre). We can find the actual efficiency of a 747 by looking up its specifications: it is indeed 25 passenger-km per litre. So travelling by plane is more energy-efficient than car if there are only one or two people in the car; and cars are more efficient if there are three or more passengers in the vehicle.

Let's re-express these results in kWh per 100 kilometres travelled. Each litre of jet fuel delivers 10 kWh of energy, so the 747's energy-consumption is

42 kWh per 100 passenger-km.

Key points

We've covered quite a lot of ground! Let's recap the key ideas. Half of the work done by a plane goes into *staying up*; the other half goes into *keeping going*. The fuel efficiency at the optimal speed, expressed as an energy-per-distance-travelled, was found in the force (C.18), and it was simply proportional to the weight of the plane; the constant of proportionality is the drag-to-lift ratio, which is determined by the shape of the plane. So whereas lowering speed-limits for cars would reduce the energy consumed per distance travelled, there is no point in considering speed-limits



Figure C.10. "Fasten your cufflinks." A Bombardier Learjet 60XR carrying 8 passengers at 780 km/h has a transport cost of 150 kWh per 100 passenger-km. Photograph by Adrian Pingstone.

for planes. Planes that are up in the air have optimal speeds, different for each plane, depending on its weight, and they already go at their optimal speeds. The only way to make a plane consume fuel more efficiently is to put it on the ground and stop it. Planes have been fantastically optimized, and there is no prospect of significant improvements in plane efficiency. (See pages 140 and 39 for further discussion of the notion that new superjumbos are "far more efficient" than old jumbos; and p37 for discussion of the notion that turboprops are "far more efficient" than jets.)

Range

Another prediction we can make is, what's the range of a plane or bird – the biggest distance it can go without refuelling? You might think that bigger planes have a bigger range, but the prediction of our model is startlingly simple. The range of the plane, the maximum distance it can go before refuelling, is proportional to its velocity and to the total energy of the fuel, and inversely proportional to the rate at which it guzzles fuel:

range =
$$v_{\text{opt}} \frac{\text{energy}}{\text{power}} = \frac{\text{energy} \times \epsilon}{\text{force}}$$
. (C.26)

Now, the total energy of fuel is the calorific value of the fuel, C (in joules per kilogram), times its mass; and the mass of fuel is some fraction f_{fuel} of the total mass of the plane. So

range =
$$\frac{\text{energy }\epsilon}{\text{force}} = \frac{Cm\epsilon f_{\text{fuel}}}{(c_{\text{d}}f_A)^{1/2}(mg)} = \frac{C\epsilon f_{\text{fuel}}}{(c_{\text{d}}f_A)^{1/2}g} = \frac{\epsilon f_{\text{fuel}}}{(c_{\text{d}}f_A)^{1/2}} \frac{C}{g}$$
. (C.27)

It's hard to imagine a simpler prediction: the range of any bird or plane is the product of a dimensionless factor $\left(\frac{\epsilon f_{\rm fuel}}{(c_{\rm d}f_A)^{1/2}}\right)$ which takes into account the engine efficiency, the drag coefficient, and the bird's geometry, with a fundamental distance,

$$\frac{C}{g}$$

which is a property of the fuel and gravity, and nothing else. No bird size, no bird mass, no bird length, no bird width; no dependence on the fluid density.

So what is this magic length? It's the same distance whether the fuel is albatross fat or jet fuel: both these fuels are essentially hydrocarbons $(CH_2)_n$. Jet fuel has a calorific value of $C=40\times 10^6\,\mathrm{J}$ per kg. The distance associated with jet fuel is

$$d_{\text{Fuel}} = \frac{C}{g} = 4000 \,\text{km}.$$

The range of the bird is the intrinsic range of the fuel, 4000 km, times a fac-

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com



Figure C.11. Boeing 737-700: 30 kWh per 100 passenger-km. Photograph © Tom Collins.

You can think of d_{Fuel} as the distance that the fuel could throw itself if it suddenly converted all its chemical energy to kinetic energy and launched itself on a parabolic trajectory with no air resistance. [To be precise, the distance achieved by the optimal parabola is twice C/g.] This distance is also the vertical height to which the fuel could throw itself if there were no air resistance. Another amusing thing to notice is that the calorific value of a fuel C, which I gave in joules per kilogram, is also a squared-velocity (just as the energy-to-mass ratio E/min Einstein's $E = mc^2$ is a squared-velocity, c^2): 40×10^6 J per kg is $(6000 \,\mathrm{m/s})^2$. So one way to think about fat is "fat is 6000 metres per second". If you want to lose weight by going jogging, 6000 m/s (12000 mph) is the speed you should aim for in order to lose it all in one giant leap. tor $\left(\frac{\varepsilon f_{\rm fuel}}{(c_{\rm d}f_A)^{1/2}}\right)$. If our bird has engine efficiency $\varepsilon=1/3$, and $(c_{\rm d}f_A)^{1/2}\simeq 0.03$, and if nearly half of the bird is fuel (a fully-laden 747 is 46% fuel), we find that all birds and planes, of whatever size, have the same range: about five times the fuel's distance, roughly 20 000 km.

This figure is again close to the true answer: the nonstop flight record for a 747 (set on March 23–24, 1989) was a distance of 16 560 km.

And the claim that the range is independent of bird size is supported by the observation that birds of all sizes, from great geese down to dainty swallows and arctic tern migrate intercontinental distances.

The longest recorded non-stop flight by a bird was a distance of 11 000 km, by a bar-tailed godwit.

How far did Steve Fossett go in the specially-designed Scaled Composites Model 311 Virgin Atlantic GlobalFlyer? 41 467 km. [33ptcg] An unusual plane: 83% of its take-off weight was fuel; the flight made careful use of the jet-stream to boost its distance. Fragile, the plane had several failures along the way.

One interesting point brought out by this cartoon is: if we ask "what's the optimum air-density to fly in?", we find that the thrust required at the optimum speed is independent of the density. So our cartoon plane would be equally happy to fly at any height; it could achieve the same miles-pergallon whatever the density; but the optimum speed does depend on the density $(v^2 \sim 1/\rho)$. So all else being equal, our cartoon plane would have the shortest journey time if it flew in the lowest-density air possible. Now real engines' efficiencies aren't independent of speed and air density. As a plane gets lighter by burning fuel, our cartoon says its optimal speed at a given density would reduce $(v^2 \sim mg/(\rho(c_d A_p A_s)^{1/2}))$. So a plane travelling in air of constant density should slow down a little as it gets lighter. But a plane can both keep going at a constant speed and continue flying at its optimal speed if it increases its altitude so as to reduce the air density. Next time you're on a long-distance flight, you could check whether the pilot increases the cruising height from, say, 31000 feet to 39 000 feet by the end of the flight.

What would a hydrogen plane do?

We've already argued that the efficiency of flight, in terms of energy per ton-km, is just a simple dimensionless number times g. Changing the fuel isn't going to change this fundamental argument. Hydrogen-powered planes are worth discussing if we're hoping to reduce climate-changing emissions. They might also have better range. But don't expect them to be radically more energy-efficient.

We can estimate the range of a hydrogen-powered plane using the idea that the range is proportional to *C*, the energy content of the fuel. Hydrogen has the highest energy content of any common fuel by weight (about three times more than gasoline), but the lowest energy content by

volume (about four times less than gasoline, if liquified). So the range of a hydrogen-fuelled plane could be three times bigger than that of a hydrocarbon-fuelled plane, if the storage tanks's weight was not significant. But if it were to have any space for passengers inside, the plane's shape would have to be altered. The big problem is storage. Real hydrogen storage containers weigh far more than the hydrogen they contain.

Engine efficiency

("Specific fuel consumption.") Typical engine efficiencies are in the range 23%–36%. For typical aircraft, overall engine efficiency ranges between 20% and 40%, with the best bypass engines delivering 30–37% when cruising. You can't simply pick the most efficient engine however, since it may be heavier (I mean, it may have bigger mass per unit thrust), thus reducing overall plane efficiency.

Overall efficiency: "The last piston-powered aircraft were as fuel-efficient as the current average jet." http://www.transportenvironment.org/

Possible areas for improvement of plane efficiency

"Laminar flow control" (cunning trick for reducing drag a little). Flying wings: said to be 25% more fuel efficient. Propfans instead of turbofans? Said to be 12% more efficient for short journeys (less than 3000 km), but not for long journeys. They're more efficient because the engine efficiency is greater.

Formation flying in the style of geese could give a 10% improvement in fuel efficiency (because the lift-to-drag ratio of the formation is higher than that of a single aircraft), but this trick relies, of course, on the geese wanting to migrate to the same destination at the same time.

Optimizing the hop lengths: long-range planes (designed for a range of say 15000 km) are not quite as fuel-efficient as shorter-range planes, because they have to carry extra fuel, which makes less space for cargo and passengers. It would be more energy efficient to fly shorter hops in shorter-range planes. The sweet spot is when the hops are about 5000 km long, so typical long-distance journeys would have one or two refuelling stops. Multi-stage long-distance flying might be about 15% more fuel efficient; but of course it would introduce other costs.

Assumptions in my cartoon

I made these assumptions in my cartoon:

Long-distance flights use fuel uniformly enough not to bother about the weight of the fuel changing the weight of the plane. In fact, when landing, the mass of a long-distance 747 is roughly half its take-off weight, because of the lost fuel.

C — Planes II 299

Eco-friendly aeroplanes

Occasionally you may hear about people making eco-friendly aeroplanes. Earlier in this chapter, however, our cartoon made the assertion that the transport efficiency of *any* plane is about

0.3 kWh/ton-km.

According to the cartoon, the only ways in which a plane could significantly improve on this figure are to reduce air resistance (perhaps by some new-fangled vacuum-cleaners-in-the-wings trick) or to change the geometry of the plane (making it look more like a glider, with immensely wide wings compared to the fuselage, or getting rid of the fuselage altogether).

So, let's look at the latest news story about 'eco-friendly aviation' and see whether one of these planes can beat the 0.3 kWh per ton-km benchmark. If so, we might conclude that the cartoon is defective.

The Electra, a wood-and-fabric single-seater, flew for 48 minutes for $50\,\mathrm{km}$ around the southern Alps [6r32hf]. The Electra has a 9-m wingspan and a 18-kW electric motor powered by 48 kg of lithium-polymer batteries. The aircraft's take-off weight is $265\,\mathrm{kg}$ (134 kg of aircraft, 47 kg of batteries, and 84 kg of human cargo). On 23rd December, 2007 it flew a distance of $50\,\mathrm{km}$. If we assume that the battery's energy density was $130\,\mathrm{Wh/kg}$, and that the flight used 90% of a full charge ($5.5\,\mathrm{kWh}$), the transport efficiency of the plane was roughly

0.4 kWh/ton-km,

which is more energy than our cartoon's ideal. So the cartoon still stands. This electrical plane is less efficient than the cartoon, and it is not a lower-energy plane than a normal fossil-sucker.

Of course, this doesn't mean that electric planes are not interesting. (Incidentally, as a person-transporter, it delivers a respectable 11 kWh per 100 p-km, identical to the electric car in our transport diagram.) If one could replace traditional planes by alternatives with equal energy consumption but no carbon emissions, that would certainly be a useful technology. But in this book the bottom line is always: "where is the energy to come from?"

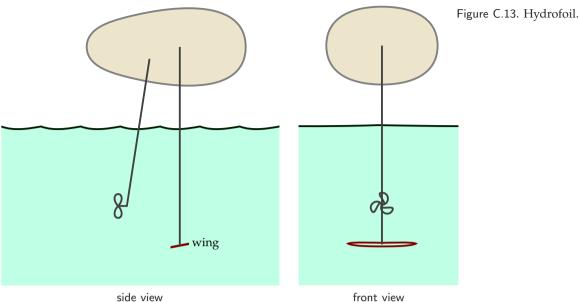
Many boats are birds too

Some time after writing this cartoon of flight, I realized that it applies to more than just the birds of the air – it applies to hydrofoils, and to other high-speed watercraft too – all those that ride higher in the water when moving.

Figure C.13 shows the principle of the hydrofoil. The weight of the craft is supported by a tilted underwater wing, which may be quite tiny compared with the craft. The wing generates lift by throwing fluid down,



Figure C.12. The Electra F-WMDJ: 11 kWh per 100 p-km. Photo by Jean-Bernard Gache. http://www.apame.eu/



just like the plane of figure C.2. If we assume that the drag is dominated by the drag on the wing, and that the wing dimensions and vessel speed have been optimized to minimize the energy expended per unit distance, then the best possible transport efficiency, in the sense of energy per tonkilometre, will be just the same as in equation (C.21):

$$\frac{(c_{\rm d}f_A)^{1/2}}{\epsilon}g$$
,

where c_d is the drag coefficient of the underwater wing, f_A is the dimensionless area ratio defined before, ϵ is the engine efficiency, and g is the acceleration due to gravity.

Perhaps c_d and f_A are not quite the same as those of an optimized plane. But the remarkable thing about this theory is that it has no dependence on the density of the fluid through which the wing is flying. So our ballpark prediction is that the transport efficiency (energy-per-distanceper-weight, including the vehicle weight) of a hydrofoil is the same as the transport efficiency of an aeroplane! Namely, roughly 0.3 kWh per ton-km.

For vessels that skim the water surface, such as high-speed catamarans and water-skiers, an accurate cartoon should also include the energy going into making waves, but I'm tempted to guess that this hydrofoil theory is still roughly right.

I've not yet found data on the transport-efficiency of a hydrofoil, but some data for a passenger-carrying catamaran travelling at 41 km/h seem to agree pretty well: it consumes roughly 1 kWh per ton-km.

It's quite a surprise to me to learn that an island hopper who goes from island to island by plane not only gets there faster than someone who hops

C — Planes II 301

by boat – he quite probably uses less energy too.

Mythconceptions

The plane was going anyway, so my flying was energy-neutral.

This is false for two reasons. First, your extra weight on the plane requires extra energy to be consumed in keeping you up. Second, airlines respond to demand by flying more planes.

Planes could be more efficient if they went slower.

False. Here's the rough idea, which this chapter covered in detail: yes, reducing the speed of a plane would reduce its turbulent drag, just as in the case of a car. But planes have to expend energy on another activity, namely throwing air down. Planes have to throw air down in order to stay up, whereas cars get pushed up for free by the road. The plane defies gravity at a cost. It costs energy to throw air down. And it's not obvious, but this throwing-down actually costs more energy, the slower the plane goes. This means that any plane has a sweet spot, an optimal speed that it should go at, in order to deliver the most miles per gallon.

Notes and further reading

page no.

Load factor of Easyjet up to 90%. BBC News, Monday, 7 August 2006. [20atgv]

Drag coefficient for 747 from www.aerospaceweb.org. Other 747 data from [2af5gw]. Albatross facts from [32judd]. Albatross estimated drag coefficient (0.1) based on C M Bishop paper – says $c_{\rm d}=0.1$ is conceivable.

- 297 The longest recorded non-stop flight by a bird...
 - New Scientist 2492. "Bar-tailed godwit is king of the skies" 26 March 2005. 11 September 2007: Godwit flies 11 500 km non-stop from Alaska to New Zealand. [2qbquv]
 - ?? Optimizing hop lengths: the sweet spot is when the hops are about 5000 km long.

Source: Green [2006].

300 Data for a passenger-carrying catamaran. From [5h6xph]: Displacement (full load) 26.3 tons. On a 1050 nautical mile voyage she consumed just 4780 litres of fuel. I reckon that's a weight-transport-efficiency of 0.93 kWh per ton-km. I'm counting the total weight of the vessel here, by the way. The same vessel's passenger-transport-efficiency is roughly 35 kWh per 100 p-km.

Further reading Tennekes [1997], Shyy et al. [1999].

D Solar II

Solar biomass II

On p44 we listed four solar biomass options:

- 1. "Coal substitution."
- 2. "Petroleum substitution."
- 3. Food for humans or other animals.
- 4. Incineration of agricultural by-products.

We'll estimate the maximum contribution of each of these processes in turn. In practice, many of these methods require so much energy be put *in* along the way that they are scarcely net contributors. But in what follows, I'll ignore such embodied-energy costs.

Solar biomass: energy crops as a coal substitute

Productivity of Britain's main biodiesel crop, rape

Typically, rape is sown in September and harvested the following August. Currently 450 000 ha of oilseed rape is grown in the UK each year. (That's 2% of the UK.) Fields of rape produce 1200 litres of biodiesel (net) per hectare per year; biodiesel has 9.8 kWh/l; that's 0.13 W/m². Source: Bayer Crop Science [2003].

I think this net figure allows for energy inputs. But does it include all of them? The processing of vegetable oil uses methanol derived from natural gas. 1 ton of oilseed rape yields 4091, which turns into 4731 of biodiesel but only with the help of 801 of methanol. Evans [2007]

Power densities of power stations				
Wind farm: $v = 6 \text{m/s}$ 2W/m^2 flat ground				
Solar				
Photovoltaic	20%	20 W/m ² South-facing roof		
	20%	20 W/m ² flat ground		
Biomass for chemicals	1%	0.5 W/m ² flat ground		
Biomass as coal-substitute	0.4%	0.2 W/m ² flat ground		
Nuclear fission		1000W/m^2		



Figure D.1. Two trees, yesterday.



Figure D.3. Oil-seed rape. If used to create biodiesel, the power density of rape is 0.13 W/m². Photo by Tim Dunne.

Table D.2. Power densities

D — Solar II 303

Bioethanol

Where sugar cane can be produced (eg Brazil) production is 80 t/ha, which yields about $17\,600\,l$ of ethanol. That's $1.2\,\text{W/m}^2$. Cellulosic ethanol yield is expected to be in the range $0.12\text{-}0.32\,l$ per kg of undried feedstock. Mabee et al. [2006]

Jatropha is no exception to the rule: biosolar has low power density

Jatropha is an oil-bearing crop that grows best in dry tropical regions (300–1000 mm rain per year). It likes temperatures 20–28 °C. The projected yield in hot countries on good land is 1600 litres of biodiesel per hectare per year. That's a power density of $0.18\,\mathrm{W/m^2}$. On wasteland, the yield is 5831 per hectare per year. Sources: Francis et al. [2005], Asselbergs et al. [2006]. That's $0.065\,\mathrm{W/m^2}$.

If the niggles are sorted out and 10% of Africa generates 0.065 W/m², and we share this power between six billion people, what do we get? 0.8 kWh/d/p. For comparison, world oil consumption is 80 million barrels per day, which, shared between six billion people, is 23 kWh/d/p. So even if *all* of Africa were covered with jatropha plantations, the power produced would be only one third of world oil consumption.

Cellulosic ethanol and switchgrass

The wonderful "next generation" biofuel? Schmer et al. [2008] found that the net energy yield of switchgrass grown over five years on marginal cropland on 10 farms in the midcontinental US was 60 GJ per hectare per year, which is $0.2\,\mathrm{W/m^2}$. "This is a baseline study that represents the genetic material and agronomic technology available for switchgrass production in 2000 and 2001, when the fields were planted. Improved genetics and agronomics may further enhance energy sustainability and biofuel yield of switchgrass."

Corn-growing in the USA for bioethanol

1 acre ($4050\,\mathrm{m}^2$) produces 122 bushels (per year?), which makes 122×2.6 US gallons of ethanol, which at $84\,000\,\mathrm{BTU}$ per gallon means $780\,\mathrm{kWh}$ per acre per year, which is $0.02\,\mathrm{W/m}^2$ – not taking into account any of the energy losses in processing.

The main research result for bioethanol is that for ethanol to break even, it is essential to make use of coproducts [Shapouri et al., 1995].

Solar biomass: farming byproducts as a coal substitute

We found a moment ago that the power per unit area of a biomass power station burning the best energy crops is $0.2 \,\mathrm{W/m^2}$. If instead we grow

crops for food, and put the left-overs that we don't eat into a power station – or if we feed the food to chickens and put the left-overs that come out of the chickens' back-ends into a power station – what power could be delivered per unit area of farmland? Let's make a rough guess, then take a look at some real data. For a wild guess, let's imagine that by-products are harvested from half of the area of Britain and trucked to power stations., and that general agriculture by-products deliver 10% as much power per unit area as the best energy crops: $0.02 \, \text{W/m}^2$. Multiplying this by $2000 \, \text{m}^2$ (half the area per person) we get 1 kWh per day per person.

Have I been unfair on agricultural garbage in making this wild guess? We can re-estimate the plausible production from agricultural left-overs by scaling up the prototype straw-burning power station at Elean in East Anglia. Elean's power output is 36 MW, and it uses 200 000 tons per year from land located within a 50-mile radius. If we assume this density can be replicated across the whole country, the Elean model offers $0.002\,\mathrm{W/m^2}$. At $4000\,\mathrm{m^2}$ per person, that's $8\,\mathrm{W}$ per person, or $0.2\,\mathrm{kWh/day}$ per person. If power stations like Elean could be packed five times more densely our calculation would have recovered the $1\,\mathrm{kWh}$ per day of my wild guess.

Landfill methane gas

At present, much of the methane gas leaking out of rubbish tips comes from biological materials, especially waste food. So, as long as we keep throwing away things like food and newspapers, landfill gas is a sustainable energy source – plus, burning that methane might be a good idea from a climate-change perspective, since methane is a stronger greenhouse-gas than CO_2 . A landfill site receiving 7.5 million tons of household waste per year can generate $50\,000\,\text{m}^3$ per hour of methane. Source: Matthew Chester, City University, London.

Gas has a calorific value of $38 \, \text{MJ/m}^3$, so this means that with methane capture at all landfill sites, total waste of 0.4 tons per year per person could generate $0.16 \, \text{m}^3$ per day per person of methane, which is $1.7 \, \text{kWh/d}$ per person (of chemical energy). Or $0.7 \, \text{kWh(e)/d}$ per person, assuming conversion to electricity at 40% efficiency.

Burning household waste

Some numbers:

SELCHP ('South East London Combined Heat and Power') http://www.selchp.com/ is a 35 MW(e) power station which receives 420 kt per year of black bag waste from the London area. They are paid £160 per ton of waste. They burn the waste (as a whole, without sorting) and are paid for the electricity (roughly £32 per MWh(e)). Ferrous metals are removed for recycling, hazardous wastes are filtered out and sent to a special landfill

site, and the remaining ash is sent for reprocessing into recycled material for road building or construction use.

The calorific value of the waste is $9000\,\mathrm{kJ/kg}$ (2.5 kWh/kg), and the thermal efficiency of the power station is about 21%, so each 1 kg of waste gets turned into 0.5 kWh(e). The carbon emissions are about $1000\,\mathrm{g\,CO_2}$ per kWh(e).

I don't think they deliver any heat to anyone, so it's not actually a CHP facility, in spite of its name.

Of the 35 MW(e) generated, about 4 MW(e) is immediately used by the plant itself to run its machinery and filtering processes.

Scaling all this per person: if every borough had one of these, and if everyone sent 1 kg per day of waste, then we'd get 0.5 kWh(e) per day per person from waste incineration.

This is similar to the figure estimated above for methane capture at landfill sites. And remember, you can't have both. More waste incineration means less methane gas leaking out of landfill site.

Check this agrees with '5 plans'.

Waste to ethanol

Another technology converts biological waste to liquid fuels with the help of bacteria. The company Ineos Bio claims to be able to convert one dry ton of biomass waste to 400 litres of bioethanol, which has a chemical energy of 2400 kWh. (They refused to disclose how much additional energy inputs their processes require.) 2.4 kWh per kg. If every person gave Ineos 0.5 kg of biomass waste per day, then the ethanol produced would contain 1.2 kWh per day per person.

Forest productivity

Other sources for productivity of forest.

Writing about willow, miscanthus, poplar, etc, not traditional wood: Select Committee on Science and Technology Minutes of Evidence – Memorandum from the Biotechnology & Biological Sciences Research Council. "Typically a sustainable crop of 10 dry t/ha/y of woody biomass can be produced in Northern Europe" "Thus an area of 1 sq km will produce 1000 dry t/y – enough for a power output 150 kWe at low conversion efficiencies or 300 kWe at high conversion efficiencies." (Which means 0.15– $0.3\,W(e)/m^2$.)

Layzell et al. [2006] [3ap71c]

Grain crops contain 13.9 GJ/t (Wet). (wheat, oats, barley, corn)

switch grass: 12 GJ/t(wet). willow: 9.3 GJ/t(wet). agri residues: 12 GJ/t(wet). municipal solid waste: 9.5 GJ/t(wet). wood: 9.3 GJ/t(wet).

Table D.4. Calorific value of wood. Sources: Yaros [1997], Ucuncu [1993].

Wood type		energy density (kWh/kg)
softwood	– air dried	4.4
	 oven dried 	5.5
hardwood	– air dried	3.75
	 oven dried 	5.0
white office	paper	4.0
glossy pape	er	4.1
newspaper		4.9
cardboard		4.5
municipal solid waste		2.6
coal		8

Wheat yields in the UK

In the UK, 7.7 tons per hectare per year. Wheat to bioethanol: 1t wheat makes 3361. That's 0.17 W/m², not accounting for energy inputs required.

Sugar beet: 53 t/ha/y. 1t sugar beet makes 1081 bioethanol. That's $0.4 W/m^2$, not accounting for energy inputs required.

SDC exaggeration – is the word 'radical' appropriate?

[Move to 'presentation' chapter?] "Wood fuel heating could radically cut climate-changing emissions." "On the basis of available evidence, it has been estimated that the wood fuel resource of 700 000 to 1 M odt per year would be able to support between 1.5 and 3.4 TWh per year of delivered energy consumption [my units: 0.8-1.8 kWh/day per person in Scotland; about 2% at most.] – enough to account for between 5% and 11% of domestic space and water heating requirements in Scotland. This would result in carbon savings of from 0.16 to 0.4 million tons of carbon (MtC), or 0.6 to 1.4 million tons of CO_2 (Mt CO_2). [0.12-0.28 tons CO_2 per person per year. About 3% at most of average emissions (10 tons).] Such savings equate to between 7% and 23% of CO_2 emissions from domestic space and water heating in Scotland."

Incidentally, note the conversion rate for thermal heat from wood from these numbers: about 3 MWh/odt, or 3 kWh/kg. (Including wood stove's efficiency.)

See also Laurie Michaelis, "The Real Cost of Liquid Biofuels," The OECD Observer, October/November 1994. [2mxsj9] Laurie Michaelis works in the Energy and Environment Division of the International Energy Agency at the OECD.

D — *Solar II* 307

Statistics for agricultural productivity

In the UK, wheat yield is $8000\,\mathrm{kg}$ per ha per year. Barley: $5800\,\mathrm{kg}$ per ha per year. Livestock per $1000\,\mathrm{ha}$ of utilized agricultural land: $668\,\mathrm{cows}$, $1695\,\mathrm{sheep}$, and $365\,\mathrm{pigs}$.

Criticisms of biofuel farms

"Biofuel farms make CO₂ emissions worse."

E Heating II

A perfectly sealed and insulated building would hold heat for ever and thus would need no heating. The two dominant reasons why buildings lose heat are:

- 1. Conduction heat flowing directly through walls, windows and doors:
- 2. **Ventilation** hot air trickling out through cracks, gaps, or deliberate ventilation ducts.

In the standard model for heat loss, both these heat flows are proportional to the temperature difference between the air inside and outside. For a typical British house, conduction is the bigger of the two losses, as we'll see.

Conduction loss

The rate of conduction of heat through a wall, ceiling, floor, or window is the product of the area of the wall, a measure of conductivity of the wall known in the trade as the "U-value" or thermal transmittance, and the temperature difference:

power loss = area \times *U* \times temperature difference.

The U-value is usually measured in $W/m^2/K$. (One kelvin (1 K) is the same as one degree Celsius (1 °C).) Bigger U-values mean bigger losses of power. The thicker a wall is, the smaller its U-value. Double-glazing is about as good as a solid brick wall. (See table E.)

The U-values of objects that are "in series," such as a wall and its inner lining, can be combined in the same way that electrical conductances combine:

$$u_{\text{series combination}} = 1 / \left(\frac{1}{u_1} + \frac{1}{u_2} \right)$$
.

There's a worked example using this rule on page E.

Ventilation loss

To work out the heat required to warm up incoming cold air, we need the heat capacity of air: $1.2 \, kJ/m^3/K$.

In the building trade, it's conventional to describe the power-losses caused by ventilation of a space as the product of the number of changes N of the air per hour, the volume V of the space in cubic metres, the heat



kitchen	2
bathroom	2
lounge	1
bedroom	0.5

Table E.3. Air changes per hour: typical values of N for draught-proofed rooms. The worst draughty rooms might have N=3 air changes per hour.

E — *Heating II* 309

U-values $(W/m^2/K)$		
old ouildings	modern standards	best methods
	0.45-0.6	0.12
2.4		
2.2		
1.0		
0.6		
	0.45	0.14
0.7		
0.8		
	0.25	0.12
0.9		
0.3		
		1.5
5.0		
2.9		
1.7		
0.7 - 0.9		
	0ld puildings 2.4 2.2 1.0 0.6 0.7 0.8 0.9 0.3 5.0 2.9 1.7	old modern standards 0.45–0.6 2.4 2.2 1.0 0.6 0.45 0.25 0.9 0.3 5.0 2.9 1.7

Table E.2. U-values of walls, floors, roofs, and windows.

capacity C, and the temperature difference ΔT between the inside and outside of the building.

power (watts) =
$$C \frac{N}{1 \, \text{h}} V(\text{m}^3) \Delta T(\text{K})$$
 (E.1)

$$= (1.2 \,\mathrm{kJ/m^3/K}) \frac{N}{3600 \,\mathrm{s}} V(\mathrm{m^3}) \Delta T(\mathrm{K}) \tag{E.2}$$

$$= \frac{1}{3}NV\Delta T. \tag{E.3}$$

Energy loss and temperature demand (degree-days)

Since energy is power \times time, you can write the energy lost by conduction through an area in a short duration as

energy loss = area
$$\times$$
 $U \times (\Delta T \times duration)$,

and the energy lost by ventilation as

$$\frac{1}{3}NV \times (\Delta T \times duration).$$

Both these energy losses have the form

Something
$$\times$$
 ($\Delta T \times$ duration),

where the "Something" is measured in watts per °C. As day turns to night, and seasons pass, the temperature difference ΔT changes; we can think of a long period as being chopped into lots of small durations, during each of which the temperature difference is roughly constant. From duration to duration, the temperature difference changes, but the Somethings don't change. When predicting a space's total energy loss due to conduction and ventilation over a long period we thus need to multiply two things:

- 1. the sum of all the Somethings (adding Area \times *U* for all walls, roofs, floors, doors, and windows, and $\frac{1}{2}NV$ for the volume); and
- 2. the sum of all the Temperature difference × Duration factors (for all the durations).

The first factor is a property of the building measured in watts per °C. I'll call this the *leakiness* of the building. (The leakiness is sometimes called the building's heat-loss coefficient.) The second factor is a property of the weather. This second factor is often expressed as a number of "degreedays," since temperature difference is measured in degrees, and days are a convenient unit for thinking about durations. For example, if your house interior is at 18 °C, and the outside temperature is 8 °C for a week, then we say that that week contributed $10 \times 7 = 70$ degree-days to the $(\Delta T \times Duration)$ sum. I'll call the sum of all the $(\Delta T \times Duration)$ factors the "temperature demand" of a period.

energy lost = leakiness \times temperature demand.

We can reduce our energy loss by reducing the leakiness of the building, or by reducing our temperature demand, or both. The next two sections look more closely at these two factors, using a house in Cambridge as a case-study.

There is a third factor we must also discuss. The lost energy is replenished by the building's heating system, and by other sources of energy such as the occupants, their gadgets, their cookers, and the sun. Focussing on the heating system, the energy energy *delivered* by the heating is not the same as the energy *consumed* by the heating. They are related by the coefficient of performance of the heating system.

energy consumed = energy delivered/coefficient of performance.

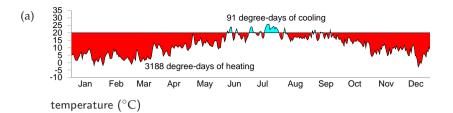
For a condensing boiler burning natural gas, for example, the coefficient of performance is 90%, because 10% of the energy is lost up the chimney.

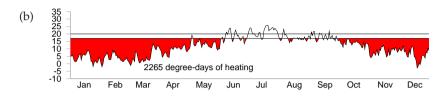
To summarise, we can reduce the energy consumption of a building in three ways:

- 1. by reducing temperature demand;
- 2. by reducing leakiness; or
- © David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

E — Heating II 311

temperature (°C)





3. by increasing the coefficient of performance.

We now quantify the potential of these options. (A fourth option – increasing the building's incidental heat gains, especially from the sun – may also be useful, but I won't address it here.)

Temperature demand

We can visualize the temperature demand nicely on a graph of external temperature versus time. For a building held at a temperature of $20\,^{\circ}\text{C}$, the total temperature demand is the *area* between the horizontal line at $20\,^{\circ}\text{C}$ and the external temperature. In figure E.4a, we see that, for one year in Cambridge, holding the temperature at $20\,^{\circ}\text{C}$ year-round had a temperature demand of 3188 degree-days of heating and 91 degree-days of cooling. These pictures allow us easily to assess the effect of turning down the thermostat and living without air-conditioning. Turning the winter thermostat down to $17\,^{\circ}\text{C}$, the temperature demand for heating drops from 3188 degree-days to 2265 degree-days (figure E.4b), which corresponds to a 30% reduction in heating demand. Turning the thermostat down to $15\,^{\circ}\text{C}$ reduces the temperature demand from 3188 to 1748 degree days, a 45% reduction.

These calculations give us a ballpark indication of the benefit of turning down thermostats, but will only give an exact prediction if we take into account two details: buildings naturally absorb energy from the sun, boosting the inside above the outside temperature, even without any heating; and the occupants and their gadget companions emit heat, so further cutting down the artificial heating requirements. The temperature demand of a location, as conventionally expressed in degree-days, is a bit of an unwieldy thing. I find it hard to remember numbers like "3500 degree-days."

Figure E.4. The temperature demand in Cambridge, 2006, visualized as an area on a graph of daily average temperatures. (a) Thermostat set to 20 °C, including cooling in summer; (b) winter thermostat set to 17 °C.

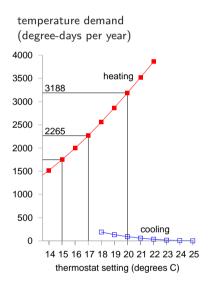


Figure E.5. Temperature demand in Cambridge, in degree-days per year, as a function of thermostat setting (°C). Reducing the winter thermostat from 20 °C to 17 °C reduces the temperature demand of heating by 30%, from 3188 to 2265 degree-days. Raising the summer thermostat from 20 °C to 23 °C reduces the temperature demand of cooling by 82%, from 91 to 16 degree-days.

And academics may find the degree-day a distressing unit, since they already have another meaning for degree days (one involving dressing up in gowns and mortar boards). We can make this quantity more meaningful and perhaps easier to work with by dividing it by 365, the number of days in the year, obtaining the temperature demand in "degree-days per day," or, if you prefer, in plain "degrees." Figure E.8 shows this replotted temperature demand. Expressed this way, the temperature demand is simply the *average* of the temperature difference between inside and outside. The highlighted temperature demands are: 8.7 °C, for a thermostat setting of 20 °C; 6.2 °C, for 17 °C; and 4.8 °C, for 15 °C.

Leakiness – example: my house

My house is a three-bedroom semi-detached house built about 1940 (figure E.6). By 2006, its kitchen had been slightly extended, and most of the windows were double-glazed. The front door and back door were both still single-glazed.

My estimate of the leakiness in 2006 is built up as follows: (I've highlighted the parameters that I altered after 2006, in modifications to be described shortly.)

Surfaces	Area (m²)	U-value (W/m²/°C)	leakiness (W/°C)
Horizontals			
Pitched roof	48	0.6	28.8
Flat roof	1.6	3	4.8
Floor	50	0.8	40
Verticals			
Extension walls	24.1	0.6	14.5
Main walls	50	1	50
Thin wall (5in)	2	3	6
Single-glazed doors and windows	7.35	5	36.7
Double-glazed windows	17.8	2.9	51.6
Total thermal leakiness			232.4

I've treated the central wall of the semi-detached house as a perfect insulating wall, but this may be wrong if the gap between the adjacent houses is actually well-ventilated.





Figure E.6. My house.

313 E — Heating II

Spaces	Volume (m ³)	N (airchanges per hour)	leakiness (W/°C)
Bedrooms	80	0.5	13.3
Kitchen	36	2	24
Hall	27	3	27
Other rooms	77	1	25.7
Total ventilation	n leakines	s	90

The total leakiness of the house is 322 W/°C, with conductive leakiness accounting for 72% and ventilation leakiness for 28%. The conductive leakiness is roughly equally divided into three parts: windows; walls; and floor and ceiling.

We can also express the leakiness as $7.7 \,\text{kWh/d/}^{\circ}\text{C}$.

One way of presenting the leakiness that allows one dwelling to be compared with another is to divide the leakiness by the floor area; this gives the heat-loss parameter of the dwelling, which is measured in $W/^{\circ}C/m^{2}$. The heat-loss parameter of this house (total floor area 88 m²) is

$$3.7 \, \text{W}/^{\circ} \text{C}/\text{m}^{2}$$
.

Let's use these figures to estimate the house's daily energy consumption on a cold winter's day, and year-round.

Assuming an external temperature of -1 °C and an internal temperature of 19 °C, the temperature difference is $\Delta T = 20$ °C. If this difference is maintained for 6 hours per day then the energy lost per day is

$$322 \,\mathrm{W}/^{\circ}\mathrm{C} \times 120 \,\mathrm{degree\text{-}hours} \simeq 39 \,\mathrm{kWh}.$$

If the temperature is maintained at 19 °C for 24 hours per day, the energy lost per day is

To get a year-round heat-loss figure, we can take the temperature demand of Cambridge from figure E.4(c). With the thermostat at 19 °C, the temperature demand in 2006 was 2866 degree-days. The average rate of heat loss, if the house is always held at or above 19 °C, is therefore:

$$7.7 \,\mathrm{kWh/d/^{\circ}C} \times 2866 \,\mathrm{degree-days/y/(365 \,days/y)} = 61 \,\mathrm{kWh/d.}$$

Turning the thermostat down to 17 °C, the average rate of heat loss drops to 48 kWh/d. Turning it up to a tropical 21 °C, the average rate of heat loss is $75 \, \text{kWh/d}$.

What's a reasonable thermostat setting to aim for? Nowadays many people seem to think that 17 °C is unbearably cold. However, the average internal temperature in British houses in 1970 was 13 °C! A human's perception of whether they feel warm enough depends on what they are doing, and what they've been doing for the last hour or so. My suggestion

The predicted reductions break down as follows (on a cold winter day):

- Ventilation reductions in hall and kitchen from 2.9 kWh/d improvements to doors and windows
- Reduction in conduction from double-glazing 1.9 kWh/d two doors and one window
- Cavity-wall insulation (applicable to two-thirds 4.8 kWh/d of the wall area)
- Improved roof insulation
 3.5 kWh/d

is, rather than fixing the thermostat to a single value, to try setting it to a low value most of the time (say 13 or 15 $^{\circ}$ C), and turn it up for a few hours whenever you feel cold.

Effects of extra insulation

During 2007, I made the following modifications to the house:

- 1. Added cavity-wall insulation (which was missing in the main walls of the house). (Add Reference to photo.)
- 2. Increased the insulation in the roof.
- 3. Added a new front door outside the old. (Add photo of new door)
- 4. Replaced the back door with double-glazed one.
- 5. Double-glazed the one window that was still single-glazed.

What's the predicted change in heat loss?

The total leakiness was 322 W/°C.

Adding cavity-wall insulation (new U-value 0.6) to the main walls reduces the house's leakiness by $20\,\mathrm{W/^\circ C}$. The improved loft insulation (new U-value 0.3) should reduce the leakiness by $14\,\mathrm{W/^\circ C}$. The glazing modifications (new U-value 1.6–1.8) should reduce the conductive leakiness by $23\,\mathrm{W/^\circ C}$, and the ventilation leakiness by something like $24\,\mathrm{W/^\circ C}$. That's a total reduction in leakiness of 25%, from roughly 320 to $240\,\mathrm{W/^\circ C}$ (7.7 to $6\,\mathrm{kWh/d/^\circ C}$).

The heat-loss parameter of this house (total floor area $88\,\text{m}^2$) is thus hopefully reduced from 3.7 to $2.7\,\text{W}/^\circ\text{C}/\text{m}^2$. (This is a long way from the $1.1\,\text{W}/^\circ\text{C}/\text{m}^2$ required of a "sustainable" house in the new building codes.)

It's frustratingly hard to make a really big dent in the leakiness of an already-built house! As we saw a moment ago, a much easier way of achieving a big dent in heat loss is to turn the thermostat down. Turning down from 20 to $17\,^{\circ}\text{C}$ gave a reduction in heat loss of 30%.

Combining these two actions – the physical modifications and the turning-down of the thermostat – this model predicts that heat loss should be reduced by nearly 50%. Since some heat is generated in a house by sunshine,

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

Table E.7.

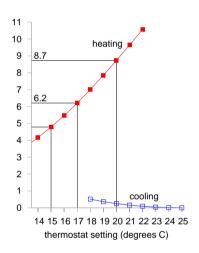


Figure E.8. The temperature demand in Cambridge, 2006, replotted in units of degree-days per day, also known as degrees. In these units, the temperature demand is just the average of the temperature difference between inside and outside.

gadgets, and humans, the reduction in the heating bill should be more than 50%.

I made all these changes to my house and monitored my meters every week. I can confirm that my heating bill indeed went down by more than 50%. My gas consumption has gone down from $40 \, \text{kWh/d}$ to $13 \, \text{kWh/d}$ – a reduction of 67%.

Leakiness reduction by internal wall-coverings

Can you reduce your walls' leakiness by covering the *inside* of the wall with insulation? The answer is yes, but there may be two complications. First, the thickness of internal covering is bigger than you might expect. To transform an existing nine-inch solid brick wall (U-value 2.2 W/m²/K) into a decent 0.30 W/m²/K wall, roughly 6 cm of insulated lining board is required. [65h3cb] Second, condensation may form on the hidden surface of such internal insulation layers, leading to damp problems.

If you're not looking for such a big reduction in wall leakiness, you can get by with a thinner internal covering. For example, you can buy 1.8-cm-thick insulated wallboards with a U-value of $1.7\,\mathrm{W/m^2/K}$. With these over the existing wall, the U-value would be reduced from $2.2\,\mathrm{W/m^2/K}$ to:

$$1/\left(\frac{1}{2.2} + \frac{1}{1.7}\right) \simeq 1 \,\text{W/m}^2/\text{K}.$$

Definitely a worthwhile reduction.

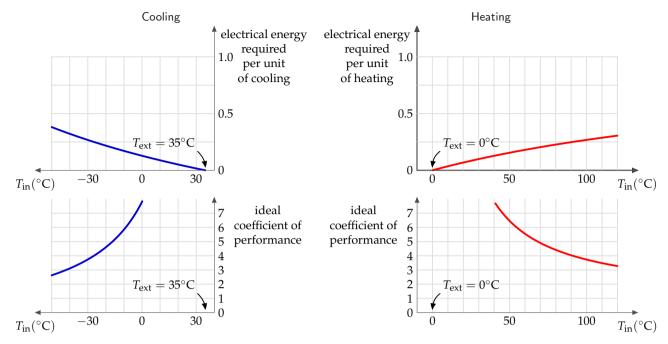
Improving the coefficient of performance

You might think that the coefficient of performance of a condensing boiler, 90%, sounds pretty hard to beat. But it can be significantly improved upon, by heat pumps. Whereas the condensing boiler takes chemical energy and turns 90% of it into useful heat, the heat pump takes some electrical energy and uses it to *move* heat from one place to another (for example, from outside a building to inside). Usually the amount of useful heat delivered is much bigger than the amount of electricity used. A coefficient of performance of 3 or 4 is normal.

Theory of heat pumps

A full explanation would require a discussion of entropy.

more here For the time being, I'll just give the formulae for the ideal efficiency, that is, the electrical energy required per unit of heat pumped. If we are pumping heat from an outside place at temperature T_1 into a place at higher temperature T_2 , both temperatures being expressed relative to absolute zero (that is, T_2 , in kelvin, is given in terms of the Celsius



temperature T_{in} , by $273.15 + T_{in}$).

efficiency =
$$1 - \frac{T_1}{T_2}$$

If we are pumping heat out from a place at temperature T_2 to a warmer exterior at temperature T_1 , the ideal efficiency is

efficiency =
$$\frac{T_1}{T_2} - 1$$
.

Ground-source heat pumps are discussed more in Chapter 21.

Performance figures in the UK

The largest drop in the the estimated coefficient of performance occurs when ideal heat exchangers are replaced by practical heat exchangers – ones both small enough to get through the door of a house and cheap enough to cost less than the house.

[Wheatley et al., 1986]

An office heating/cooling unit, using external air as the heat source or sink, says in its blurb that it uses up to $0.83\,\mathrm{kW}(e)$ when heating and delivers $3.6\,\mathrm{kW}$. Or when cooling, it uses $0.62\,\mathrm{kW}(e)$ and delivers $2.6\,\mathrm{kW}$. The ratio of heat pumped in or out to power required is called the coefficient of performance. Both ratios are a bit more than 4. According to Wheatley

Figure E.9. Ideal heat pump efficiencies. Top left: ideal electrical energy required, according to the limits of thermodynamics, to pump heat out of a place at temperature T_{in} when the heat is being pumped to a place at temperature $T_{\text{out}} = 35 \,^{\circ}\text{C}$. Right: ideal electrical energy required to pump heat into a place at temperature $T_{\rm in}$ when the heat is being pumped from a place at temperature $T_{\text{out}} = 0$ °C. Bottom row: the efficiency is conventionally expressed as a "coefficient of performance," which is the heat pumped per unit electrical energy. In practice, ground-source heat pumps and the best air-source heat pumps have a coefficient of performance of 3

E — Heating II 317

et al. [1986], however, we should expect any air-source heat pump based on the standard Rankine cycle working between temperatures of 5 and $20\,^{\circ}$ C (and thus having its cold and hot sides at -5 and $45\,^{\circ}$ C) to have a coefficient of performance of 3 or at most 4.

A domestic ground-source heat pump with an output temperature of $45\,^{\circ}\text{C}$ and output power of $4\,\text{kW}$, collecting heat from a 200-m ground loop buried just 1-m deep, had a coefficient of performance of 3.16. This domestic system included a 90-W distribution pump which ran non-stop all year round. Performance would have been better (a coefficient of performance of 3.43) if the pump had switched off when not needed. The ground collector collects heat at a rate of about 20 or 30 W per metre of collector length. [5mo7fd]

These anecdotal examples suggest that, while in theory ground-source heat pumps might have better performance than air-source, in practice an air-source heat pump might be the best and simplest choice. In cities, there may be uncertainty about the future effectiveness of ground-source heat pumps, because the more people use them in winter, the colder the ground gets; this thermal fly-tipping problem may also show up in the summer in cities where too many buildings use ground-source (or should I say "ground-sink"?) heat pumps for air-conditioning.



Figure E.10. Great Oak Cohousing project, Ann Arbor, Michigan.

Notes

page no.

[K-value is conductivity, usually measured in W/m/K, for example 0.023 W/m/K. Sometimes called λ -value? R-value is thermal resistance (the inverse of U-value), usually measured in m²K/W.]

air-changes The recommended minimum rate of air exchange is between 0.5 and 1.0 air changes per hour, providing adequate fresh air for human health, for safe combustion of fuels and to prevent damage to the building fabric from excess moisture in the air (EST 2003).

313 The average internal temperature in British houses in 1970 was 13 °C! [Department of Trade and Industry, 2002a, para 3.11]

What about the other things in the house that are involved in heating up and cooling down?

Heat capacity of asphalt, brick, concrete, glass, granite, marble, sand, soil: all around $0.85\,kJ/kg/K$. Very close to air's $1\,kJ/kg/K$. Wood: $0.4\,kJ/kg/K$. Iron: $0.45\,kJ/kg/K$.

Chairs: 10 at 5 kg. Sofa: 60 kg. Tables: 30 kg. Cabinets: 50 kg. China: 50 kg. Everything: maybe a ton of stuff, similar to wood? So warming a ton of stuff has an energy cost of $1000 \, \text{kg} \times 20 \, ^{\circ}\text{C} \times 0.4 \, \text{kJ/m}^3/^{\circ}\text{C} = 8000 \, \text{kJ} = 3 \, \text{kWh}$. So the stuff dominates the air, heating-wise.

Air-exchange

Once a building is really well insulated, the principal loss of heat will be through ventilation (air changes) rather than through conduction. The heat loss through ventilation can be reduced by transferring the heat from the outgoing air to the incoming air. Remarkably, a great deal of this heat can indeed be transferred without any additional energy being required. The trick is to use a nose, as discovered by natural selection. A nose warms incoming air by cooling outgoing air. There's a temperature gradient along the nose; the walls of a nose are coldest near the nostrils. The longer your nose, the better it works as a counter-current heat exchanger. Noses also use the same principle to reduce water-loss. In nature's noses, the direction of the air-flow usually alternates. Another way to organize a nose is to have two air-passages, one for in-flow and one for out-flow, separate from the point of view of air, but tightly coupled or intertwined with each other so that heat can easily flow. This is how the noses work in buildings. It's conventional to call these noses heat-exchangers.

Ground storage from summer to winter

A spike of heat put down a hole in the ground will spread as

$$\frac{1}{\sqrt{4\pi\kappa t}}\exp\left(-\frac{x^2}{4(\kappa/(C\rho))t}\right)$$

where κ is the conductivity of the ground, C is its heat capacity, and ρ is its density. This describes a bell-shaped curve with width

$$\sqrt{2\frac{\kappa}{C\rho}t};$$

for example, after a time $t=1.6\times 10^7\,\mathrm{s}$ (six months), using the figures for granite ($C=0.82\,\mathrm{kJ/kg/K}$, $\rho=2500\,\mathrm{kg/m^3}$, $\kappa=2.1\,\mathrm{W/m/K}$), the width is 6 m.

Using the figures for water ($C = 4.2 \,\text{kJ/kg/K}$, $\rho = 1000 \,\text{kg/m}^3$, $\kappa = 0.6 \,\text{W/m/K}$), the width is 2 m.

So if the storage region is bigger than $20 \,\text{m} \times 20 \,\text{m} \times 20 \,\text{m}$ then most of the heat stored will still be there in six months time.

Two other constraints force the dimensions of the storage region: it must be big enough to hold all the energy that we want to leave there, and it must have enough surface area exposed to our pipes for us to be able to get the heat in.

An energy-efficient house

In 1984, an energy consultant, Alan Foster, built an energy-efficient house near Cambridge; he kindly gave me his thorough measurements. The

(W/1	m/K)
water	0.6
quartz	8
granite	2.1
earth's crust	1.7
dry soil	0.14

Table E.11. Thermal conductivities.

E — Heating II 319

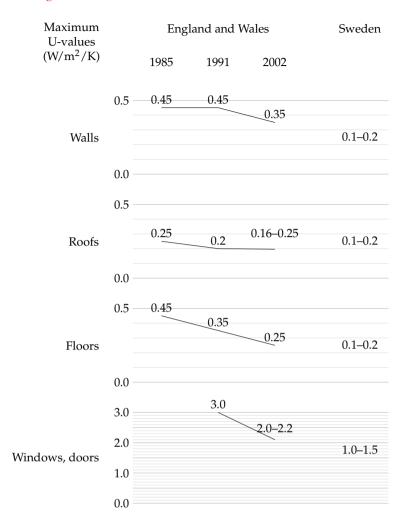


Figure E.12. U-values required by British and Swedish building regulations.

house is a timber-framed bungalow based on a Scandinavian "Heatkeeper Serrekunda" design, with a floor area of 140 m², composed of three bedrooms, a study, two bathrooms, a living room, a kitchen, and a lobby. The wooden outside walls were supplied in kit form by a Scottish company, and the main parts of the house took only a few days to build.

The walls are 30 cm thick and have a U-value of 0.28. From the inside out, they consist of 13 mm of plasterboard, 27 mm airspace, a vapour barrier, 8 mm of plywood, 90 mm of rockwool, 12 mm of bitumen-impregnated fibreboard, 50 mm cavity, and 103 mm of brick. The external bricks are not load-bearing. The ceiling construction is similar with 100–200 mm of rockwool insulation. The ceiling has a U-value of $0.27 \, \text{W/m}^2/^{\circ}\text{C}$, and the floor, $0.22 \, \text{W/m}^2/^{\circ}\text{C}$. The windows are double-glazed (U-value $2 \, \text{W/m}^2/^{\circ}\text{C}$), with the inner panes' outer surfaces specially coated to reduce radiation. The windows are arranged to give substantial solar gain, contributing about

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

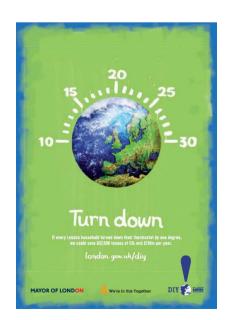


Figure E.13. Advertisement from the Mayor of London's "DIY planet repairs" campaign of 2007. The text reads "Turn down. If every London household turned down their thermostat by one degree, we could

30% of the house's space-heating.

The house is well sealed, every door and window lined with neoprene gaskets. The house is heated by warm air pumped through floor grilles; in winter, pumps remove used air from several rooms, exhausting it to the outside, and they take in air from the loft space. The incoming air and outgoing air pass through a heat exchanger, which saves 60% of the heat in the extracted air. The heat exchanger is a passive device, using no energy: it's like a big metal nose, warming the incoming air with the outgoing air. On a cold winter's day, the outside air temperature was $-8\,^{\circ}\text{C}$, the temperature in the loft's air intake was $0\,^{\circ}\text{C}$, and the air coming out of the heat exchanger was at $+8\,^{\circ}\text{C}$.

For the first decade, the heat was supplied entirely by electric heaters, heating a 150-gallon heat store during the overnight economy period. More recently a gas supply was brought to the house, and the space heating was obtained from a condensing boiler.

The heat loss through conduction and ventilation is $4.2 \, kWh/d/^{\circ}C$. The heat loss parameter (the leakiness per square metre of floor area) is $1.25 \, W/m^2/^{\circ}C$ (cf. my house's $2.7 \, W/^{\circ}C/m^2$).

With the house occupied by two people, the average space-heating consumption, with the thermostat set at 19 or $20\,^{\circ}\text{C}$ during the day, was $8100\,\text{kWh}$ per year, or $22\,\text{kWh/d}$; the total energy consumption for all purposes was about $15000\,\text{kWh}$ per year, or $40\,\text{kWh/d}$. Expressed as an average power per unit area, that's $6.6\,\text{W/m}^2$.

The German Passivhaus standard aims for power consumption for heating and cooling of $15 \, \text{kWh/m}^2/\text{y}$, which is $1.7 \, \text{W/m}^2$; and total power consumption of $120 \, \text{kWh/m}^2/\text{y}$, which is $13.7 \, \text{W/m}^2$.

Benchmarks for offices

The average energy consumption of the UK service sector, per unit floor area, is $30 \,\text{W/m}^2$.

An energy-efficient office

The National Energy Foundation built themselves a low-cost low-energy building. It has solar panels for hot water, solar photovoltaic (PV) panels generating up to $6.5\,\mathrm{kW}$ of electricity, and is heated by a 14-kW ground-source heat pump and occasionally by a wood stove. The floor area is $400\,\mathrm{m}^2$ and the number of occupants is about 30. It is a single-storey building. The walls contain $300\,\mathrm{mm}$ of rockwool insulation. The heat-pump's coefficient of performance in winter was 2.5. The energy used is $65\,\mathrm{kWh}$ per year per square metre of floor area $(7.4\,\mathrm{W/m^2})$. The PV system delivers almost 20% of this energy.

E — Heating II 321

Contemporary offices

Cambridge University built two new office buildings about the same time.

Roger Needham Building, Cambridge. (holds computer science researchers and administrators.) Area: 7216 m². Consumption 1923 MWh/y, or 266 kWh/y/m², or 0.73 kWh/d/m², or 30 W/m². Roughly 150 people work there on average. 35 kWh/d per person. "The Roger Needham building is designed for low energy consumption with a high degree of of spatial flexibility and comfort in order to adapt to future research trends and practices. The building has no conventional heating system, and cooling is achieved through chilled beams. The omission of heating system and choice of cooling system will minimize greenhouse gas emission and this building will set a new low energy standard for a computer building in the UK." [5r6c7t]

William Gates building: holds computer science researchers, administrators, and a small café. Roughly 274 people work there. 11110 m². 1982 MWh/y. 178 kWh/m²/y, or 20 W/m². And 20 kWh/d per person. This building won a RIBA award in 2001 for its predicted energy consumption. "The architects have incorporated many environmentally friendly features into the building." [5dhups]

But are these buildings impressive? Next door, the Rutherford building, designed in the 1970s without any fancy eco-claims – indeed without even double glazing – has a floor area of 4998 $\rm m^2$ and consumes 1096 MWh per year; that's $0.6\,\rm kWh/d/m^2$, or $25\,\rm W/m^2$. Roughly 200? people work there. So that's $15\,\rm kWh/d$ per person.

Further reading: Hastings and Wall [2006].

Thermal mass

Does increasing the thermal mass of a building help reduce its heating and cooling bills? It depends. The outdoor temperature can vary during the day by about 10 °C. A building with large thermal mass – thick stone walls, for example – will naturally ride out those variations in temperature, and, without heating or cooling, will have a temperature close to the average outdoor temperature. Such buildings, in the UK, need neither heating nor cooling for many months of the year. In contrast, a poorly-insulated building with low thermal mass might be found too hot during the day and too cool at night, leading to greater expenditure on cooling and heating.

However, large thermal mass is not always a boon. If a room is occupied in winter for just a couple of hours a day (think of a lecture room for example), the energy cost of warming the room up to a comfortable temperature will be greater, the greater the room's thermal mass. This extra invested heat will linger for longer in a thermally massive room, but if nobody is there to enjoy it, it's wasted heat. So in the case of infrequently used rooms it makes sense to aim for a structure with low thermal mass,

and to warm that small mass rapidly when required.

Heating and the ground

Here's an interesting calculation to do. Imagine having solar heating panels on your roof, and, whenever the water in the panels gets above 50°C , pumping the water through a large rock under your house. When a dreary grey cold month comes along, you could then use the heat in the rock to warm your house. Normal ground-source heat pumps are different from this scheme in two ways: they don't usually bother with the solar heating panels and they use a cunning electrical pump to boost the heat flow from the rock into the building. But before we discuss them, let's do this simple calculation for the solar scheme: roughly how big a 50°C rock would you need to hold enough energy to heat a house for a whole month? Let's assume we're after $24\,\text{kWh}$ per day for 30 days and that the house is at 16°C . The heat capacity of granite is $0.195 \times 4200\,\text{J/kg/K} = 820\,\text{J/kg/K}$. The mass of granite required is:

mass =
$$\frac{\text{energy}}{\text{heat capacity} \times \text{temperature difference}}$$

= $\frac{24 \times 30 \times 3.6 \text{ MJ}}{(820 \text{ J/kg/°C})(50 \text{ °C} - 16 \text{ °C})}$
= $100 000 \text{ kg}$,

one hundred tonnes, which corresponds to a cuboid of rock of size $6\,\text{m} \times 1\,\text{m}$.

What *area* of interface is needed in order to dump or extract energy? Just to get a rough estimate, let's assume we need to dump $24\,\mathrm{kWh}$ into rock during one hour, and that the temperature difference is $10\,^\circ\mathrm{C}$ – over what length-scale? Conductivity of granite: $2.1\,\mathrm{W/m/K}$.

This incomplete calculation overlaps the one on page 322

Ground source heat pumps – limits

Assume that we have a neighbourhood with quite a high population density. Can *everyone* use ground-source heat pumps, without using the summer replenishment trick? For this calculation, I'll assume the ground just below the surface is held at a steady temperature by the combined influence of sun, air, cloud, and night sky. I'll assume that we put the ground loops in a layer $h=5\,\mathrm{m}$ deep – much shallower, and the ground temperature would fluctuate more during the year, reducing the pump's efficiency; much deeper, and the resulting temperature drop induced by our heat pump would reduce efficiency too. (Redo this, showing what the optimal depth actually is?) I'll assume that we'll allow ourselves to suck the ground temperature down to $\Delta T=5\,^{\circ}\mathrm{C}$ below the average ground

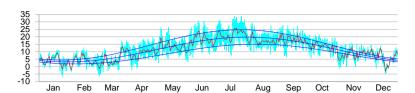
© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

Heat capacity: $C = 820 \, \text{J/kg/K}$ Conductivity: $\kappa = 2.1 \, \text{W/m/K}$ Density: $\rho = 2750 \, \text{kg/m}^3$ Heat capacity per unit volume: $C_V = 2.3 \, \text{MJ/m}^3/\text{K}$

Table E.14. Vital statistics for granite. (I use granite as an example of a typical rock.)

E — Heating II 323

temperature (°C)



temperature at the surface. We can then use the assumed conductivity to deduce the heat flux from the surface:

Flux = Conductivity
$$\times \frac{\Delta T}{h} = 2 \text{ W/m}^2$$
.

Let's pick $6200/\mathrm{km}^2$ as our representative density of a residential area; that's $160\,\mathrm{m}^2$ per person. This is the population density of a typical English suburb: rows of semi-detached houses with about $400\,\mathrm{m}^2$ per house (including pavements and streets). Then the maximum power per person deliverable by ground source heat pumps, if everyone in a neighbourhood has them, is $320\,\mathrm{W}$, which is $8\,\mathrm{kWh/d}$ per person. Add in the electrical contribution, assuming a COP of 3: $12\,\mathrm{kWh/d}$ per person.

If I'd said depth = $1.25\,\text{m}$ then the flux could be $8\,\text{W/m}^2$, and the maximum power delivered could be $48\,\text{kWh/d}$ per person. But bear in mind I assumed that the ground is granite all the way through. The conductivity of dry soil is about ten times smaller than that of granite.

Ground source heat pumps – details

WARNING: this section is intended for an undergraduate science audience.

Let's work out a cartoon theory for below-ground temperatures, and for what happens when we lay down tubes and suck out heat.

I'm going to assume the ground is made of granite.

Response to external temperature

If we assume the ground is made of solid homogenous granite, then the temperature at depth z below the ground and time t responds to the imposed temperature at the surface in accordance with the diffusion equation

$$\frac{\partial T(z,t)}{\partial t} = \frac{\kappa}{C_{\rm V}} \frac{\partial^2 T(z,t)}{\partial z^2}.$$
 (E.4)

For a sinusoidal imposed temperature with frequency ω and amplitude A imposed at depth z=0,

$$T(0,t) = T_{\text{surface}}(t) = T_{\text{average}} + A\cos(\omega t),$$
 (E.5)

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

Figure E.16. The temperature in Cambridge, 2006, and a cartoon, which says the temperature is the sum of an annual sinusoidal variation between 3 °C and 20 °C, and a daily sinusoidal variation with range up to 10.3 °C. The average temperature is 11.5 °C.

	People per km ²
Bangalore	26719
Manhattan	25 849
Paris	24 775
Chelsea	15 177
Tokyo	13 800
Moscow	10 275
Taipei	9626
The Hague	6600
San Francisco	6423
Singapore	6411
Cambridge M	A 6086
Sydney	5736
Portsmouth	4689

Table E.15. Some urban population densities.

the resulting temperature at depth z and time t is a decaying and oscillating function

$$T(z,t) = T_{\text{average}} + A e^{-z/z_0} \cos(\omega t - z/z_0), \tag{E.6}$$

where z_0 is the characteristic length-scale of both the decay and the oscillation,

$$z_0 = \sqrt{\frac{2\kappa}{C_V \omega}}. (E.7)$$

For daily variations, this characteristic length-scale is $z_0=0.16\,\mathrm{m}$. (So 32 cm of rock is what you need to ride out external daily temperature fluctuations.) For yearly variations, the characteristic length-scale is $z_0=3\,\mathrm{m}$. At a depth of $2z_0$, the variations in temperature are one seventh of those at the surface, and lag them by about one third of a cycle (figure E.17). At a depth of $3z_0$, the variations in temperature are one twentieth of those at the surface, and lag them by half a cycle.

The flux of heat (the power per unit area) at depth z is

$$\kappa \frac{\partial T}{\partial z} = \kappa \frac{A}{z_0} \sqrt{2} e^{-z/z_0} \sin(\omega t - z/z_0 - \pi/4).$$

For example, at the surface, the peak flux is

$$\kappa \frac{A}{z_0} \sqrt{2} = A \sqrt{C_V \kappa \omega},$$

which for the yearly driving signal of amplitude A = 8.3 °C corresponds to 8 W/m^2 .

This flux is a useful benchmark, giving guidance about what sort of power we could expect to extract with a ground source heat pump. If we suck a flux significantly smaller than $8\,\text{W/m}^2$, the perturbation we introduce to the natural flows will be small. If on the other hand we try to suck a flux bigger than $8\,\text{W/m}^2$, we should expect that we'll be shifting the temperature of the ground significantly away from its natural value, and such fluxes may be impossible to demand.

If, as on p323, we pick 160 m² per person as our representative density of a residential area, we deduce that a ballpark limit for heat pump power delivery is

$$8\,\text{W/m}^2\times 160\,\text{m}^2=1300\,\text{W}=31\,\text{kWh/d}$$
 per person.

This is uncomfortably close to the sort of power we would like to deliver in winter-time: it's plausible that our peak winter-time demand for hot air and hot water might be $48\,\mathrm{kWh/d}$ per person.

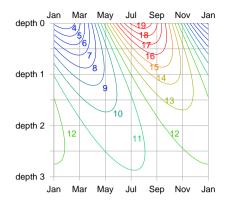


Figure E.17. Temperature (in $^{\circ}$ C) versus depth and time. The depths are given in units of the characteristic depth z_0 , which for granite and annual variations is 3 m.

depth 0 surface depth 1 3 m depth 2 6 m

depth 3 9 m

At "depth 2" (6 m), the temperature is always about 11 or 12 °C. At "depth 1" (3 m), it wobbles between 8 and 15 °C.

F Waves II

The physics of deep-water waves

Waves contain energy in two forms: potential energy, and kinetic energy. The potential energy is the energy required to move all the water from the troughs to the peaks. The kinetic energy is associated with the water moving around.

People sometimes assume that when the crest of a wave moves across an ocean at 30 miles per hour, the water in that crest must also be moving at 30 miles per hour in the same direction. But this isn't so. It's just like a Mexican wave. When the wave rushes round the stadium, the humans who are making the wave aren't themselves moving round the stadium: they just bob up and down a little. The motion of a piece of water in the ocean is similar: if you focussed on a bit of seaweed floating in the water as waves go by, you'd see that the seaweed moves up and down; at the same time it moves a little to and fro in the direction of travel of the wave – the exact effect could be recreated in a Mexican wave if people moved like window-cleaners, polishing a big piece of glass in a circular motion. The wave has potential energy because of the elevation of the crests above the troughs. And it has kinetic energy because of the small circular bobbing motion of the water.

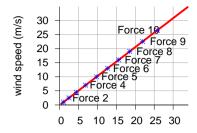
Our rough calculation of the power in ocean waves will require three ingredients: an estimate of the period T of the waves (the time between crests), an estimate of the height h of the waves, and a physics formula that tells us how to work out the speed v of the wave from its period.

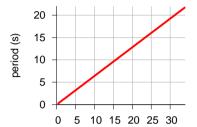
The wavelength λ and period of the waves (the distance and time respectively between two adjacent peaks) depend on the speed of the wind that creates the waves as shown in figure F.1. The height of the waves doesn't depend on the windspeed; rather, it depends on how long the wind has been caressing the water surface.

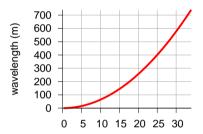
You can estimate the period of ocean waves by recalling the time between waves arriving on an ocean beach. Is 10 seconds reasonable? For the height of ocean waves, let's assume an amplitude of 1 m, which means 2 m from trough to peak. In waves this high, a man in a dinghy can't see beyond the nearest crest when he's in a trough; I think this height is bigger than average, but we can revisit this estimate if we decide it's important. The speed of deep-water waves is related to the time *T* between peaks by

$$v = \frac{gT}{2\pi}.$$

(This formula is explained in this chapter's end-notes.) For example, if T=10 seconds, then $v=16\,\mathrm{m/s}$. The wavelength of such a wave – the distance between crests – is $\lambda=vT=gT^2/2\pi=160\,\mathrm{m}$, where is the acceleration of gravity (9.8 m/s²).







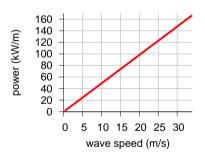
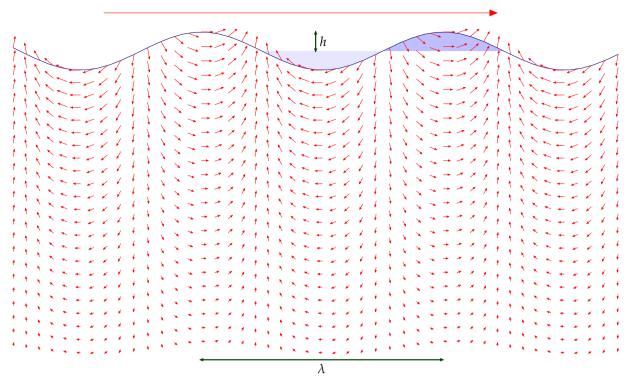


Figure F.1. Facts about deep-water waves. In all four figures the horizontal axis is the wave speed in m/s. From top to bottom the graphs show: wind speed (in m/s) required to make a wave with this wave speed; period (in seconds) of a wave; wavelength (in m) of a wave; and power density (in kW/m) of a wave with amplitude 1 m.



If a wave of wavelength λ passes by every T=10 seconds, and if the height of each peak and depth of each trough is h=1 m, then the potential energy passing per unit time, per unit length, is

$$P_{\text{potential}} \simeq m^* g \bar{h} / T,$$
 (F.1)

where m^* is the mass per unit length, which is roughly $\frac{1}{2}\rho h(\lambda/2)$ (approximating the area of the shaded crest in figure F.2 by the area of a triangle), and \bar{h} is the change in height of the centre-of-mass of the chunk of elevated water, which is roughly h. So

$$P_{\text{potential}} \simeq \frac{1}{2}\rho h \frac{\lambda}{2} gh/T.$$
 (F.2)

And λ/T is simply the speed at which the wave travels, v, so:

$$P_{\rm potential} \simeq \frac{1}{4} \rho g h^2 v.$$
 (F.3)

Now waves have kinetic energy as well as potential energy, and, remarkably, these are exactly equal; so the total power of the waves is double the power calculated from potential energy.

$$P_{\text{total}} \simeq \frac{1}{2} \rho g h^2 v.$$
 (F.4)

Figure F.2. A wave has energy in two forms: potential energy associated with raising water out of the light-shaded troughs into the heavy-shaded crests; and kinetic energy of all the water within a few wavelengths of the surface – the speed of the water is indicated by the small arrows. The speed of the wave, travelling from left to right, is indicated by the much bigger arrow at the top.

327

Plugging in $v = 16 \,\mathrm{m/s}$ and $h = 1 \,\mathrm{m}$, we find

$$P_{\text{total}} \simeq \frac{1}{2} \rho g h^2 v = 80 \,\text{kW/m}. \tag{F.5}$$

Are ocean waves usually two metres high from peak to trough every day? As I said, that sounds quite big. We should certainly allow for some calmer days. Let's halve this estimate to obtain our average estimate of wave power:

Wave power (average) = $40 \,\text{kW/m}$.

This rough estimate agrees with real measurements in the Atlantic [Mollison, 1986]. (See p79.)

Real wave power systems

Deep-water devices

How effective are real systems at extracting power from waves? Stephen Salter's "duck" has been well characterized: a row of 16-m diameter ducks sucks about 50% of the power out of incoming Atlantic waves, and the efficiency of the remaining steps (conversion to electricity, and transmission to a "hydrodynamically underprivileged area" such as London) is about 60%. So if we completely fill half of the 1000 km of exposed Atlantic deep-seacoastline with 50% efficient ducks, followed by 60% conversion and transmission efficiency, we get $40\,\mathrm{kW/m} \times (1/2) \times 0.5 \times 0.6 \times 10^6\mathrm{m} = 6\,\mathrm{GW}$ or $2.4\,\mathrm{kWh/d}$ per person.

Memorable figures: deep water Salter Ducks, feeding off 45 MW/km, deliver 19 MW/km, including transmission to central Scotland [Mollison, 1986].

From Mollison [1986]: "The large scale resource of the NE Atlantic, from Iceland to North Portugal, has a net resource of 40–50 MW/km, of which 20–30 MW/km is potentially economically extractable." Using a conservative mean output estimate of 15–20 MW/km, the potential power delivered is UK: 12 GW (100 TWh/y, or 5 kWh/d per person); Ireland: 12 GW; Faeroes, France, Spain, Portugal: 5–8 GW each.

The Pelamis device, created by Ocean Power Delivery, has taken over the Salter duck's mantle as the leading floating deep-water wave device. Each snake-like device is 130 m long and is made of a chain of four segments, each 3.5 m in diameter. It has a maximum power output of 750 kW. The Pelamises are designed to be moored in a depth of about 50 m. In a wavefarm, 39 devices in three rows would face the principal wave direction, occupying a square km of ocean, about 400 m deep and 2.5 km wide. The effective cross-section of a single Pelamis is 7 m (i.e., for good waves, it extracts 100% of the energy that would cross 7 m). The company says that such a wave-farm would deliver about 10 kW/m (10 MW/km).

If 50% of the exposed Atlantic deep-sea coastline (500 km) were occupied by Pelamis wave-farms (a total of 7500 devices in 200 wavefarms) then the power delivered would be 5 GW, or 2 kWh/d per person in the UK.

What is the mass of each device? 700 tons, including 350 or 400 tons of ballast. Compare with the steel-requirements for offshore wind: An offshore wind-turbine with a maximum power of 3 MW weighs 500 tons, including its foundation. So the total weight per kW of a wave-machine, half a ton per kW, is not much bigger than that of a wind-turbine.

Shallow-water devices

Typically 70% of energy in ocean waves is lost through bottom-friction as the depth decreases from 100 m to 15 m. So the average wave-power per unit length of coastline in shallow waters is reduced to about 12 kW/m. The Oyster, developed by Queen's University Belfast and Aquamarine Power Ltd, is a bottom-mounted flap, about 12 m high, that is intended to be deployed in waters about 12 m deep, in areas where the average incident wave power is greater than 15kW/m. Peak power 600 kW. A single device would produce about 270 kW in wave heights greater than 3.5 m. Assume its width is about 20 m? Then the ideal power for a device of cross-section 20 m would be 240 kW. A rough average figure is about 100 kW. A smaller power than the Pelamis, but a bigger power per unit mass of hardware.

Oysters could also be used to directly drive reverse-osmosis desalination facilities. "The peak freshwater output of each Oyster desalinator is between 2000 and 6000 $\rm m^3/day$," That production has a value, going by the Jersey facility (which uses 8 kWh per $\rm m^3$), equal to 16 000–48 000 kWh per day, that is, 600–2000 kW.

If 400 km of the shallow coastline were peppered with Oysters, three of them every hundred metres, then the power delivered would be 1.2 GW, or about 0.5 kWh/d per person.

The total from deep- and shallow-water devices would be at most $5.2\,\mathrm{GW}$ (perhaps a little less, if they were installed in such a way that the one shadowed the other). $(2.1\,\mathrm{kWh/d/p.})$

Notes

Facts about deep-water waves. See Faber [1995], p. 170.

Conventions

Most of this is to be cut.

From Mollison [1986], we learn the following facts and conventions. A wave-train of amplitude *a* has root-mean-square wave-height *H* given by

$$H^2 = \frac{1}{2}a^2.$$

F — *Waves II* 329

The power flux is

$$P = \frac{\rho g^2}{4\pi} H^2 T,$$

where *T* is the period. The phase velocity is $U = gT/(2\pi)$; the wavelength is $L = gT^2/(2\pi)$. The "significant wave height" is

$$H_{\rm S}=4H_{\rm rms}$$
.

Wave growth

Wave energy density per unit area, $E = \rho g H^2$, grows roughly linearly with fetch x:

 $H_{\rm rms}^2 \simeq 1.6 \times 10^{-7} U_{10}^2 \frac{x}{g}$

where U_{10} is the windspeed measured 10 m above the sea surface. The greater the fetch, the greater the mean period $T_{\rm e}$ of the waves created. Empirically $T_{\rm e} \sim x^{1/3}$. In fully developed seas, $H_{\rm rms} = 0.0053 U_{19.5}^2$ (presumably SI units). And the mean period is $T_{\rm e} = 0.625 U_{19.5}$ – again, presumably SI units. The associated phase velocity for this period of wave is $U_{\rm e} = g T_{\rm e}/(2\pi) = \frac{g}{2\pi} 0.625 U_{19.5} = 0.98 U_{19.5}$. The power in such a fully developed sea is proportional to U^5 and the fetch required to generate it is proportional to U^2 . This fetch is roughly 3000 wavelengths. (Using the wavelength associated with the mean period.) For example, if $U_{19.5} = 20\,{\rm m/s}$, $H_{\rm rms} = 2.12\,{\rm m}$, $T_{\rm e} = 12.5\,{\rm s}$, and the required fetch is about 700 km. The power density attained is 440 kW/m, and the mean rate of energy transfer from wind to sea is $0.6\,{\rm W/m^2}$.

Losses from viscosity are minimal: a wave of 9 seconds period would have to go three times round the world to lose 10% of its amplitude.

G Tide II

Power density of tidal pools

Production on ebb and flood

To estimate the power of an artificial tide-pool, imagine that it's filled rapidly at high tide, and emptied rapidly at low tide. Power is generated in both directions. (This is called two-way generation or double-effect generation.) The change in potential energy of the water, each six hours, is mgh, where h is the change in height of the centre of mass of the water, which is half the range. (The range is the difference in height between low and high tide; figure G.1.) The mass per unit land-area covered by tide-pool is $\rho \times (2h)$, where ρ is the density of water (1000 kg/m³). So the power per unit area generated by a tide pool is

$$\frac{2\rho hgh}{6 \text{ hours}'}$$

assuming perfectly efficient generators. Plugging in $h = 2 \,\mathrm{m}$ (i.e., range 4 m), we find the power per unit area of tide-pool is $3.6 \,\mathrm{W/m^2}$. Allowing for an efficiency of 90% for conversion of this power to electricity, we get

power per unit area of tide-pool $\simeq 3 \text{ W/m}^2$.

So to generate $1\,\mathrm{GW}$ of power (on average), we need a tidepool with an area of about $300\,\mathrm{km}^2$. A circular pool with diameter $20\,\mathrm{km}$ would do the trick. (For comparison, the area of the Severn estuary behind the proposed barrage is about $550\,\mathrm{km}^2$, and the area of the Wash is more than $400\,\mathrm{km}^2$.

If a tidepool produces electricity in one direction only, the power per unit area is halved. The average power density of the tidal barrage at La Rance, where the mean tidal range is $10.9\,\text{m}$, has been $2.7\,\text{W/m}^2$ for decades (p92).

The raw tidal resource

Tides as tidal waves

The tides around Britain are tidal waves – unlike tsunamis, which are called "tidal waves," but are nothing to do with tides. Follow a high tide as it rolls in from the Atlantic. The time of high tide becomes progressively later as we move east up the English channel from the Isles of Scilly to Portsmouth and on to Dover. Similarly, a high tide moves clockwise round Scotland, rolling down the North Sea from Wick to Berwick and on to Hull. These two high tides converge on the Thames Estuary. By coincidence, the Scottish wave arrives about 12 hours later than the one

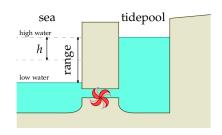
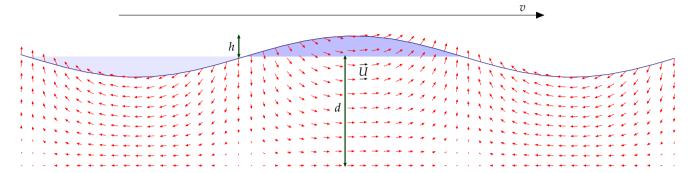


Figure G.1. A tide-pool in cross section. The pool was filled at high tide, and now it's low tide. We let the water out through the electricity generator to turn the water's potential energy into electricity.

G — Tide II 331

that came via Dover, so it arrives in synchrony with the next high tide via Dover, and London receives the normal two high tides per day. The location of the high tide moves much faster than the tidal flow – one hundred miles per hour, say, while the water itself moves at just one mile per hour.



The energy we can extract from tides, using tidal pools or tide-farms, can never be more than the energy of these tidal waves from the Atlantic. We can estimate the total power of these great Atlantic tidal waves in the same was as we estimate the power of their smaller cousins, ordinary waves. The next section describes a standard model for the power arriving in travelling waves in water of depth d, that is shallow compared to the wavelength of the waves (figure G.2). The power per unit length of wavecrest of shallow-water tidal waves is $\rho g^{3/2} \sqrt{d}h^2/2$. Table G.3 shows the power per unit length of wave crest for some plausible figures. If $d=100\,\mathrm{m}$, and h=1 or $2\,\mathrm{m}$, the power per unit length of wave crest is $150\,\mathrm{kW/m}$ or $600\,\mathrm{kW/m}$ respectively. These figures are impressive compared with the raw power per unit length of ordinary Atlantic deep-water waves, $40\,\mathrm{kW/m}$ (Chapter F). Atlantic waves and the Atlantic tide have similar vertical amplitudes (about $1\,\mathrm{m}$), but the raw power in tides is roughly 10 times bigger than that of ordinary wind-driven waves.

Fortunately we don't have to depend on my rough model of incoming tidal power. Taylor [1920] worked out a more detailed model that includes important details such as the Coriolis effect (the effect produced by the earth's daily rotation), the existence of tidal waves travelling in the opposite direction, and the direct effect of the moon on the energy flow in the Irish Sea. Since then, experimental measurements and computer models have verified and extended Taylor's analysis.

Flather [1976] built a detailed numerical model of the lunar tide, chopping the continental shelf around the British Isles into roughly a thousand square cells. Flather estimated that the total average power entering this region is 215 GW. According to his model, 180 GW enters the gap between France and Ireland. From Northern Ireland round to Shetland, the incoming power is 49 GW. Between Shetland and Norway there is a net loss of 5 GW.

Cartwright et al. [1980] found experimentally that the average power

Figure G.2. A shallow-water wave. Just like a deep-water wave, the wave has energy in two forms: potential energy associated with raising water out of the light-shaded troughs into the heavy-shaded crests; and kinetic energy of all the water moving around as indicated by the small arrows. The speed of the wave, travelling from left to right, is indicated by the much bigger arrow at the top. For tidal waves, a typical depth might be 100 m, the crest velocity 30 m/s, the vertical amplitude at the surface 1 or 2 m, and the water velocity amplitude 0.3 or $0.6\,\mathrm{m/s}$.

transmission was 60 GW between Malin Head (Ireland) and Florø (Norway) and 190 GW between Valentia (Ireland) and the Brittany coast near Ouessant. The power entering the Irish Sea was found to be 45 GW, and entering the North Sea via the Dover Straits, 16.7 GW.

The power of tidal waves

This section, which can safely be skipped, provides more details behind the formula for tidal power used in the previous section. I'm going to go into this model of tidal power in some detail because most of the official estimates of the UK tidal resource have been based on a model that I believe is incorrect.

Figure G.2 shows a model for a tidal wave travelling across relatively shallow water. This model is intended as a cartoon, for example, of tidal crests moving up the English channel or down the North Sea. It's important to distinguish the speed U at which the water itself moves (which might be about 1 mile per hour) from the speed v at which the high tide moves, which is typically one or two hundred miles per hour.

The water has depth d. Crests and troughs of water are injected from the left hand side by the 12-hourly ocean tides. The crests and troughs move with velocity

$$v = \sqrt{gd}. (G.1)$$

We assume that the wavelength is much bigger than the depth, and we neglect details such as Coriolis forces and density variations in the water. Call the vertical amplitude of the tide h. For the standard assumption of nearly-vorticity-free flow, the horizontal velocity of the water is near-constant with depth. The horizontal velocity U is proportional to the surface displacement and can be found by conservation of mass:

$$U = vh/d. (G.2)$$

If the depth decreases gradually, the wave velocity v reduces (equation (G.1)). For the present discussion we'll assume the depth is constant. Energy flows from left to right at some rate. How should this total tidal power be estimated? And what's the maximum power that could be extracted?

One suggestion is to choose a cross-section and estimate the average *flux of kinetic energy* across that plane, then assume that this quantity represents the power that could be extracted. This kinetic-energy-flux method was used by consultants Black and Veatch to estimate the UK resource. In our cartoon model, we can compute the total power by other means. We'll see that the kinetic-energy-flux answer is too small by a significant factor.

The peak kinetic-energy flux at any section is

$$K_{\rm BV} = \frac{1}{2}\rho A U^3,\tag{G.3}$$

<i>h</i> (m)	$\rho g^{3/2} \sqrt{d}h^2/2$ (kW/m)
0.9	125
1.0	155
1.2	220
1.5	345
1.75	470
2.0	600
2.25	780

Table G.3. Power fluxes (power per unit length of wave crest) for depth d = 100 m.

G — *Tide II* 333

where A is the cross-sectional area. (This is the standard formula for kinetice energy flux, which we encountered in Chapter B.) The true total incident power is different from the kinetic-energy flux.

The true total incident power in a shallow-water wave is a standard textbook calculation; one way to get it is to find the total energy present in one wavelength and divide by the period.

The total energy per wavelength is the sum of the potential energy and the kinetic energy. The kinetic energy happens to be identical to the potential energy. (This is a standard feature of almost all things that wobble, be they masses on springs or children on swings.) So to compute the total energy all we need to do is compute one of the two – the potential energy per wavelength, or the kinetic energy per wavelength – then double it. Let's go for the potential energy.

The potential energy of a wave (per wavelength and per unit width of wavefront) is found by integration to be

$$\frac{1}{4}\rho gh^2\lambda. \tag{G.4}$$

So, doubling and dividing by the period, the true power of this model shallow-water tidal wave is

power =
$$\frac{1}{2}(\rho g h^2 \lambda) \times w/T = \frac{1}{2}\rho g h^2 v \times w,$$
 (G.5)

where w is the width of the wavefront. Substituting $v = \sqrt{gd}$,

power =
$$\rho g h^2 \sqrt{g d} \times w/2 = \rho g^{3/2} \sqrt{d} h^2 \times w/2$$
. (G.6)

Let's compare this power with the kinetic-energy flux $K_{\rm BV}$. Strikingly, the two expressions scale differently with amplitude. Using the amplitude conversion relation (G.2), the crest velocity (G.1), and A=wd, we can re-express the kinetic-energy flux as

$$K_{\rm BV} = \frac{1}{2} \rho A U^3 = \frac{1}{2} \rho w d (v h / d)^3 = \rho \left(g^{3/2} / \sqrt{d} \right) h^3 \times w / 2.$$
 (G.7)

Thus the kinetic-energy-flux method suggests that the total power of a shallow-water wave scales as amplitude cubed (equation (G.7)); but the correct formula shows that the power scales as amplitude squared (equation (G.6)).

The ratio is

$$\frac{K_{\rm BV}}{\text{power}} = \frac{\rho w \left(g^{3/2}/\sqrt{d}\right) h^3}{\rho g^{3/2} h^2 \sqrt{d} w} = \frac{h}{d}.$$
 (G.8)

Because h is usually much smaller than d, estimates of tidal power resources that are based on the kinetic-energy-flux method may be too small by a significant factor, at least in cases where this shallow-water cartoon of tidal waves is appropriate.

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com



Figure G.4. Average tidal powers measured by Cartwright et al. [1980].

U / (m/s)	U / (knots)	Tide-farm power (W/m ²)
0.5	1	1
1	2	8
2	4	60
3	6	200
4	8	500
5	10	1000

Table G.5. Tide-farm power density (in watts per square metre of sea-floor) as a function of flow speed U. (1 knot = 1 nautical mile per hour = $0.514 \,\mathrm{m/s.}$) The power density is computed using $\frac{\pi}{200} \frac{1}{2} \rho v^3$ (equation (B.8)).

Moreover, estimates based on the kinetic-energy-flux method incorrectly assert that the total available power at springs (the biggest tides) is eight times greater than at neaps (the smallest tides), assuming an amplitude ratio, springs to neaps, of two; but the correct answer is that the total available power of a travelling wave scales as its amplitude squared, so the springs-to-neaps ratio of total-incoming-power is four.

Effect of shelving of sea bed, and Coriolis force

If the depth d decreases gradually and the width remains constant such that there is minimal reflection or absorption of the incoming power, then the power of the wave will remain constant. This means $\sqrt{d}h^2$ is a constant, so we deduce that the height of the tide scales with depth as $h \sim 1/d^{1/4}$.

This is a crude model. One neglected detail is the Coriolis effect. The Coriolis force causes tidal crests and troughs to tend to drive on the right – for example, going up the English Channel, the high tides are higher and the low tides are lower on the French side of the channel. By neglecting this effect I may have introduced some error into the estimates.

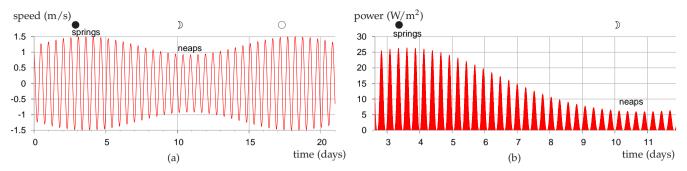
Power density of tidal stream farms

Imagine sticking underwater windmills on the sea-bed. The flow of water will turn the windmills. Because the density of water is roughly a thousand times that of air, the power of water flow is one thousand times greater than the power of wind at the same speed.

Polish me

It depends crucially on whether or not we can add up the power contributions of *adjacent* pieces of sea-floor. For wind, this additivity assumption is believed to work fine: as long as the wind turbines are spaced a standard distance apart from each other, the total power delivered by 10 adjacent wind-farms is the sum of the powers that each would deliver if it were alone.

G — Tide II 335



Does the same go for tide-farms? Or do underwater windmills interfere with each other's power extraction in a different way? I don't think the answer to this question is known in general. We can name two alternative assumptions, however, and identify cartoon situations in which each assumption seems valid. The "tide is like wind" assumption says that you can put tide-turbines all over the sea-bed, spaced about 5 diameters apart from each other, and they won't interfere with each other, no matter how much of the sea-bed you cover with such tide-farms. This assumption seems to me to be valid if the heights of the turbines are small compared to the water depth. I think it might be valid even for tall turbines, but I'm not sure.

The "you can have only one row" assumption, in contrast, asserts that the maximum power extractable in a region is the power that would be delivered by a *single* row of turbines facing the flow. A situation where this assumption is correct is the special case of a hydroelectric dam: if the water from the dam passes through a single well-designed turbine, there's no point putting any more turbines behind that one. You can't get one hundred times more power by putting ninety-nine more turbines downstream from the first. The oomph gets extracted by the first one, and there isn't any more oomph left for the others. The "you can have only one row" assumption is the right assumption for estimating the extractable power in a place where water flows through a narrow channel from approximately stationary water at one height into another body of water at a lower height. (This case is analysed by Garrett and Cummins [2005, 2007].)

I'm now going to nail my colours to a mast. I think that in many places round the British Isles, the "tide is like wind" assumption is a good approximation. Perhaps some spots have some of the character of a narrow channel. In those spots, my estimates may be over-estimates.

Let's assume that the rules for laying out a sensible tide-farm will be similar to those for wind-farms, and that the efficiency of the tidemills will be like that of the best windmills, about 1/2. Given these assumptions, table G.5 shows this tide-farm power for a few tidal currents.

Now, what are plausible tidal currents? Tidal charts usually give the currents associated with the tides with the largest range (called spring

Figure G.6. (a) Tidal current over a 21-day period at a location where the maximum current at spring tide is $2.9 \, \text{knots} \, (1.5 \, \text{m/s})$ and the maximum current at neap tide is $1.8 \, \text{knots} \, (0.9 \, \text{m/s})$.

(b) The power per unit sea-floor area over a nine-day period extending from spring tides to neap tides. The power peaks four times per day, and has a maximum of about 27 W/m^2 . The average power of the tide farm is 6.4 W/m^2 .

Region	(k:	nots)	power density (W/m²)	(km^2)	average power (kWh/d/p)
1	1.7	3.1	7	400	1.1
2	1.8	3.2	8	350	1.1
3	1.3	2.3	2.9	1000	1.2
4	1.7	3.4	9	400	1.4
5	1.7	3.1	7	300	0.8
6	5.0	9.0	170	50	3.5
Total					9

Table G.8. Tidal power estimates assuming that stream farms are like wind farms. Power density is the average power density in W/m^2 of sea floor. The six regions are indicated in figure G.7.

tides) and the tides with the smallest range (called neap tides). Spring tides occur shortly after each full moon and each new moon. Neap tides occur shortly after the first and third quarters of the moon. The power of a tide farm would vary throughout the day in a completely predictable manner. Figure G.6 illustrates the variation of power density of a tide-farm with a maximum current of $1.5\,\mathrm{m/s}$. The average power of this tide-farm would be $6.4\,\mathrm{W/m^2}$. There are many places around the British Isles where the power per unit area of tide-farm would be $6\,\mathrm{W/m^2}$ or more. This power density is similar to our estimates of the power densities of wind farms $(2-3\,\mathrm{W/m^2})$ and of photovoltaic solar farms $(5\,\mathrm{W/m^2})$.

Tide power is not to be sneezed at! How would it add up, if we assume that there are no economic obstacles to the exploitation of tidal power at all the hot spots around the UK?

We'll now use this "tide farms are like wind farms" theory to estimate the extractable power from tidal streams in promising regions around the British Isles. As a sanity check, we'll also work out the total tidal power crossing each of these regions, using the "power of tidal waves" theory, to check our tide-farm's estimated power isn't bigger than the total power available. The main locations around the British Isles where tidal currents are large are shown in figure G.7.

I estimated the typical peak currents at six locations from low-resolution tidal charts in Reed's Nautical Almanac. (These estimates could easily be off by 30%.) Have I over-estimated or under-estimated the area of each region? I haven't surveyed the sea floor so I don't know if some regions might be unsuitable in some way – too deep, or too shallow, or too tricky to build on. I've included only six small regions with large currents. Perhaps I should also have included an estimate for the power from the much larger regions with small currents.

Admitting all these uncertainties, I arrive at an estimated total power of 9 kWh/d per person from tidal stream-farms; plus another 2 kWh/d per person from tidal lagoons and tidal barrages. This corresponds to 9% of the raw incoming power mentioned on p88, 100 kWh per day per person.

G — *Tide II* 337

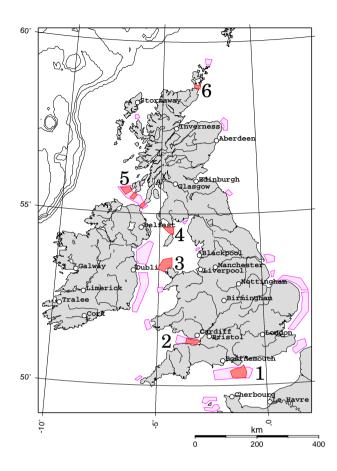


Figure G.7. Regions around the British Isles where peak tidal flows exceed 1 m/s. The six darkly-coloured regions are included in table G.8:

1.the English channel (south of the Isle of Wight);

2.the Bristol channel;

3.to the north of Anglesey;

4.to the north of the Isle of Man;

5.between Northern Ireland, the Mull of Kintyre, and Islay; and

6.the Pentland Firth (between Orkney and mainland Scotland), and within the Orkneys.

There are also enormous currents around the Channel Islands, but they are not governed by the UK.
Runner-up regions include the North Sea, from the Thames (London) to the Wash (Kings Lynn).

The contours show water depths greater than 100 m.

Tidal data from Reed's Nautical Almanac and DTI Atlas of UK Marine Renewable Energy Resources.

Tide-farm Region Raw depth width power estimate (m) (km) Ν (kWh/d/p)1 30 2.3 7.8 1.1 30 2 30 17 1.5 4.7 1.1 3 50 30 3.0 9.3 1.2 4 30 20 1.5 6.3 1.4 5 0.8 40 10 1.2 4.0 6 70 10 24 78 3.5 Total 9

Table G.9. This table compares the tide-farm estimates of extractable power of table G.8 with the raw incoming power estimated on p332. The six regions are indicated in figure G.7. N = Neaps. S = Springs.

<i>v</i> (m/s)	v (knots)	Friction power (W/m²)		Tide-farm power (W/m²)
, ,	,	$R_1 = 0.01$	$R_1 = 0.003$, ,
0.5	1	1.25	0.4	1
1	2	10	3	8
2	4	80	24	60
3	6	270	80	200
4	8	640	190	500
5	10	1250	375	1000

Table G.10. Friction power density $R_1\rho U^3$ (in watts per square metre of sea-floor) as a function of flow speed, assuming $R_1=0.01$ or 0.003. Flather [1976] uses $R_1=0.0025-0.003$; Taylor [1920] uses 0.002. (1 knot = 1 nautical mile per hour = 0.514 m/s.) The final column shows the tide-farm power estimated in table G.5.

Estimating the tidal resource via bottom friction

Another way to estimate the power available from tide is to compute how much power is already dissipated by friction on the sea floor. A coating of turbines placed just above the sea floor could act as a substitute bottom, exerting roughly the same drag on the passing water as the sea floor used to, and extracting roughly the same amount of power as friction used to dissipate, without significantly altering the tidal flows.

So, what's the power dissipated by "bottom friction"? Unfortunately, there isn't a straightforward model of bottom friction. It depends on the roughness of the sea bed and the material that the bed is made from and even given this information, the correct formula to use is not settled. One widely used model says that the magnitude of the stress (force per unit area) is $R_1\rho U^2$, where U is the average flow velocity and R_1 is a dimensionless quantity called the shear friction coefficient. We can estimate the power dissipated per unit area by multiplying the stress by the velocity. Table G.10 shows the power dissipated in friction, $R_1\rho U^3$, assuming $R_1 = 0.01$ or $R_1 = 0.003$. (Add citations.) Kowalik [2004] Sleath [1984]. What this table shows is that, for values of the shear friction coefficient between 0.003 and 0.01, the friction power is very similar to the estimated power that a tide farm would deliver. This is good news, because it suggests that planting a forest of underwater windmills on the sea-bottom, spaced five diameters apart, won't radically alter the flow in the region. The natural friction already has an effect that is in the same ballpark.

Tidal pools with pumping

There is a trick, "the pumping trick," which artificially increases the amplitude of the tides in the tidal pool so as the amplify the power obtained. The energy cost of pumping in extra water at high tide is repaid with interest when the same water is let out at low tide; similarly, extra water can be pumped *out* at low tide, then let back in at high tide. The pumping trick is sometimes used at La Rance, boosting its net power generation by

tidal amplitude (half-range) <i>h</i> (m)	optimal boost height <i>b</i> (m)	power with pumping (W/m²)	power without pumping (W/m²)
0.5	3.3	0.9	0.2
1.0	6.5	3.5	0.8
2.0	13	14	3.3
3.0	20	31	7.4
4.0	26	56	13

Table G.11. Theoretical power density from tidal power using the pumping trick, assuming no constraint on the height of the basin's walls.

about 10% Wilson and Balls [1990]. Let's work out the theoretical limit for this technology.

I'll assume that generation has an efficiency of $\epsilon_g=0.9$ and that pumping has an efficiency of $\epsilon_p=0.85$. (These figures are based on the pumped storage system at Dinorwig.)

Let the tidal range be 2h. I'll assume that the prices of buying and selling electricity are the same at high tide and low tide, so that the optimal height boost b to which the pool is pumped above high water is given by (marginal cost of extra pumping = marginal return of extra water):

$$b/\epsilon_p = \epsilon_g(b+2h).$$

Defining the round-trip efficiency $\epsilon = \epsilon_{\rm g} \epsilon_{\rm p}$, we have

$$b = 2h \frac{\epsilon}{1 - \epsilon}.$$

For example, with a tidal range of 2h = 4 m, and a round-trip efficiency of $\epsilon = 76\%$, the optimal boost is b = 13 m. This is the maximum height to which pumping can be justified if the price of electricity is constant.

Let's assume the complementary trick is used at low tide. (This requires the basin to have a vertical range of 30 m!) The delivered power per unit area is then

$$\left(\frac{1}{2}\rho g\epsilon_{\rm g}(b+2h)^2-\frac{1}{2}\rho g\frac{1}{\epsilon_{\rm p}}b^2\right)/T$$
,

where T is the time from high tide to low tide. We can express this as the maximum possible power density without pumping, $\epsilon_{\rm g} 2\rho g h^2/T$, scaled up by a boost factor

$$\left(\frac{1}{1-\epsilon}\right)$$
,

which is roughly a factor of 4. Table G shows the theoretical power density that pumping could deliver. Unfortunately, this pumping trick will rarely be exploited to the full because of the economics of basin construction: full exploitation of pumping requires the total height of the pool to be roughly 4 times the tidal range, and increases the delivered power fourfold. But the material in a sea-wall of height H scales as H^2 , so the cost

tidal amplitude (half-range) h (m)	boost height b (m)	power with pumping (W/m²)	power without pumping (W/m²)
0.5	0.5	0.4	0.2
1.0	1.0	1.6	0.8
2.0	2.0	6.3	3.3
3.0	3.0	14	7.4
4.0	4.0	25	13

Table G.12. Power density offered by the pumping trick, assuming the boost height is constrained to be the same as the tidal amplitude. This assumption applies, for example, at neap tides, if the pumping pushes the tidal range up to the springs range.

of constructing a wall four times as high will be more than four times as big. Extra cash would probably be better spent on enlarging a tidal pool horizontally rather than vertically.

The pumping trick can nevertheless be used for free on any day when the range of natural tides is smaller than the maximum range: the water level at high tide can be pumped up to the maximum. Table G gives the power delivered if the boost height is set to h, that is, the range in the pool is just double the external range. A doubling of vertical range is plausible at neap tides, since neap tides are typically about half as high as spring tides. Pumping the pool at neaps so that the full springs range is used thus allows neap tides to deliver roughly twice as much power as they would offer without pumping. So a system with pumping would show two-weekly variations in power of just a factor of 2 instead of 4.

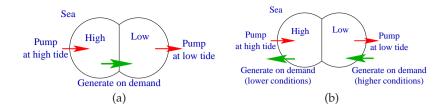
The two-basin scheme: an "always-on" tidal power scheme

A neat idea: have two basins, one of which is the 'full' basin and one the "empty" basin; every high tide, the full basin is topped up; every low tide, the empty basin is emptied. These toppings-up and emptyings could be done either passively through sluices, or even actively by pumps (using the trick mentioned elsewhere). Whenever power is required, water is allowed to flow from the full basin to the empty basin, or (better in power terms) between one of the basins and the sea. The power per unit area is the same as that of the single-basin tidal barrage; the capital cost may be bigger because of the need for extra barriers; the big win is that power is available all the time, so the facility can follow demand.

We can even use power generated from the empty basin to pump extra water into the full basin at high tide, and similarly use power from the full basin to pump down the empty basin at low tide. This self-pumping would boost the total power delivered by the facility without ever needing to buy energy from the grid.

A two-basin system could also function as a pumped-storage facility. I'll come back to this in chapter 26. (p351) (*Perhaps move all this material to one place*).

G — *Tide II* 341



Using multiple pools - for example, a high pool and a low pool doesn't increase the deliverable power, but does increase the flexibility of when power can be delivered, thus enhancing the value of a facility. A two-pool facility is "always on," and would be able to provide the same sort of valuable service as the Dinorwig pumped-storage station. A twopool facility can also do its own pumping. It's a delightful feature of a two-pool solution that the optimal time to pump water into the high pool is high tide, which is also the optimal time to generate power from the low pool. Similarly low tide is the perfect time to pump down the low pool, and it's the perfect time to generate power from the high pool. In a simple simulation, I've found that a two-lagoon system in a location with a natural tidal range of 4 m can, with an appropriate pumping schedule, deliver a steady power of 4.5 W/m² [MacKay, 2007a]. One lagoon's water level is always kept above sea-level; the other lagoon's level is always kept below sea-level. This power density of 4.5 W/m² is 50% bigger than the maximum possible average power density of an ordinary tide-pool in the same location (3 W/m²). The steady power of the lagoon system would be more valuable than the intermittent and less-flexible power from the ordinary tide-pool.

Haishan

There is a two-basin tidal power plant at Haishan, Maoyan Island, China. A single generator located between the two basins (as shown in figure G.13(a)) delivers power continuously, and generates 39 kW on average.

Bristol barrage details

From Hammons Tidal Power paper Hammons [1993] and Taylor [2002]. 16 km barrage. The enclosed area of water would measure 520 km². 7 m mean tide range. Annual output of 17 TWh (2 GW average; peak capacity of 8.6 GW) would include a 10% boost from the pumping trick. Construction would take 9 years and cost £10 billion. (Note, £5 million per (average) megawatt; similar to windmills, which seem to cost about £3 million per (average) megawatt?) 370 km of new 400 kV transmission lines would be required.

Mersey barrage: 2 km long. 6.5 m mean tide range. 61 km² basin area.

Figure G.13. Different ways to use the tidal pumping trick. Two lagoons are located at sea-level. (a) One simple way of using two lagoons is to label one the high pool and the other the low pool; when the surrounding sea level is near to high tide, let water into the high pool, or actively pump it in (using electricity from other sources); and similarly, when the sea level is near to low tide, empty the low pool, either passively or by active pumping; then whenever power is sufficiently valuable, generate power on demand by letting water from the high pool to the low pool. (b) Another arrangement that might deliver more power per unit area has no flow of water between the two lagoons. While one lagoon is being pumped full or pumped empty, the other lagoon can deliver steady, demand-following power to the grid. Pumping may be powered by bursty sources such as wind, by spare power from the grid (say, nuclear power stations), or by other half of the facility, using one lagoon's power to pump the other lagoon to a greater height.

	Barrage	Lagoons (largest scenario)
power generated	17–19 TWh/y	24 TWh/y
average output	1.95-2.17 GW	2.75 GW
capacity	8.64 GW	4.50 GW
impounded area	185 square miles	115 square miles
overall wall length	9.8 miles	95 miles (approx)
aggregates required	13 M tons	200 M tons (approx)

1.5 TWh/y, or 170 MW average, again including the pumping trick. Peak capacity 700 MW. Estimated cost: about £1 billion.

Swansea circular lagoon

Tidal Electric limited, backed by The Environment Trust, by AEA Technology, and by W.S. Atkins Engineering.

Area $5 \,\mathrm{km^2}$. Peak capacity of $60 \,\mathrm{MW}$. Annual output $187 \,\mathrm{GWh}$, i.e., $21 \,\mathrm{MW}$ average. (Which is $4 \,\mathrm{W/m^2}$.)

They say the potential capacity for the UK is 1500 MW in the Mersey, 4500 MW in the Severn Estuary, and 150 MW in the Thames Estuary. Dividing by 3 to get the average delivered, that's about 2 GW, or 1 kWh/d per person.

Friends of the Earth compare the Bristol barrage with the largest lagoon envisaged for the Severn Estuary. Friends of the Earth Cymru [2004] [s8dry] A good comparison they make is the tonnage of aggregates (200 Mt) compared with the tonnage of coal to produce the same power – 5 Mt coal per year, for 22 TWh/y. So 40 years' worth of coal.

Mersey lagoon

Tidal Lagoon without pumping. 7 km in diameter $350\,\mathrm{MW}$ "capacity"; average power $650\,\mathrm{GWh/y} = 74\,\mathrm{MW}$. $(2\,\mathrm{W/m^2})$.

For comparison, their Tidal Barrage plan $700\,\mathrm{MW}$ "capacity"; average power $1200\,\mathrm{GWh/y} = 137\,\mathrm{MW}$.

(They call this "a sizeable proportion of the energy needs of Merseyside"). Fact: the population of Merseyside in the 2001 census was $1\,362\,034$. How do the energy needs of Merseyside actually compare with the tidal energy figure, assuming, like the rest of the UK, that Merseysiders use $120\,\mathrm{kWh/d}$ per person? Well, $1200\,\mathrm{GWh}$ per year shared between $1.3\,\mathrm{million}$ works out to $2.4\,\mathrm{kWh/d}$ per person. Worth doing? I think so. But "a sizeable proportion" of $120\,\mathrm{kWh/d}$? Well, only if you call 2% a sizeable proportion!

Notes

page no.

334 *Table G.5.* To work out the power of a tide-farm (per unit sea-floor), we steal the formula for the power of a wind-farm (per unit land area) from p284. The power per unit sea-floor area is

$$\frac{\text{power per tidemill}}{\text{area per tidemill}} = \frac{\pi}{200} \frac{1}{2} \rho v^3$$

For more on the estimation of the UK tidal resource, see MacKay [2007b].

- 336 The main locations around the UK where tidal currents are large... I identified the regions with biggest flows using the DTI Atlas of UK Marine Renewable Energy Resources (2004).
- There is a two-basin tidal power plant at Haishan [2bqapk].

For more on tidal lagoons, see MacKay [2007a].

Area behind the Bristol barrage is $480 \, \text{km}^2$. So with average output of 2 GW, it would indeed deliver $4 \, \text{W/m}^2$.

Estimates of possible tidal lagoon / barrage projects in the UK from [2bqapk]

site	mean tidal range (m)	basin area (km²)	capacity (MW)	annual output (TWh/year)	load factor
Severn	7.0	520	8 640	17.0	23%
Mersey	6.5	61	700	1.4	23%
Duddon	5.6	20	100	0.212	22%
Wyre	6.0	5.8	64	0.131	24%
Conwy	5.2	5.5	33	0.060	21%

Assumptions

In this chapter, we assumed that power would be produced with equal efficiency at all flow speeds. If tidemills are similar to windmills, this assumption won't be true; there will be only a range of speeds at which power is produced efficiently.

We also assumed that the flow rate at depth is the same as the flow rate at the surface, quoted in the Nautical Almanac. Again, this assumption is inaccurate. It's an object of ongoing research to measure the actual variations of current with depth. Figure G.15 shows the sort of variation of speed with depth that we expect in inviscid fluids: the flow is almost constant with depth, except in a thin layer near the sea floor.

Pentland Firth...

Bottom friction and variation of flow with depth Sleath [1984].

Further reading: Shaw and Watson [2003b], Blunden and Bahaj [2007], Charlier [2003a,b].

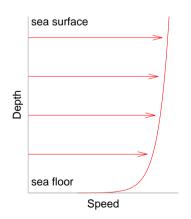


Figure G.15. Tidal flows at depth are usually similar to the surface flow. This figure is just a cartoon, indicating the expected shape of the speed-versus-depth curve. Real flows are always turbulent, with speeds fluctuating around a mean curve like

this one. The numerical details depend on the roughness of the sea

floor.

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

H Stuff II

Imported energy

Dieter Helm and his colleagues estimated the footprint of each pound's worth of imports from country X using the average carbon intensity of country X's economy (that is, the ratio of their carbon emissions to their gross domestic product). They concluded that the embodied carbon in imports to Britain (which should be added to Britain's official carbon footprint of 11 tons $CO_2^{(e)}$ per year per person) is roughly 16 tons $CO_2^{(e)}$ per year per person. A subsequent, more detailed, study commissioned by DEFRA estimated that the embodied carbon in imports is smaller, but still very significant: about 6.2 tons $CO_2^{(e)}$ per year per person. In energy terms, 6 tons $CO_2^{(e)}$ per year is something like 60 kWh/d.

Here, let's see if we can reproduce these conclusions in a different way, using the weights of the imports.

Figure H.1 shows Britain's imports in the year 2006 in three ways: on the left, the total value of the imports is broken down by the country of origin. In the middle, the same total financial value is broken down by the type of stuff imported, using the categories of HM Revenue and Customs. On the right, all maritime imports to Britain are shown by *weight* and broken down by the categories used by the Department for Transport, which doesn't care whether something is leather or tobacco – it keeps track of how heavy stuff is, whether it is dry or liquid, and whether the stuff arrived in a container or a lorry.

The energy cost of the imported fuels (top right) *is* included in the standard accounts of British energy consumption; the energy costs of all the other imports are not. For most materials, the embodied energy per unit weight is greater than or equal to 10 kWh per kg – the same as the energy per unit weight of fossil fuels. This is true of all metals and alloys, all polymers and composites, most paper products, and many ceramics, for example. The exceptions are raw materials like ores; porous ceramics such as concrete, brick, and porcelain, whose energy cost is 10 times lower; wood and some rubbers; and glasses, whose energy-cost is a whisker lower than 10 kWh per kg. [r22oz]

We can thus roughly estimate the energy footprint of our imports simply from the weight of their manufactured materials, if we exclude things like ores and wood. Given the crudity of the data with which we are working, we will surely slip up and inadvertently include some things made of wood and glass, but hopefully such slips will be balanced by our underestimation of the energy content of most of the metals and plastics and more complex goods, many of which have an embodied energy of not 10 but 30 kWh per kg, or even more.

H - Stuff II 345

Weight of imports in Mt Value of imports Value of imports Bulk fuels: 131 (not to scale) Bulk fuels: £30b Ores: £5.5b Agricultural Ores: 18 products: £27b Wood: £3b Agricultural products: 9 Metals: £20b EU: £161b Forestry products: 8 Chemicals Iron, steel products: 6 (including Liquid bulk plastics): £42b products: 7 Dry bulk Paper, public'ns: £8b products: 11 Textiles, leather: £20b Machinery: £21b Containerized Norway: £15b freight: Russia: £6 Switzerland: £4.5b USA: £26b Electrical equipment: £60b Canada: £5 China: £16b Japan: £8b Furniture, Other Hong Kong: £7.5b other stuff: £15b Singapore: £4b Turkey: £4b South Africa: £4b freight: 50 Vehicles: £48b other countries Vehicles: 3.2

Thrap us lie at input draft 2.9.0 August 048117008 www.withput 10.22 in com

Figure H.1. Imports of stuff to the UK, 2006.

For this calculation I'll take from the right-hand column in figure H.1 the iron and steel products, the dry bulk products, the containerized freight and the "other freight," which total 98 million tons per year. I'm leaving the vehicles to one side for a moment. I subtract from this an estimated 25 million tons of food which is presumably lurking in the "other freight" category (34 million tons of food were imported in 2006), leaving 73 million tons.

Converting 73 million tons to energy using the exchange rate suggested above, and sharing between 60 million people, we estimate that those imports have an embodied energy of 33 kWh/d per person.

For the cars, we can handwave a little less, because we know a little more: the number of imported vehicles in 2006 was $2.4 \, \text{million}$. If we take the embodied energy per car to be $76\,000 \, \text{kWh}$ (a number we picked up on p95) then these imported cars have an embodied energy of $8 \, \text{kWh/d}$ per person.

We've arrived at a total estimate of 41 kWh/d per person for the embodied energy of imports – definitely in the same ballpark as the estimate of Dieter Helm and his colleagues.

I left the "liquid bulk products" out of these estimates because I am not sure what sort of products they are. If they are actually liquid chemicals then their contribution might be significant. I suspect that $41\,\mathrm{kWh/d}$ per person may be an underestimate because the energy intensity we assumed $(10\,\mathrm{kWh/d/person})$ is too low for most forms of manufactured goods such as machinery or electrical equipment. However, without knowing the weights of all the import categories, this is the best estimate I can make for now.

Actual consumption of road transport in the UK

In 2005: heavy goods vehicles (diesel) 9.22 Mtons of petroleum; light goods diesel: 4.77 Mtons of petroleum; out of total 38.10Mtons. light goods vehicles motor spirit: 0.50 Mtons.

In 1997, 12.52 is goods vehicles, out of total of 37.04 for road transport. 2005, All petroleum for transport (air, water, road, rail) = 52.72.

HGV rigid vehicles do 8.3 mi/gal on average; articulated vehicles: 8.1 mi/gal. (Cars do 33 mi/gal.)

In 1997, amounts of goods moved: in billion tkm. 41 food, drink, to-bacco 43 bulk products 15 chemicals, petrol, fertilizer 51 miscellaneous to-tal 150 billion ton km (1643 million tons lifted, taken 23111 million vehicle km. 1997.) That is 6.5 tons per vehicle on average.

So taking 12.52 M t fuel / 150 b tkm, and 45.9 GJ/ton of petroleum, deduce that the transport efficiency of UK road freight is 45.9×12.52 MGJ / 150 G tkm = 3.8 MJ/tkm = 1.06 kWh/tkm. Based on megastatistics.

transwatch say Rail freight - 181 ton-miles per gallon. Road freight - 120 ton-miles per gallon. (assuming 8mpg and 30 ton load, empty half the

347

time) 2.351/100 tkm; which is 0.21 kWh/tkm.

Typical 38 ton lorry uses power of 400 kW at 105 km/h.

Freight movement in the UK: 163 billion ton-kilometres/y. Average haul: 87 kilometres. Food transport is quarter of HGV kilometres. UK international water-borne freight = 446 million tons/y.

Lifecycle analysis for buildings

http://www.greenhouse.gov.au/yourhome/technical/fs31.htm

"LCA examines the total environmental impact of a material or product through every step of its life - from obtaining raw materials (for example, through mining or logging) all the way through manufacture, transport to a store, using it in the home and disposal or recycling." "Process Energy Requirement (PER) is a measure of the energy directly related to the manufacture of the material. This is simpler to quantify. Consequently, most figures quoted for embodied energy are based on the PER. This would include the energy used in transporting the raw materials to the factory but not energy used to transport the final product to the building site." That's what's quoted here. The gross energy requirement widens the boundary, including the embodied energy of urban infrastructure, the embodied energy of the machinery that makes the raw materials. A rough rule of thumb to get the gross energy requirement of a building is to double the process energy requirement.

Example: a three-bedroom house, process energy.

	Area × energy density	energy (GJ)	
Floors	100×293	= 29	_
Roof	75×271	= 20	
External walls	75×906	= 68	
Internal walls	75×450	= 34	
Total		151 GJ	= 42 000 kWh

If we share $42\,000\,\text{kWh}$ over 100 years, and double it to allow for the gross energy cost, the embodied energy cost of a house comes to about $2.3\,\text{kWh/d}$. This is the energy cost of the *shell* of the house only – the bricks, tiles, roof beams.

All the stuff in China

As a double-check of the embedded energy of imported stuff, let's take China's energy consumption and attribute one quarter of it to "us" – a billion people in the developed world (since China is the world's workshop).

Source: Dr Tao Wang and Dr Jim Watson reckon that 25% of China's carbon emissions are associated with exports http://www.greencarcongress.com/2007/10/manufacture-and.html. China's primary energy consumption

Material	Embodied energy	
	(MJ/kg)	(kWh/kg)
kiln-dried sawn softwood	3.4	0.94
kiln-dried sawn hardwood	2.0	0.56
air dried sawn hardwood	0.5	0.14
hardboard	24.2	6.7
particleboard	8.0	2.2
MDF	11.3	3.1
plywood	10.4	2.9
glue-laminated timber	11	3.0
laminated veneer lumber	11	3.0
straw	0.24	0.07
stabilised earth	0.7	0.19
imported dimension granite	13.9	3.9
local dimension granite	5.9	1.6
gypsum plaster	2.9	0.8
plasterboard	4.4	1.2
fibre cement	4.8	1.3
cement	5.6	1.6
in situ concrete	1.9	0.53
precast steam-cured concrete	2.0	0.56
precast tilt-up concrete	1.9	0.53
clay bricks	2.5	0.69
concrete blocks	1.5	0.42
autoclaved aerated concrete	3.6	1.0
plastics – general	90	25
PVC	80	22
synthetic rubber	110	30
acrylic paint	61.5	17
glass	12.7	3.5
fibreglass (glasswool)	28	7.8
aluminium	170	47
copper	100	28
galvanised steel	38	10.6
stainless steel	51.5	14.3

Table H.2. Embodied energy of building materials (assuming virgin product used, rather than recycled). (Dimension stone is natural stone or rock that has been selected and trimmed to specific sizes or shapes.)



H-StuffII 349

		ed energy
	(MJ/m^2)	(kWh/m^2)
Walls		
timber frame, timber weatherboard, plasterboard lining	188	52
timber frame, clay brick veneer, plasterboard lining	561	156
timber frame, aluminium weatherboard, plasterboard lining	403	112
steel frame, clay brick veneer, plasterboard lining	604	168
double clay brick, plasterboard lined	906	252
cement stabilised rammed earth	376	104
Floors		
elevated timber floor	293	81
110 mm concrete slab on ground	645	179
200 mm precast concrete T beam/infill	644	179
Roofs		
timber frame, concrete tile, plasterboard ceiling	251	70
timber frame, terracotta tile, plasterboard ceiling	271	75
timber frame, steel sheet, plasterboard ceiling	330	92

Table H.3. Embodied energy in various constructions. Source: Lawson [1996].

in 2004 was 17500 TWh; if we share the blame for 25% of China's energy among one billion of "us," that's $12\,kWh/d$ per person.

UK imports of goods and services in 2006 had a value of £300 billion per year, a three-fold increase over 1990 levels.

Energy costs of raw materials for stuff

The energy requirements for virgin production of steel are 26–35 MJ/kg (10 kWh per kg); 8–11 times higher for nickel; 1.2–1.6 times higher for lead; 1.5–2 times higher for zinc; and 2–4 times higher for plastics. [Rydh and Karlström, 2002].

Plastic bags

Tesco, Asda, Sainsburys, Morrisons, and Waitrose hand out 9 billion plastic bags per year. That's 150 bags per year for each of our 60 million population.

Phones and computers

Some helpful cautions about life-cycle analysis: http://www.gdrc.org/uem/lca/life-cycle.html

more links: http://www.epa.gov/ord/NRMRL/lcaccess/resources.htm

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

Industry

Notes and further reading

page no.

344 A subsequent more-detailed study commissioned by DEFRA estimated that the embodied carbon in imports is about 6.2 tons $CO_2^{(e)}$ per person. Wiedmann et al. [2008].



Figure H.4. Millau Viaduct in France, the highest bridge in the world. Steel and concrete, 2.5 km long and 353 m high.



Figure H.5. Continuous casting of steel strands at Korea Iron and Steel Company.



© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

I Storage II

Pumped storage

The working volume required, V, depends on the height drop we assume. If ϵ is the efficiency of potential energy to electricity conversion,

$$V = 50 \,\text{GWh}/(\rho g h \epsilon). \tag{I.1}$$

Assuming the generators have an efficiency of $\epsilon = 0.9$, table 26 (p207) shows a few ways of storing 50 GWh, for a range of height drops.

Tidal pumped storage

This calculation goes with the discussion on p??.

Let's denote the tidal range by 2h and the extra head by b. We start a daily cycle one evening, with high and low lagoons both at the mid-tide level. Overnight we pump the high lagoon up and the low lagoon down at the optimal times near to high and low tide. The total energy cost of the pumping, per unit area of facility, is

$$\frac{1}{2}\rho gb^2/\epsilon_{\rm p}$$

where ϵ_p is the pump's efficiency. In the design of figure ??(a), the energy returned at the time of peak demand, per unit area, is

$$\epsilon_{\rm g} \frac{1}{2} \rho g (h+b)^2$$
.

The alternative design, figure ??(b), delivers slightly greater power by picking which pool to exploit depending on the sea level. At a randomly chosen time, there is a 50% chance that the tide is in quite an extreme state – more than 71% of the way to high tide or more than 71% of the way to low tide; and there is a 66% chance that the tide is either beyond half-high or beyond half-low. So, as long as the profitable period lasts more than a couple of hours, both of the pools will have a good chance of serving high-value electricity and the energy returned, per unit area, is about

$$\epsilon_{\rm g} \frac{1}{2} \rho g \left(\frac{3}{2} h + b \right)^2.$$

Let's find the size required for a system with a stored energy of $10\,\mathrm{GWh}$ (about the same as Dinorwig), assuming $2h=4\,\mathrm{m}$ and $b=10\,\mathrm{m}$. That's about $57\,\mathrm{km}^2$, which would fit inside an $8\,\mathrm{km}$ square, and would need about $40\,\mathrm{km}$ of wall. Equipped with generators like Dinorwig's, it would deliver $2\,\mathrm{GW}$ of power during 5 hours of peak demand each day. And

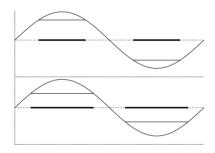


Figure I.1. Half the time, the tide is more than 71% of the way to high tide or more than 71% of the way to low tide; two thirds of the time, the tide is above half-high or below half-low.

the energy cost of delivering that $10\,\text{GWh}$ would be just $6.7\,\text{GWh}$. For comparison with other renewable sources, the power density of the useful power delivered at peak demand would be $10\,\text{W/m}^2$, averaged over 24 hours. The average net power delivered would be $3.3\,\text{W/m}^2$.

The economics for such a scheme favour large facilities: the cost of the lagoons' walls would be proportional to the walls' length, but the area enclosed, and thus the delivered power, would increase as the *square* of the length.

I Carbon II

We, humanity, cannot release to the atmosphere all, or even most, fossil fuel CO_2 . To do so would guarantee dramatic climate change, yielding a different planet...

J. Hansen et al (2007)

"Avoiding dangerous climate change" is impossible – dangerous climate change is already here. The question is, can we avoid *catastrophic* climate change?

David King, UK Chief Scientist, 2007

When I first planned this book, my intention was to ignore climate change altogether. In some circles, "is climate change happening?" was a controversial question. As were "is it caused by humans?" and "does it matter?." And, dangling at the end of a chain of controversies, "what should we do about it?" I felt that sustainable energy was a compelling issue by itself, and it was best to avoid controversy. My argument was to be: "never mind when fossil fuels are going to run out; never mind whether climate change is happening; burning fossil fuels is not sustainable; let's imagine living sustainably, and figure out how much sustainable energy is available."

However, climate change has risen into public consciousness, and it raises all sorts of interesting back-of-envelope questions. So I decided to discuss it a little in the preface and in the closing chapter. Not a complete discussion, just a few interesting numbers and cartoons.

Understanding CO₂

Where is all the carbon? And where is the CO_2 ?

We need to know how much is in the oceans, in the ground, and in vegetation, compared to the atmosphere, if we want to understand the consequences of CO_2 emissions.

If nearly all of the CO_2 is in the atmosphere, then tripling the CO_2 concentration in the atmosphere would be a mistake that nature could not reverse.

If nearly all of the CO_2 is in the oceans, then tripling the CO_2 concentration in the atmosphere might be a reversible mistake – if we subsequently stopped emitting CO_2 , the oceans would gradually mop up CO_2 , and the CO_2 concentration might return close to its original levels (after perhaps a few centuries of catastrophic climate change).





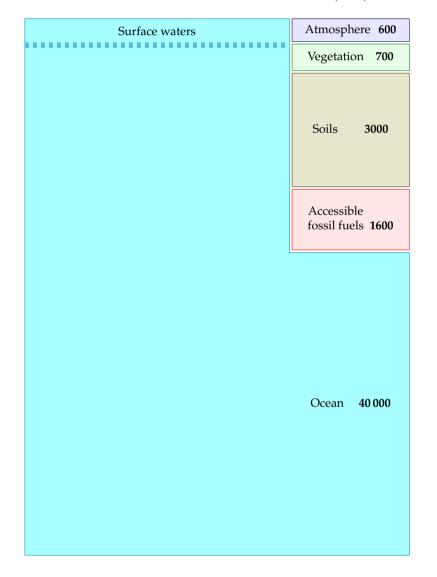


Figure J.1. Estimated amounts of carbon, in gigatons, in accessible places on the earth. (There's a load more carbon in rocks too; this carbon moves round on a timescale of millions of years, with a long-term balance between carbon in sediment being subducted at tectonic plate boundaries, and carbon popping out of volcanos from time to time. For simplicity I ignore this geological carbon.)

J — Carbon II 355

Units

Just as energy is measured in many different units, there is no single established unit for quantities of carbon. Carbon pollution charges are usually measured in dollars or euros per ton of CO₂, so I'll use the **ton of CO**₂ as the main unit when talking about personal carbon pollution, and the **ton of CO**₂ **per year** to measure rates of pollution. But when talking about carbon in fossil fuels, vegetation, soil, and water, I'll talk about tons of carbon.

One ton of CO_2 contains 12/44 tons of carbon, a bit more than a quarter of a ton. On a planetary scale, I'll talk about gigatons of carbon (GtC). A gigaton of carbon is a billion tons, also known as a petagram (Pg) ("peta" means 10^{15}). Gigatons are hard to imagine, but if you want to bring it down to a human scale, imagine burning one ton of coal (which is what you might use to heat a house over a year). Now imagine everyone on the planet burning one ton of coal per year: that's 6 GtC per year, because the planet has 6 billion people.

Where is the carbon?

Figure J.1 shows where the carbon is. Most of it $-40\,000\,\mathrm{Gt}$ – is in the ocean (in the form of dissolved CO_2 gas, carbonates, living plant and animal life, and decaying materials). Soils and vegetation together contain about 3700 Gt. Accessible fossil fuels – mainly coal – contain about 1600 Gt. Finally, the atmosphere contains about 600 Gt of carbon.

Until recently, all these pools of carbon were roughly in balance: all flows of carbon out of a pool (say, soils, vegetation, or atmosphere) were balanced by equal flows into that pool. The flows into and out of the fossil fuel pool were both negligible. Then humans started burning fossil fuels. This added two extra unbalanced flows, as shown in figure J.3.

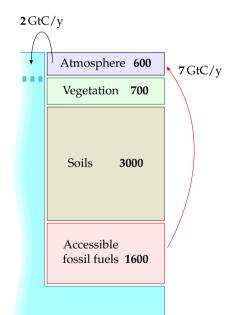
The rate of fossil fuel burning was roughly $1\,\text{GtC/y}$ in 1920, $2\,\text{GtC/y}$ in 1955, and $8.4\,\text{GtC}$ in 2006. (These figures include a small contribution from cement production, which releases CO_2 from limestone.)

How has this significant extra flow of carbon modified the picture shown in figure J.1? Well, it's not exactly known. Figure J.3 shows the key things that *are* known. Much of the extra 8.4 GtC per year that we're putting into the atmosphere stays in the atmosphere, raising the atmospheric concentration of carbon-dioxide. The atmosphere equilibrates fairly rapidly with the surface waters of the oceans (the equilibration has a five-year time-scale), and there is a net flow of CO₂ from the atmosphere into the surface waters of the oceans, amounting to 2 GtC per year. (Recent research indicates the rate of carbon-uptake by the oceans may be reducing.) This unbalanced flow into the surface waters causes ocean acidification, which is bad news for coral. Some extra carbon is moving into vegetation and soil too, perhaps about 1.5 GtC per year, but these flows are less well

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com



Figure J.2. The weights of an atom of carbon and a molecule of CO_2 are in the ratio 12 to 44, because the carbon atom weighs 12 units and the two oxygen atoms weigh 16 each. 12 + 16 + 16 = 44.



Ocean 40 000

measured. What is certain is that continued carbon pollution at a rate of 8.4 GtC per year will continue to increase CO₂ levels in the atmosphere, and in the surface waters.

What is the long-term destination of the extra CO_2 ? Well, since the amount in fossil fuels is so much smaller than the total in the oceans, 'in the long term' the extra carbon will make its way into the ocean, and the amounts of carbon in the atmosphere, vegetation, and soil will return to normal. However, 'the long term' means thousands of years. Equilibration between atmosphere and the *surface* waters is rapid, taking only a few tens of years. But figures J.1 and J.3 show a dashed line separating the surface waters of the ocean from the rest of the ocean. On a time-scale of fifty years, this boundary is virtually a solid wall. Radioactive carbon dispersed across the globe by the atomic bomb tests of the 1960s and 70s has penetrated the oceans to a depth of only about 400 m. In contrast the average depth of the oceans is about 4000 m.

The oceans circulate slowly: a chunk of deep-ocean water takes about 1000 years to roll up to the surface and down again. The circulation of the deep waters is driven by a combination of temperature gradients and salinity gradients, so it's called the thermohaline circulation (in contrast to the circulations of the surface waters, which are wind-driven).

This slow turn-over of the oceans has a crucial consequence: we have enough fossil fuels to seriously influence the climate over the next thousand years.

Where is the carbon going

Figure J.3 is a gross simplification. For example, humans are causing additional flows not shown on this diagram: the burning of peat and forests in Borneo in 1997 alone released about 0.7 GtC. Accidentally-started fires in coal seams release about 0.25 GtC per year.

Nevertheless, this cartoon helps us understand roughly what will happen in the short term and the medium term under various policies. First, if carbon pollution follows a "business as usual" trajectory, burning another 500 Gt of carbon over the next 50 years, we can expect the carbon to continue to trickle gradually into the surface waters of the ocean at a rate of 2 GtC per year. By 2055, at least 100 Gt of the 500 would have gone into the surface waters, and CO₂ concentrations in the atmosphere would be roughly double their pre-industrial levels.

If carbon pollution were halted in the 2050s, much of the 500 Gt we put into the atmosphere would gradually drift into the oceans over the next few thousand years, as the surface waters roll down and are replaced by new water from the deep.

Thus eventually our perturbation of the carbon concentration might eventually be righted, but only after thousand years. And that's assuming that this large perturbation of the atmosphere doesn't drastically alter the

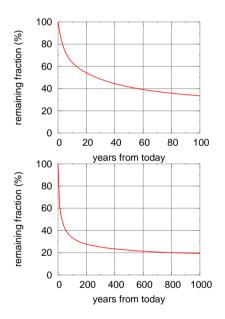


Figure J.4. Decay of a small pulse of CO_2 added to today's atmosphere, according to the Bern model of the carbon cycle.

ecosystem. It's conceivable, for example, that the acidification of the surface waters of the ocean might cause a sufficient extinction of ocean plantlife that a new vicious cycle kicks in: acidification means extinguished plant-life, means plant-life absorbs less CO₂ from the ocean, means oceans become even more acidic. Such vicious cycles (which scientists call "positive feedbacks" or "runaway feedbacks") have happened on earth before: it's believed, for example, that ice ages ended relatively rapidly because of positive feedback cycles in which rising temperatures caused surface snow and ice to melt, which reduced the ground's reflection of sunlight, which led to increased temperatures. (Melted snow - water - is much darker than snow.) Another positive feedback possibility to worry about involves methane hydrates, which are frozen in gigaton quantities in places like Arctic Siberia, and in 100-gigaton quantities on continental shelves. Global warming greater than 1 °C would possibly melt methane hydrates, which release methane into the atmosphere, which increases global warming more strongly than CO_2 does.

This isn't the place to discuss the uncertainties of climate change in any more detail. I highly recommend the books *Avoiding Dangerous Climate Change* and *Global Climate Change* Schellnhuber et al. [2006], Dessler and Parson [2006]. Hansen et al. [2007]. Charney et al. [1979].

Notes

page no.

- 353 *climate change ... was a controversial question*. Indeed there still is a "yawning gap between mainstream opinion on climate change among the educated elites of Europe and America" [voxbz].
- 355 Where is the carbon? Sources: Schellnhuber et al. [2006] Davidson and Janssens [2006].
 - The rate of fossil fuel burning... Source: Marland et al. [2007].
 - Recent research indicates carbon-uptake by the oceans may be reducing. http://www.timesonline.co.uk/tol/news/uk/science/article1805870. ece, http://www.sciencemag.org/cgi/content/abstract/1136188, [yofchc], Le Quéré et al. [2007].
- 356 Radioactive carbon ... has penetrated to a depth of only about 400 m. The mean value of the penetration depth of bomb 14 C for all observational sites during the late 1970s is $390\pm39\,\mathrm{m}$ (Broecker et al., 1995). From [3e28ed]
- 357 Global warming greater than 1°C would possibly melt methane hydrates. Source: [Hansen et al., 2007, p1942].

Part IV

Useful data

K Terminology

Words, words, words

Just so you know I've thought about some of the choices of words in this book, here are some responses to frequently asked questions and comments.

You refer to wind turbines as "windmills". They are not mills, because a mill is something that grinds grain (or coffee), not that produces electricity.

Windmills – I agree, perhaps the wrong noun. However, I like short words. (Wind turbine takes longer to say and write.) And I think the abuse of the word windmill, generalizing it to have the wider meaning, 'any wind machine', has a long pedigree. Imagine you are in 19th-century Holland, for example – what would you have called the things with four sails going round? Bear in mind that many of them were not grinding grain, but pumping water. Does anyone say 'I love the beautiful Dutch windpumps'? And what do people call the classic many-bladed wind machine of the American farmland? The Oxford English Dictionary defines a windmill to be 'a mill ... for grinding corn, pumping water ... or sawing.' The term 'windmill' has been used for general wind-powered machines since 1759. Finally, I like to use this word because it tweaks the noses of wind engineers who don't like their machines being confused with children's toys.

You refer to CO_2 "pollution". I think this term confuses the public. CO_2 is not a pollutant in the sense that the public understands the word – it has no discernable direct impact on humans until well above 1000 ppmv, and is directly beneficial to plants. Why not just say " CO_2 emissions"? The big concern is potentially catastrophic effects on climate, and the changes needed to avert this problem are far more fundamental than those needed to deal with any conventional pollution problem to date.

I have actually deliberately been through the book and changed almost all mentions of CO₂ "emission" to "pollution". I think unless we call it pollution, which is what it is when emitted on a 20 gigaton-per-year scale, we won't get action. I don't see a problem with the definition of the word "pollutant" including "something that has potentially catastrophic effects on climate".

If we call them emissions, then people will talk about "emissions rights" and go on about useless trading systems. The term "pollution rights" sticks in the throat more. Like "murder permit".

Give them an inch and they'll drive a mile.

Units

Watt. This SI unit is named after James Watt. As for all SI units whose names are derived from the proper name of a person, the first letter of its symbol is uppercase (W). But when an SI unit is spelled out, it should always be written in lowercase (watt), unless it begins a sentence or is the name "degree Celsius".

from wikipedia

SI stands for Système Internationale. SI units are the ones that all engineers should use, to avoid losing spacecraft.

SI units					
energy	one joule	1 J			
power	one watt	1 W			
force	one newton	1N = 1J/m			
length	one metre	1 m			
time	one second	1 s			

	My preferred units, expres	sed in S.I.	
energy power force	one kilowatt-hour one kilowatt-hour per day one kilowatt-hour per 100 km	1 kWh 1 kWh/d 1 kWh/100 km = 36 N	3600000 J (1000/24) W $\simeq 40 \text{ W}$
time	one hour one day one year	1h 1d 1y	$3600 \mathrm{s}$ $24 \times 3600 \mathrm{s} \simeq 10^5 \mathrm{s}$ $365.25 \times 24 \times 3600 \mathrm{s} \simeq \pi \times 10^7 \mathrm{s}$

Additional units

In this book I use the following additional units:

Thing measured	unit name	symbol	value
humans	person	р	
mass	tonne or ton	t	1 t = 1000 kg
			$1 \text{Gt} = 10^9 \times 1000 \text{kg} = 1 Pg$
transport	person-kilometre	p-km	
transport	ton-kilometre	t-km	
volume	litre	1	$11 = 1/1000 \mathrm{m}^3$
area	square kilometre	sq km, km²	$1 \text{sq km} = 10^6 \text{m}^2$
	hectare	ha	$1 \text{ha} = 10^4 \text{m}^2$
	Wales		$1 \text{Wales} = 21 000 \text{km}^2$
	London		$1 \operatorname{London} = 1500 \operatorname{km}^2$
energy	Dinorwig		1 Dinorwig = 9 GWh

[©] David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

For example, a bus that travels 10 km with 20 people on board has delivered an amount of personal transportation equal to 200 p-km. A truck that shifts 10 tons of stuff a distance of 100 km provides 1000 t-km of transport.

When I write $1 \text{ km}^2 \text{ I mean } 1 (\text{km})^2$, not 1000 m^2 .

When discussing millions, I use the prefix M (for example, one million tons of oil equivalent is written 1 Mtoe). When discussing money I use b for "billion".

Annoying units

homes

The "home" is the one of the most common units used to describe the power of a new wind farm. For example, The £300 million Whitelee project's 140 turbines will generate 322 MW – enough to power 200 000 homes." The "home" is defined by E-ON and the British Wind Energy Association to be 4700 kWh per year. That's 0.54 kW, or 13 kWh per day. http://www.bwea.com/ukwed/operational.asp [Some organizations use 4000 kWh/y per household. That means one "home" uses 11 kWh/d. Or 0.46 kW.]

The "home" annoys me because I worry that people forget all their other methods of energy consumption. They think that the statement "these windmills will power one million homes" means that *all* energy used by the people living in those homes is covered by the windmills. But what about the energy cost of their workplaces, of the stuff they buy, and of their transport habits?

If I announced a new renewable source that would provide enough power for "all the homes in Britain," I think many people would think we didn't need any more power than that. But using the standard exchange rates, the amount of power would be just 14 GW, which is only one third of current electricity consumption, and only one twentieth of the total power consumption of the UK.

Incidentally, when they talk of the CO₂ emissions of a "home", the official exchange rate appears to be 4 tonsCO₂ per home per year.

power stations

Energy saving ideas are sometimes described in terms of power stations. For example according to a BBC report on putting new everlasting LED lightbulbs in traffic lights, "The power savings would be huge – keeping the UK's traffic lights running requires the equivalent of two medium-sized power stations." http://news.bbc.co.uk/1/low/sci/tech/specials/sheffield_99/449368.stm

What is a medium-sized power station? $10\,\text{MW}$? $50\,\text{MW}$? $100\,\text{MW}$? $500\,\text{MW}$? I don't have a clue. A google search indicates that some people think it's $30\,\text{MW}$, some $250\,\text{MW}$, some $500\,\text{MW}$ (the most common choice), and some $800\,\text{MW}$. What a useless unit!

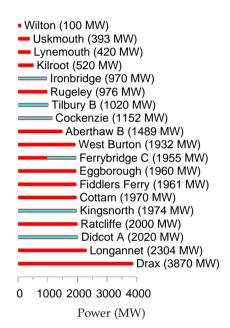


Figure K.1. Powers of Britain's coal power stations. I've highlighted 8 GW of generating capacity that will close by 2015. 3.4 GW of nuclear power will also close by 2015, and another 5.8 GW by 2019. 2500 MW, shared across Britain, is the same as 1 kWh per day per person.

Nobody knows how many medium power stations our country's power consumption corresponds to. Surely it would be clearer for the article about traffic lights to express what it's saying as a percentage? "Keeping the UK's traffic lights running requires *x* MW of electricity, which is *y* percent of the UK's electricity." The only problem with expressing traffic lights in such precise terms instead of hiding them behind the fuzzy veil of "medium-sized power stations" is that the resulting statement would not sound like "huge" power savings any more!

Here is my rewrite with the correct value of the power inserted (obtained from [2tsyxe]):

The power savings would be huge too – keeping the UK's traffic lights running requires 11 MW, which is about three tenthousandths of the nation's electricity. I'm sorry, did I say "huge"? I meant "hugely easy to exaggerate".

I think whoever came up with the original "two power stations" line here made a plain mistake. There is no way that 5 MW could be considered a "medium-sized power station" today! Figure K shows the powers of the UK's nineteen coal power stations. http://www.ukqaa.org.uk/PowerStation.html

cars taken off the road

I've recently noticed advertisements describing reductions in CO₂ pollution in terms of the "equivalent number of cars taken off the road." For example, Richard Branson asserts that if Virgin Trains' Voyager fleet switched to 20% biodiesel – incidentally, don't you feel it's outrageous that people call a train a "green" biodiesel-powered train when it runs on 80% fossil fuels and just 20% biodiesel?, Sorry, I got distracted. Richard Branson asserts that *if* Virgin Trains' Voyager fleet switched to 20% biodiesel – I emphasize the "*if*" because people like Beardie and BP are always getting media publicity for announcing that they are *thinking of* doing good things. Do they ever deliver? Sorry, I got distracted again. Richard Branson asserts that *if* Virgin Trains' Voyager fleet switched to 20% biodiesel, then there would be a reduction of 34500 tons of CO₂ per year, which is equivalent to "23000 cars taken off the road".

I'm grateful to Beardie for this statement because it reveals the exchange rate.

"one car taken off the road" \longleftrightarrow -1.5 tonsper year of CO₂

barrels

An annoying unit loved by the oil community. Why can't they just stick to one unit, such as the ton of oil? A barrel of oil is 6.1 GJ or 1700 kWh.

Barrels are doubly annoying because there are multiple definitions of barrels.

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

K — Terminology 363

One barrel is 42 U.S. gallons; 159 litres; One barrel of oil is 0.1364 tons of oil; 1 barrel of crude oil is 5.75 GJ. The carbon-pollution rate of crude oil is 400 kg of CO₂ per barrel. http://www.chemlink.com.au/conversions.htm

This means that when the price of oil is \$90 per barrel, people are paying \$5.4 per kWh, and they are paying \$225 per ton of CO_2 emitted.

1 ton of crude oil is 7.33 barrels and 42.1 GJ.

gallons

Gallons would be a fine human-sized unit, except the Americans messed it up by defining the gallon differently from everyone else. They've similarly messed up the pint and the quart. The US volumes are all roughly five-sixths of the correct volumes.

1 US gal = 3.7851 = 0.83 imperial gal. 1 imperial gal = 4.5451.

Tons

Tons are annoying because there are short tons, long tons and metric tons. They are close enough that I don't bother distinguishing between them. 1 short ton $(2000\,lb) = 907.2\,kg$; 1 long ton $(2240\,lb) = 1016\,kg$; 1 metric ton $= 1000\,kg$.

BTU and quads

British thermal units are annoying because they are neither part of the *Système Internationale*, nor are they of a useful size. They are too small, so you have to roll out silly prefixes like "quadrillion" (10¹⁵) to make practical use of them.

1 kJ is 0.947 BTU. 1 kWh is 3409 BTU

A "Quad" is 1 quadrillion BTU = 293 terawatt-hours.

Bushels

Bushels are what grains come in.

Before April 2007, wheat used to cost at most \$5 per bushel. In August 2007, wheat prices rose above \$7 per bushel.

Funny units

Cups of tea

Is this a way to make solar panels sound good? "Once all the 7000 photovoltaic panels are in place, it is expected that the solar panels will create 180000 units of renewable electricity each year - enough energy to make nine million cups of tea." This announcement thus equates 1kWh to 50 cups of tea.

As a unit of volume, 1 US cup (half a US pint) is officially 0.241; but a cup of tea or coffee is usually about 0.181. I confirm that to raise 50 cups of water, at 0.181 per cup, from $15\,^{\circ}$ C to $100\,^{\circ}$ C requires 1 kWh.

```
= 1 \text{ kWh}
                       1 unit
                                                    3.6 MJ
                   2500 kCal
                                    3 kWh
                                                    10000 kJ
                                    0.3 kWh
                        1 MJ
                   1000 BTU
                                    0.3 kWh
         1000 BTU per hour
                                    0.3 \, \text{kW}
                                                    7kWh/d
1 horse power (1 hp or 1 cv)
                                    0.75\,\mathrm{kW}
                                                    18kWh/d
                                    1 kW
                                                    24 kWh/d
```

Box K.2. How other energy and power units relate to the kilowatt-hour and the kilowatt-hour per day.

"Nine million cups of tea per year" is another way of saying "20 kW."

The solar panels are outdone by Pendolino trains however: the regenerative braking systems of Virgin's Pendolinos deliver enough energy to brew 2.6 billion cuppas a year!

The personal computer

The same solar panel advertisement says 180 000 kWh is "enough to power 1000 PCs for a year" http://www.cis.co.uk/servlet/Satellite?cid=1116834043897&pagename=CoopBank/Page/tplBlank&c=Page but that's not true. It would be true if a PC took only 20 W. But a typical PC takes 80 W or more.

Double-decker buses, Albert Halls and Wembley stadiums

"If everyone in the UK that could, installed cavity wall insulation, we could cut carbon dioxide emissions by a huge 7 million tons. That's enough carbon dioxide to fill nearly 40 million double-decker buses or fill the new Wembley stadium 900 times!"

From which we learn the helpful fact that one Wembley is 44 000 double decker buses.

"If every household installed just one energy saving light bulb, there would be enough carbon dioxide saved to fill the Royal Albert Hall 1,980 times!"

As I pointed out on p??, expressing amounts of CO_2 by volume rather than mass is a great way to make them sound big. Should "1kg of CO_2 per day" sound too small, just say "two hundred thousand litres of CO_2 per year"!

Wales

The Wales is a unit of area. One Wales is 20 000 km².

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

K — *Terminology* 365

Useful conversion rates				
Diesel	250 gCO ₂ /kWh			
Biodiesel	$320\mathrm{gCO_2/kWh}$			
Densities relative to water				
gasoline 0.74				
diesel	0.820-0.950			
Calorific value of fuel	10 kWh per litre			

Table K.3. Carbon dioxide emissions per unit energy (gross calorific value) of various fuels.

k	kilo	1000^{1}	10^{3}	1 000
M	mega	1000^{2}	10^{6}	1 000 000
G	giga	1000^{3}	10^{9}	1 000 000 000
T	tera	1000^{4}	10^{12}	1 000 000 000 000
P	peta	1000^{5}	10^{15}	1000000000000000
E	exa	1000^{6}	10^{18}	1000000000000000000

hectare	$= 10^4 \text{m}^2$	$=10^{-2} \mathrm{km}^2$
acre	$= 4050 \mathrm{m}^2$	$= 0.0040 \mathrm{km}^2$
square mile	$= 2.6 \times 10^6 \mathrm{m}^2$	$= 2.6 \mathrm{km}^2$
square foot	$= 0.093 \mathrm{m}^2$	$=9.3\times10^{-8}\mathrm{km}^2$
square yard	$= 0.84 \mathrm{m}^2$	$= 8.4 \times 10^{-7} \mathrm{km}^2$

Table K.4. Areas.

In this book, I use the square-kilometre and the square-metre as my two units of area. The hectare ($1\,ha=10\,000\,m^2$, a football field) would actually be a good choice of unit in which to measure areas per person, but I feel it is not as well known a unit as the square-kilometre and the square metre.

m/s	km/h	knot	mph	Beaufort				
				scale				
1	3.6	1.9	2.2	Force 1				
2	7.2	3.9	4.5	Force 2				
3	10.8	5.8	6.7	Force 2				
4	14.4	7.8	8.9	Force 3				
5	18.0	9.7	11.2	Force 3				
6	21.6	11.7	13.4	Force 4				
7	25.2	13.6	15.7	Force 4				
8	28.8	15.6	17.9	Force 4				
9	32.4	17.5	20.1	Force 5				
10	36.0	19.4	22.4	Force 5		1 /1	1 .	1
11	39.6	21.4	24.6	Force 5	m/s	km/h	knot	mph
12	43.2	23.3	26.8	Force 6				
13	46.8	25.3	29.1	Force 6	38	136.8	73.9	85.0
14	50.4	27.2	31.3	Force 6	39	140.4	75.8	87.2
15	54.0	29.2	33.6	Force 7	40	144.0	77.8	89.5
16	57.6	31.1	35.8	Force 7	41	147.6	79.7	91.7
17	61.2	33.0	38.0	Force 7	42	151.2	81.6	94.0
18	64.8	35.0	40.3	Force 8	43	154.8	83.6	96.2
19	68.4	36.9	42.5	Force 8	44	158.4	85.5	98.4
20	72.0	38.9	44.7	Force 8	45	162.0	87.5	100.7
21	75.6	40.8	47.0	Force 9	46	165.6	89.4	102.9
22	79.2	42.8	49.2	Force 9	47	169.2	91.4	105.1
23	82.8	44.7	51.5	Force 9	48	172.8	93.3	107.4
24	86.4	46.7	53.7	Force 9	49	176.4	95.3	109.6
25	90.0	48.6	55.9	Force 10	50	180.0	97.2	111.9
26	93.6	50.5	58.2	Force 10				
27	97.2	52.5	60.4	Force 10				
28	100.8	54.4	62.6	Force 10				
29	104.4	56.4	64.9	Force 11				
30	108.0	58.3	67.1	Force 11				
31	111.6	60.3	69.3	Force 11				
32	115.2	62.2	71.6	Force 11				
33	118.8	64.2	73.8	Force 12				
34	122.4	66.1	76.1	Force 12				
35	126.0	68.0	78.3	Force 12				
36	129.6	70.0	80.5	Force 12				
37	133.2	71.9	82.8	Force 12				

Meter reading

How to convert you gas-meter reading into kilowatt-hours.

- If the meter reads cubic feet, take the number of units used, and
- © David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

K — Terminology 367

multiply by 32.32 to get the number of kWh.

• If the meter reads **cubic metres**, take the number of units used, and multiply by **11.42** to get the number of kWh.

L Populations and areas

Region	Population	Land area	People	Area each
O	1	(km^2)	per km ²	(m^2)
		(KIII)	per kin	(111)
World	6 440 000 000	148 000 000	43	23 100
Asia	3 670 000 000	44 500 000	82	12 100
1 10101				
Africa	778000000	30 000 000	26	38 600
Europe	732000000	9 930 000	74	13500
North Ameri	ica 483 000 000	24 200 000	20	50200
Latin Americ	ca 342 000 000	17800000	19	52 100
Oceania	31 000 000	7680000	4	247 000
Antarctica	4000	13 200 000		

Table L.3. Population densities of the continents. These data are displayed graphically in figure 25.2 (p191).

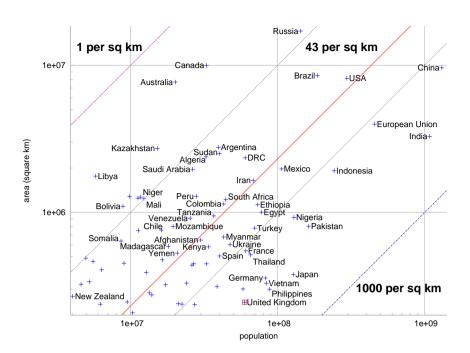
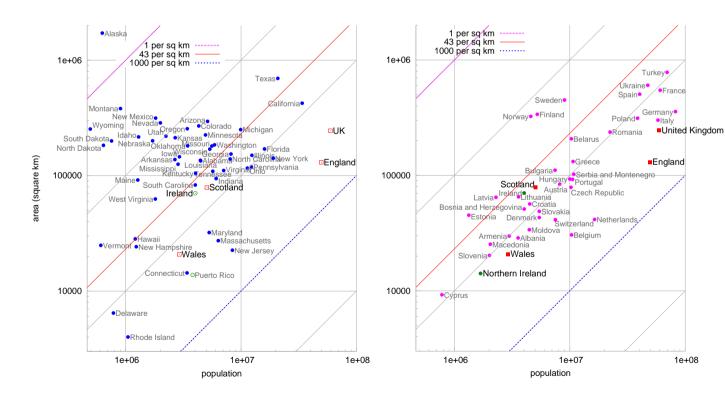


Figure L.1. Populations and areas of countries and regions of the world. Both scales are logarithmic. Sloping lines are lines of constant population density. This figure shows detail from figure 25.2 (p191).



Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

Figure L.2. Populations and areas of the States of America and regions around Europe.

Region	Population	Area	People	Area each
O	1	(km^2)	per km²	(m^2)
Antarctica	4 000	13 200 000		
Greenland	56 300	2 160 000	0.026	38 400 000
Alaska	655 000	1 480 000	0.44	2 260 000
Western Sahara	273 000	266 000	1	974 000
Mongolia	2 790 000	1 560 000	1.8	560 000
Namibia	2 030 000	825 000	2.5	406 000
Australia	20 000 000	7 680 000	2.6	382 000
Suriname	438 000	163 000	2.7	372 000
Botswana	1 640 000	600 000	2.7	366 000
Mauritania	3 080 000	1 030 000	3	333 000
Libya	5760000	1750000	3.3	305 000
Canada	32 800 000	9 980 000	3.3	304 000
Kazakhstan	15 100 000	2710000	6	178 000
CAR	3790000	622 000	6	163 000
Chad	9 820 000	1280000	8	130 000
Bolivia	8 850 000	1 090 000	8	124 000
Russia	143 000 000	17 000 000	8	119 000
Angola	11 100 000	1 240 000	9	111 000
Niger	11 600 000	1 260 000	9	108 000
Mali	12 200 000	1240000	10	100 000
Somalia	8 590 000	637 000	13	74200
Saudi Arabia	26 400 000	1 960 000	13	74 200
Algeria	32 500 000	2 380 000	14	73 200
Argentina	39 500 000	2760000	14	69 900
Zambia	11 200 000	752 000	15	66 800
New Zealand	4030000	268 000	15	66 500
Sudan	40100000	2 500 000	16	62 300
Chile	16 100 000	756 000	21	46 900
Peru	27 900 000	1280000	22	46 000
Brazil	186 000 000	8 510 000	22	45 700
Mozambique	19 400 000	801 000	24	41 300
DRC	60 000 000	2 340 000	26	39 000
Venezuela	25 300 000	912 000	28	35 900
Madagascar	18000000	587 000	31	32 500
USA (ex. Alaska)	295 000 000	8 150 000	36	27 600
South Africa	44300000	1 210 000	36	27 500
Colombia	42 900 000	1 130 000	38	26 500
Tanzania	36 700 000	945 000	39	25 700
Yemen	20 700 000	527 000	39	25 400
Iran	68 000 000	1 640 000	41	24 200
World	6 440 000 000	148 000 000	43	23 100

Table L.4. Some regions with population density *less than* or equal to the world average. Populations above 50 million and areas greater than 5 million km² are highlighted. These data are displayed graphically in figure 25.2 (p191). See p368 for an alphabetical table.

Region	Population	Area (km²)	People per km ²	Area each (m ²)
World	6 440 000 000	148 000 000	43	23 100
Afghanistan	29 900 000	647 000	46	21 600
Mexico	106 000 000	1970000	54	18 500
Ireland	4010000	70 200	57	17 500
Kenya	33 800 000	582 000	58	17 200
Myanmar	42 900 000	678 000	63	15 800
Scotland	5 050 000	78 700	64	15 500
Ethiopia	73 000 000	1 120 000	65	15 400
Egypt	77 500 000	1 000 000	77	12 900
Ukraine	47 400 000	603 000	78	12 700
Spain	40 300 000	504 000	80	12 500
Turkey	69 600 000	780 000	89	11 200
France	60 600 000	547 000	110	9 0 1 0
European Union	496 000 000	4330000	115	8720
Poland	39 000 000	313 000	124	8 000
Indonesia	241 000 000	1910000	126	7 930
Thailand	65400000	514 000	127	7850
China	1 300 000 000	9 590 000	136	7 3 4 0
Nigeria	128 000 000	923 000	139	7 170
Wales	2910000	20 700	140	7 110
Italy	58 100 000	301 000	192	5 180
Pakistan	162 000 000	803 000	202	4 940
Germany	82 400 000	357 000	230	4 3 3 0
United Kingdom	59 500 000	244 000	243	4 110
Vietnam	83 500 000	329 000	253	3 940
Philippines	87 800 000	300 000	292	3 4 1 0
India	1080000000	3 280 000	328	3 040
Japan	127 000 000	377 000	337	2960
England	49 600 000	130 000	380	2 630
South Korea	48400000	98 400	491	2 0 3 0
Taiwan	22 800 000	35 900	636	1 570
Bangladesh	144000000	144 000	1 000	997
Gaza Strip	1 370 000	360	3 820	261
Hong Kong	6 890 000	1 090	6310	158
Singapore	4420000	693	6 380	156

Table L.5. Some regions with population density *greater than* or equal to the world average. Populations above 50 million and areas greater than 5 million km² are highlighted. These data are displayed graphically in figure 25.2 (p191). See p368 for an alphabetical table.

Region	Population	Area	People	Area each
0	1	(km ²)	per km ²	(m^2)
Iceland	296 000	103 000	2.9	347 000
Norway	4 593 000	324 000	14	71 000
Finland	5 220 000	338 000	15	64 700
Sweden	9 000 000	449 000	20	49 900
Estonia	1 330 000	45 200	29	33 900
Latvia	2 290 000	64 500	35	28 200
Belarus	10 300 000	207 000	50	20 100
Lithuania	3 590 000	65 200	55	18 100
Ireland	4010000	70 200	57	17 500
Scotland	5 050 000	78 700	64	15 500
Bulgaria	7450000	110 000	67	14800
Ukraine	47400000	603 000	78	12700
Spain	40 300 000	504 000	80	12 500
Croatia	4490000	56 500	80	12 500
Greece	10 600 000	131 000	81	12 300
Republic of Macedonia	2 040 000	25 300	81	12 300
Turkey	69 600 000	780 000	89	11 200
Bosnia and Herzegovina	4 020 000	51 100	79	12700
Romania	22 300 000	237 000	94	10 600
Austria	8 180 000	83 800	98	10 200
Slovenia	2 010 000	20 200	99	10 000
Serbia and Montenegro	10 800 000	102 000	105	9 450
Hungary	10 000 000	93 000	107	9 290
France	60 600 000	547 000	110	9 0 1 0
Slovakia	5430000	48 800	111	8 990
Portugal	10500000	92 300	114	8 740
Albania	3 560 000	28 700	123	8 060
Poland	39 000 000	313 000	124	8 000
Denmark	5430000	43 000	126	7 9 3 0
Czech Republic	10 200 000	78 800	129	7700
Moldova	4450000	33 800	131	7 590
Wales	2910000	20 700	140	7 1 1 0
Switzerland	7480000	41 200	181	5 5 1 0
Italy	58 100 000	301 000	192	5 180
Germany	82 400 000	357 000	230	4330
United Kingdom	59 500 000	244 000	2 43	4 110
Belgium	10 000 000	31 000	340	2 945
England	49 600 000	130 000	380	2 630
Netherlands	16 400 000	41 500	395	2 5 3 0
Malta	398 000	316	1 260	792

Table L.6. Population densities of regions around Europe. These data are displayed graphically in figure L.2 (p369). See p368 for an alphabetical table.

Region	Population	Area	People	Area each
		(km^2)	per km²	(m^2)
Afghanistan	29 900 000	647 000	46	21 600
Africa	778 000 000	30 000 000	26	38 600
Alaska	655 000	1480000	0.44	2 260 000
Albania	3 560 000	28 700	123	8 060
Algeria	32 500 000	2380000	14	73 200
Angola	11 100 000	1 240 000	9	111 000
Antarctica	4 000	13 200 000		
Argentina	39 500 000	2760000	14	69 900
Asia	3 670 000 000	44500000	82	12 100
Australia	20 000 000	7680000	2.6	382 000
Austria	8 180 000	83 800	98	10 200
Bangladesh	144 000 000	144 000	1 000	997
Belarus	10 300 000	207 000	50	20 100
Belgium	10 000 000	31 000	340	2 945
Bolivia	8 850 000	1 090 000	8	124 000
Bosnia and Herzego	vina 4 020 000	51 100	79	12700
Botswana	1640000	600 000	2.7	366 000
Brazil	186 000 000	8 510 000	22	45 700
Bulgaria	7450000	110 000	67	14800
CAR	3 790 000	622 000	6	163 000
Canada	32 800 000	9 980 000	3.3	304 000
Chad	9 820 000	1280000	8	130 000
Chile	16 100 000	756 000	21	46 900
China	1300000000	9 590 000	136	7340
Colombia	42 900 000	1 130 000	38	26 500
Croatia	4490000	56 500	80	12 500
Czech Republic	10 200 000	78 800	129	7 700
DRC	60 000 000	2340000	26	39 000
Denmark	5 430 000	43 000	126	7 930
Egypt	77 500 000	1 000 000	77	12 900
England	49 600 000	130 000	380	2630
Estonia	1 330 000	45 200	29	33 900
Ethiopia	73 000 000	1 120 000	65	15 400
Europe	732 000 000	9 930 000	74	13 500
European Union	496 000 000	4 330 000	115	8 720
Finland	5 220 000	338 000	15	64 700
France	60 600 000	547 000	110	9 010

Table L.7. Regions and their population densities (alphabetical order). Populations above 50 million and areas greater than 5 million km² are highlighted. These data are displayed graphically in figure 25.2 (p191).

Region	Population	Area	People	Area each
		(km ²)	per km ²	(m^2)
Gaza Strip	1 370 000	360	3 820	261
Germany	82 400 000	357 000	230	4 3 3 0
Greece	10 600 000	131 000	81	12 300
Greenland	56 300	2 160 000	0.026	38 400 000
Hong Kong	6 890 000	1 090	6310	158
Hungary	10 000 000	93 000	107	9 290
Iceland	296 000	103 000	2.9	347 000
India	1080000000	3 280 000	328	3 040
Indonesia	241 000 000	1910000	126	7 9 3 0
Iran	68 000 000	1640000	41	24 200
Ireland	4010000	70 200	57	17 500
Italy	58 100 000	301 000	192	5 180
Japan	127000000	377 000	337	2960
Kazakhstan	15100000	2710000	6	178 000
Kenya	33 800 000	582 000	58	17 200
Latin America	342 000 000	17800000	19	52 100
Latvia	2 290 000	64 500	35	28 200
Libya	5 760 000	1750000	3.3	305 000
Lithuania	3 590 000	65 200	55	18 100
Madagascar	18 000 000	587 000	31	32 500
Mali	12 200 000	1 240 000	10	100 000
Malta	398 000	316	1 260	792
Mauritania	3 080 000	1 030 000	3	333 000
Mexico	106 000 000	1970000	54	18 500
Moldova	4450000	33 800	131	7 590
Mongolia	2790000	1560000	1.8	560 000
Mozambique	19 400 000	801 000	24	41 300
Myanmar	42 900 000	678 000	63	15 800
Namibia	2 030 000	825 000	2.5	406 000
Netherlands	16400000	41 500	395	2 5 3 0
New Zealand	4 030 000	268 000	15	66 500
Niger	11 600 000	1260000	9	108 000
Nigeria	128 000 000	923 000	139	7 170
North America	483 000 000	24 200 000	20	50 200

Table L.8. Regions and their population densities (alphabetical order). Populations above 50 million and areas greater than 5 million km² are highlighted. These data are displayed graphically in figure 25.2 (p191).

Region	Population	Area (km²)	People per km ²	Area each (m ²)
	4.500.000			
Norway	4 593 000	324 000	14	71 000
Oceania	31 000 000	7 680 000	4	247 000
Pakistan	162 000 000	803 000	202	4 940
Peru	27 900 000	1 280 000	22	46 000
Philippines	87 800 000	300 000	292	3 4 1 0
Poland	39 000 000	313 000	124	8 000
Portugal	10 500 000	92 300	114	8 740
Republic of Macedoni		25 300	81	12 300
Romania	22 300 000	237 000	94	10 600
Russia	143 000 000	17 000 000	8	119 000
Saudi Arabia	26 400 000	1 960 000	13	74 200
Scotland	5 050 000	78 700	64	15 500
Serbia and Montenego	o 10 800 000	102 000	105	9 450
Singapore	4420000	693	6 380	156
Slovakia	5 430 000	48 800	111	8 990
Slovenia	2 010 000	20 200	99	10 000
Somalia	8 590 000	637 000	13	74 200
South Africa	44 300 000	1 210 000	36	27 500
South Korea	48400000	98 400	491	2 0 3 0
Spain	40 300 000	504 000	80	12 500
Sudan	40 100 000	2 500 000	16	62 300
Suriname	438 000	163 000	2.7	372 000
Sweden	9 000 000	449 000	20	49 900
Switzerland	7480000	41 200	181	5 5 1 0
Taiwan	22 800 000	35 900	636	1 570
Tanzania	36 700 000	945 000	39	25 700
Thailand	65 400 000	514 000	127	7 850
Turkey	69 600 000	780 000	89	11 200
Ukraine	47 400 000	603 000	78	12 700
United Kingdom	59 500 000	244 000	2 43	4 110
USA (ex. Alaska)	295 000 000	8 150 000	36	27 600
Venezuela	25 300 000	912 000	28	35 900
Vietnam	83 500 000	329 000	253	3 940
Wales	2910000	20 700	140	7110
Western Sahara	273 000	266 000	1	974 000
World	6 440 000 000	148 000 000	43	23 100
Yemen	20 700 000	527 000	39	25 400
Zambia	11 200 000	752 000	15	66 800

Table L.9. Regions and their population densities (alphabetical order). Populations above 50 million and areas greater than 5 million km² are highlighted. These data are displayed graphically in figure 25.2 (p191).

M UK energy history

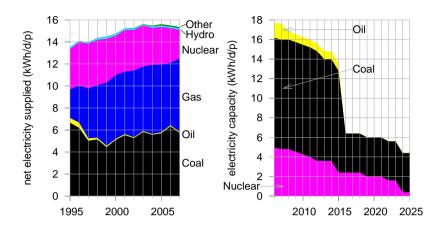


Figure M.1. Left: UK net electricity supplied, by source, in kWh per day per person. (Another 0.9 kWh/d/p is generated and used by the generators themselves.)

Right: the energy gap created by UK power station closures, as projected by energy company EdF. This graph shows the predicted *capacity* of nuclear, coal, and oil power stations, in kilowatt-hours per day per person. The capacity is the maximum deliverable power of a source.

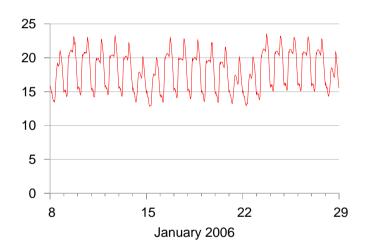
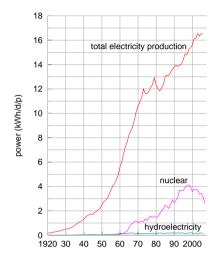


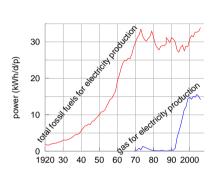
Figure M.2. Electricity demand in Great Britain (in kWh/d per person) during two winter weeks of 2006. The peaks in January are at 6pm each day. (If you'd like to obtain the national demand in GW, the top of the scale, 24 kWh/d per person, is the same as 60 GW per UK.)

	2006	2007
'Primary units' (the first 2 kWh/d)	10.73 p/kWh	17.43 p/kWh
'Secondary units' (the rest)	8.13 p/kWh	9.70 p/kWh

Table M.3. Domestic electricity charges (2006, 2007) for Powergen customers in Cambridge, including tax.

M — *UK energy history* 377





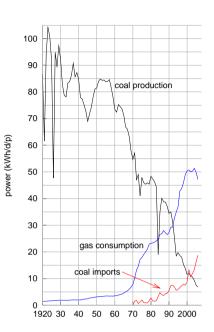


Figure M.4. History of UK production of electricity, hydroelectricity, and nuclear electricity. History of UK use of fossil fuels for electricity production. UK production and imports of coal, and UK consumption of gas. Powers are expressed "per person" by dividing each power by 60 million.

kWh/d/p Primary fuel kWh(e)/d/pOil 43 Natural gas 47 Coal 20 Nuclear 9 3.4 Hydro 0.2 Other renewables 0.8

Table M.5. Breakdown of primary energy sources in the UK (2004–2006).

N Quick reference

numbers

List of tables: Powers per unit area Transport efficiencies (kWh per 100 Passenger-km) Energy contents of fuels Carbon contents of fuels Things equivalent to one ton of CO₂ per year Energy conversion Power conversion Population densities

Powers per unit area

Put my own figures here.

	area per	$MW (m^2)$	
	Nuclear	630	
	Oil	870	(*)
From Hodgson nago 127 area nor MW (m²).	Gas	1500	
From Hodgson page 127, area per MW (m ²):	Coal	2400	(*)
	Solar	1000000	
	Hydro	265 000	
	Wind	1700000^*	

(of which much of the land can be used for other purposes, e.g. agriculture)

power density (W/m²)
Nuclear 1600
Oil 1150
Gas 670
Coal 420
Solar 1
Hydro 3.8
Wind 0.6

Energy conversion

 $1\,kWh=3.6\,MJ$ kJ/mol in eV: kT in eV and kJ/mol: 1 Food Calorie = 1000 calories = 4200 J.

 $1 \text{ TOE} = 10^7 \text{ kilocal} = 397 \text{ therms} = 41.9 \text{ GJ} = 11630 \text{ kWh}$ 100000 Btu = 1 therm = 29 kWh.

Power conversion

$$1 \text{ kWh/d} = \frac{1}{24} \text{ kW}$$

 $1 \text{ toe/y} = 1.33 \text{ kW}$

1 ton of CO_2 per year \leftrightarrow 3 kg CO_2 per day

Table N.1. Conversion rates for carbon emissions

Power from a petrol pump

Petrol comes out at about half a litre per second. So that's 10 kWh per 2 seconds, or 18 MW.

Power of a formula one racing car: 560 kW.

Energy contents of fuels

ton of coal equivalent = 29.3 GJ. = 8000 units of heat.

Coal LHV/HHV = 0.96.

Hydrocarbons: 30 000 kJ per kg

Fusion energy of ordinary water: 1800 kWh per litre.

 $1 \text{ kWh} \leftrightarrow 250 \text{ g of CO}_2 \text{ (oil, petrol)}$

for gas, $1 \text{ kWh} \leftrightarrow 200 \text{ g CO}_2$.

1kWh(e) = 0.445 kg CO2 from Gas 1kWh = 0.955 kg CO2 from Coal(from Carbon trust talk)

Petrol: 1 kWh \leftrightarrow 250 g of CO₂ (oil, petrol). 1 litre of fuel \leftrightarrow 10 kWh \leftrightarrow $2.2 \,\mathrm{kg}$ of CO_2 . (check)

Heat capacities

The heat capacity of water is $C = 4200 \,\text{J/litre/}^{\circ}\text{C}$.

The heat capacity of air is 1000 J/kg/°C. 1 kJ/kg/°C. Or 29 J/mol/°C. The density of air is 1.2 kg/m^3 .

So the heat capacity of air per unit volume is $1 \text{ kJ/kg/}^{\circ}\text{C} \times 1.2 \text{ kg/m}^{3} =$ $1.2 \, kJ/m^3/^{\circ}C$.

Latent heat of vaporization of water: 2257.92 kJ/kg. Water vapour's heat capacity: 1.87 kJ/kg/K. Water's heat capacity: 4.187 kJ/kg/K. Steam's density: $0.590 \,\mathrm{kg/m^3}$.

Name	exa	peta	tera	giga	mega	kilo	hecto	
Symbol Factor		P 10 ¹⁵	T 10 ¹²	G 10 ⁹	M 10 ⁶	k 10 ³	h 10 ²	
Name	centi	milli	micro	nano	pico	femto	atto	
Symbol Factor	_	m 10 ⁻³	$\frac{\mu}{10^{-6}}$	n 10 ⁻⁹	р 10 ⁻¹²	f 10 ⁻¹⁵	a 10 ⁻¹⁸	

Table N.2. SI prefixes

SI prefixes

Throughout this book "a billion" means an American billion, that is, 10^9 , or a thousand million. A trillion is 10^{12} . The standard prefix meaning 'billion' (10^9) is 'giga'.

In continental Europe, the abbreviations Mio and Mrd are used to mean million and billion respectively. Mrd is short for milliard, which means 10⁹.

The abbreviation m is often used to mean million, but this abbreviation is incompatible with the SI (think of mg (milligram) for example). So I don't use m to mean million. Where some people use m, I replace it by M. For example, I used Mtoe for million tons of oil equivalent, and $MtCO_2$ for million tons of CO_2 .

The abbreviation bn is often used to mean billion. I prefer b. But perhaps I should stick to bn.

Non-SI units

I use y for year, d for day, and p for person. Also t for ton.

p-km means passenger-kilometre or person-kilometre; t-km means ton-kilometre.

Assorted crazy units

For flow of water: $1 \text{Sv (sverdrup)} = 10^6 \text{ m}^3/\text{s}$.

Not to be confused with the SI unit of radiation (sievert), 1 Sv = 1 J/kg.

$2g CO_2 \leftrightarrow 1 litre$

Table N.3. Volume-to-mass conversion: every 44 g of CO₂ occupies 22 litres.

Carbon

It takes 2.1 billion tons of carbon to raise the atmospheric CO2 concentration by one part per million. If all the CO2 we pumped into the atmosphere stayed there, the concentration would be rising by more than three ppm per year – but it is actually rising only one and a half ppm annually.

Carbon intensity of steel and concrete

Steel: roughly 2 tons of CO₂ per ton of steel.

Concrete: a life-cycle analysis gives $43-240\,\mathrm{kg}$ CO₂ per ton, depending on the type of concrete, with $100\,\mathrm{kg}$ per ton of concrete as a median figure http://www.sustainableconcrete.org.uk/main.asp?page=210.

Cement: [6syoq1]Worrell et al. [2001]: "The average intensity of carbon dioxide emissions from global cement production is $222 \, \text{kg}$ of C/t of cement." (814 kg CO₂per t of cement).

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

N — Quick reference 381

Energy intensity of steel and concrete

Embodied energies: 32 MPa concrete: 5.85 GJ/m³. 5 MPa concrete: 2.03 GJ/m³. Steel (for use in road building): 68.6 GJ/t. Asphalt: 10.8 GJ/m³. Treloar et al. [2004]

Carbon intensity of electricity production

In the UK, latest figure for 2007: 505 tons CO₂ per GWh.

Source: PriceWaterHouse, EDF, www.manicore.com 2001

Temperatures

Standard swimming pool temperature: 28 °C, with the hall 1 °C warmer. Standard temperature for accommodation for elderly people: 20–21 °C. Average winter temperature of British houses in the 1970s: 12 °C.

Areas

The area of the globe is $500 \times 10^6 \, \text{km}^2$; the land area is $150 \times 10^6 \, \text{km}^2$.

Volumes

A container is 2.4 wide by 2.6 high by (6.1 or 12.2) metres long (for the TEU and FEU respectively).

One TEU is the size of a small 20-foot container – an interior volume of about $33 \,\mathrm{m}^3$. Most containers you see today are 40-foot containers with a size of 2 TEU. A 40-foot container weighs 4 tons and can carry 26 tons of stuff; its volume is $67.5 \,\mathrm{m}^3$.

A swimming pool has a volume of about 3000 m³.

An Albert Hall has a volume of roughly 100 000 cubic metres.

The great pyramid at Giza has a volume of 2500 000 cubic metres.

DUKES standards

In DUKES the standard multiplier is 1 TWh of electricity = 0.086 Mtoe. This means 1 Mtoe = 11.6 TWh(e).

UK electricity carbon emissions (DUKES 07): coal 239 tC per GWh; gas 101 tC per GWh; all fossil fuels $172 \, \text{tC/GWh}$; average for all electricity 131 tC/GWh. Or in grams of CO₂ per kWh: coal 876; gas 370; all fossil fuels 630; average for all electricity 480.

A price of €30 per ton of CO_2 implies €0.03 per kWh of electricity for coal generation.

Hmm, that figure for gas sounds smaller than normal?

France	83
Sweden	87
Canada	220
Austria	250
Belgium	335
European Union	353
Finland	399
Spain	408
Japan	483
Portugal	525
UK	580
Luxembourg	590
Germany	601
USA	613
Netherlands	652
Italy	667
Ireland	784
Greece	864
Denmark	881

Table N.4. Carbon intensity of electricity production (g CO₂ per kWh of electricity).

Emission factors of fuels (gCO_2/MJ): Coal: anthracite 96.8, bituminous coal 87.3, sub-bit 90.3, lignite 91.6 Wood: 78.4 Natural gas: 50 Distiliiate fuel oil 68.6 Residual fuel oil 73.9 Kerosene 67.8 LPG 59.1 Motor gasoline 69.3

World consumption

World power consumption is 15 TW. World electricity = 2 TW.

House size

USA: in the last 25 years, the average size of a single-family house has increased from 1740 square feet (162 m²) to 2330 square feet (216 m²).

UK: my 3-bedroom house has a floor area of 88 m².

Greenhouse gas intensities of economies

The UK's GHG intensity in 2006 was $458 \, t \, CO_2^{(e)}$ per \$M (at year 2000 prices) Helm et al. [2007]. China's was $4,140 \, t \, CO_2^{(e)}$ /\$M.

Energy intensities: the embodied energy intensity of of UK agriculture was 20 MJ of primary fossil energy use per US\$ in 1985. Battjes et al. [1998] (Which is roughly four times the direct energy intensity.) For UK industry, 22 MJ per US\$; UK transport, 24 MJ per \$; UK services, 12 MJ per \$. (All in 1985.)

Mode	g CO ₂ ^(e) per ton-km
7.5-ton truck	174
40-ton truck	56
Fast rail	39
Slow rail	14
Aircraft	3 4 1 4

Greenhouse-gas intensities of transport

Table N.5. Carbon dioxide emissions by freight transport (CO₂ equivalent).

_		MJ/t-km	kWh/t-km
	inland water	0.3	0.083
	rail	0.3	0.083
	truck	2.7	0.75
	air	10.0	2.8
Energy intensity of transport modes	oil pipeline	0.2	0.056
	gas pipeline	1.7	0.47
	int. air	10.0	2.8
	int. water container	0.2	0.056
	int. water bulk	0.2	0.056
	int. water tanker	0.1	0.028

That's US data from Weber and Matthews [2008].

⁽c) David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

N — *Quick reference* 383

Metabolism

 $1 \text{ ml } O_2 = 20.9 \text{ J}$. (Ranges from 19.6 to 21.15, depending on what you're burning.)

Fluxes

Incoming solar flux at ground level on a clear day: 240-250 W/m². Outgo-

ing flux from black bodies at temperatures of $0 \,^{\circ}\text{C}$ $4 \,^{\circ}\text{C}$ $10 \,^{\circ}\text{C}$ $20 \,^{\circ}\text{C}$ $316 \, \text{W/m}^2$ $335 \, \text{W/m}^2$ $364 \, \text{W/m}^2$ $419 \, \text{W/m}^2$

Nitrogen fertilizers: cost 80 GJ per ton to make.

Cattle feed: feed's calorific value is 13 GJ per ton.

Viscosity

 $\nu=\mu/\rho$. ν (kinematic viscosity) is in m²/s. The dynamic viscosity μ of water at 20 °C is 1.0020 cP (cgs unit) \simeq 1 mPa s (SI unit). That corresponds to a kinematic viscosity of $\mu\simeq 10^{-6}\,\mathrm{m}^2/\mathrm{s}$.

For a gas with average molecular speed \bar{u} , ν is related to mean free path λ by $\nu=2\bar{u}\lambda$.

Pressure

Atmospheric pressure: $1\,\mathrm{bar} \simeq 10^5\,\mathrm{Pa}$. Pressure under $1000\,\mathrm{m}$ of water: $100\,\mathrm{bar}$. Pressure under $3000\,\mathrm{m}$ of water: $300\,\mathrm{bar}$.

Densities

Sea water: 1027 kg/m^3 .

Specific density of rock: varies; roughly 2.8. (That is, density is 2800 kg/m³.)

Aluminium: 2.7.

Carbon dioxide at standard temperature and pressure: 2 kg/m³.

Useful conversion factors

To change TWh per year to GW, divide by 9.

1 kWh/d per person is the same as 2.5 GW per UK, or 22 TWh/y per UK.

To change mpg (miles per UK gallon) to km per litre, divide by 3.

The most useful numbers of all

Consumption

UK energy consumption is 125 kWh per day per person, or 300 GW per UK.

UK CO₂ emissions are 10 tons of CO₂ per year per person, or 600 Mt CO₂ per year per UK, or 160 Mt Carbon per year per UK. "Safe" global emissions would be one eighth of this: $1\frac{1}{4}$ tons of CO₂ per year per person.

UK electricity consumption is 17 kWh per day per person, or 42.5 GW per UK. UK electricity production emits 30% of UK CO₂.

Costs

Nuclear costs £30–37/MWh or 3–3.7 p/kWh.

Air-conditioning

'One ton' of air-conditioning = $3.5 \, kW$. According to three dudes on the internet, it's the heat removal-rate needed to freeze one ton of ice per day, and a standard average one ton A/C unit consumes $1.335 \, kW(e)$, and cools an area of $400 \, square$ feet.

Exchange rates

Coal: 1000 g of CO₂ per kWh electricity. Gas: 445 g of CO₂ per kWh electricity.

Nuclear: 30 g.

More numbers

ton of coal equivalent = 29.3 GJ. = 8000 units

ton of oil equivalent = 41.8GJ = 10 tons of TNT. = 12,000 UNITS

1Megaton = $4.2e15 \text{ J.} = 10^9 \text{ UNITS (actually 1.17e9)}$

USgal = 3.7851.

gasoline = \$3 per gallon to consumer in USA. Which is \$0.79 per litre.

UK average income \$34,000. (2004)

Cape Town / LHR return: your emissions are 2.82 tons of CO_2 . The cost to offset this CO_2 will be £21.18.

Climatecare.org: £7.50 per ton CO₂'offset'.

growaforest.com said 2.13 tons – 4 trees.

From co2Seq.tex 4 kWh of heat from fossil fuels is roughly 1 kg of CO₂ asserted that The Carbon impact of Gas was 0.5kg per unit (0.445 kg CO₂); and of coal, 1kg per unit (0.955 kg CO₂).]

	CO ₂	Carbon
Coal	$1000 \mathrm{g}\mathrm{CO}_2/\mathrm{kWh}(\mathrm{e})$	250 tC/GWh(e)
Gas	$400 \mathrm{g}\mathrm{CO}_2/\mathrm{kWh}(\mathrm{e})$	100 tC/GWh(e)
Nuclear	$16 g CO_2/kWh(e)^*$	$4.4\mathrm{tC/GWh(e)^*}$

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

Table N.6. Exchange rate between carbon emissions and electrical energy.

^{*)} The figure for nuclear depends on the source of the energy for nuclear fuel creation. Currently, the UK is highly dependent on fossil-fired electricity generation, making indirect emissions the primary source of nuclear CO₂ output. If nuclear plants replaced fossil-fired plants as the primary electricity generators, the CO₂ emissions for nuclear power would fall. (from Nuclear-paper2, Sustainable Development Commission p23)

N — *Quick reference* 385

Carbon coefficients

from ORNL [2hcgdh].

	carbon coefficient kg CO ₂ per kWh
coal	0.32
natural gas	0.18
jet fuel	0.24
motor gasoline	0.24

Heavy fuel oil - carbon emissions: 0.825 MtC/Mtoe.

Energy densities

coal: 20 GJ/ton. Crude oil: 37 MJ/l Natural gas: 38 MJ/m³

20 GJ per ton of dry wood.

Motor gasoline: 1 barrel = 0.1172 metric tons

Let's have a table converting between miles per gallon, miles per litre, miles per kilometre, and grammes CO₂ per kilometre

Lexus with a hybrid engine (emissions $184\,\mathrm{g}$ per km). The Lexus RX 400h CO₂ emissions are $192\,\mathrm{g/km}$. Toyota Prius (104g). 65.7mpg

Money

I assumed the following exchange rates when discussing money: $\leq 1 = \$1.26$; £1 = \$1.85; \$1 = \$1.12 Canadian. These exchange rates were correct in mid-2006.

Official conversion factors

These emission figures are taken from DEFRA's Environmental Reporting Guidelines for Company Reporting on Greenhouse Gas Emissions.

Fuel Type	Emissions (kg CO ₂ per kWh)
grid electricity	0.43
natural gas	0.19
gas/diesel oil	0.25
petrol	0.24
heavy fuel oil	0.26
coal	0.30
LPG	0.21
coking coal	0.30
jet kerosene	0.24
ethane	0.20
naptha	0.26
petroleum coke	0.34
refinery gas	0.20

By weight By volume Solid fuels kWh/ton litres/ton kWh/litre Coal (weighted average) 7,417 – Coke 8,445 – Liquid fuels kWh/ton litres/ton kWh/litre Crude oil (weighted average) 12,682 1,192 10.6 Petroleum products (weighted average) 12,751 – Ethane 14,071 2,730 5.2 Liquefied petroleum gas 13,721 1,850 7.4 Aviation turbine fuel 12,845 1,251 10.3 Motor spirit 13,087 1,362 9.6 Gas/diesel oil 12,668 1,187 10.7 Fuel oil 12,087 1,031 11.7 Power station oil 12,087 1,142 10.6 Gaseous fuels kWh/ton litres/ton kWh/m³ Natural gas – 11.00 Coke oven gas – 5.00 Blast furnace gas – 0.83 Landfill gas – 5.8-7.0* Sewage gas – 5.8-7.0* Solid renewables kWh/ton litres/ton kWh/m³ Domestic wood (2) 2,778 Industrial wood (3) 3,306 – 4,167 Straw 2,445 – Poultry litter General industrial waste 4,445 – 3,889 Hospital waste Municipal solid waste 2,639 – Refuse-derived waste 5,139 – 8,890 – Tyres Source: Annex A of the Digest of UK Energy Statistics 2005

```
1 \text{ therm} = 29.31 \text{ kWh}
1 \text{ Btu} = 0.2931 \times 10^{-3} \text{ kWh}
1 \text{ MJ} = 0.2778 \text{ kWh}
1 \text{ GJ} = 277.8 \text{ kWh}
1 \text{ toe} = 11630 \text{ kWh}
1 \text{ kcal} = 1.163 \times 10^{-3} \text{ kWh}
```

In DUKES, Electricity generated from renewables is converted to equivalent Mtoe using (*x*TWh) 0.085985. Nuclear has thermal efficiency of 38%.

$$1 \text{ kWh} = 0.03412 \quad 3412 \quad 3.6 \quad 86 \times 10^{-6} \quad 859.7$$

therms Btu MJ toe kcal

Conversion of fossil fuel burning to CO_2 concentration changes: 1 ppm is roughly 7.5 Gt CO_2/y .

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

Carbon per energy

Coal-fired plants produced a kilogram of carbon dioxide for every unit (kWh) of energy produced. In contrast, gas produces only half a kilogram and nuclear just 30g.

Quick reference - conversion factors

standards.tex

Things I need on every page

Surface Area of the planet Surface Area of the land Population of earth $1kWh = 3600 \ kJ$

USEFUL IDENTITIES 1kT per molecule = 2.5 kJ/mol 1 kWh = 3600 kJ

USEFUL IDENTITIES $1 kT = \frac{1}{40} \text{eV}$ Visible photon = 2 eV

--

Useful relationships $10^4\,\mathrm{K} \quad \leftrightarrow 1\,\mathrm{eV}$ Visible photon $\leftrightarrow 2\,\mathrm{eV}$

Conversion factors

Burning fossil fuels: $4 \text{ kWh(enthalpy)} \leftrightarrow 1 \text{ kg of CO}_2$

World: 43 people per km². England population density: 380 per km², or 2600 m² per person.

Energy density of petrol: 30 MJ/l or 40 MJ/kg.

European: 120 kWh/day.

THE BIG CONSUMPTION LIST

Food: Calories per day 2500 Cal = 10460 kJ = 10MJ = 2.9kWh = 3kWh

From BP Statistical Review. One million tons of oil produces about 4500 GWh of electricity in a modern power station. One ton of oil equivalent equals 42GJ of heat or 12,000 kWh.

One ton of oil per year is 32 kWh/day.

So 3.8 tons of oil per year is the same as 125 kWh/day; 9.8 toe per year is the same as 312 kWh/day (13kW).

1 British thermal unit (Btu) = 0.252 kcal = 1.055 kJ 1 kilowatt-hour (kWh) = 860 kcal = 3600 kJ = 3412 Btu

Calorific equivalents One ton of oil equivalent equals approximately: Heat units 10 million kilocalories 42 gigajoules 40 million Btu Solid fuels 1.5 tons

of hard coal 3 tons of lignite Gaseous fuels see natural gas and LNG table Electricity 12 megawatt-hours — — — — One million tons of oil produces about 4500 gigawatt-hours (= 4.5 terawatt-hours) of electricity in a modern power station.

List of web links

This section lists the full links corresponding to each of the tiny URLs mentioned in the text. Each item starts with the page number on which the tiny URL was mentioned. See also http://tinyurl.com/yh8xse (or http://www.inference.phy.cam.ac.uk/sustainable/book/tex/cft.url.html) for a clickable page with all URLs in this book.

```
iii f754 http://www.archive.org/web/web.php
18 ydoobr http://www.bbc.co.uk/radio4/news/anyquestions_transcripts_20060127.shtml
19 2jhve6 http://www.ft.com/cms/s/0/48e334ce-f355-11db-9845-000b5df10621.html
70 25e59w http://news.bbc.co.uk/1/low/uk_politics/7135299.stm
19 507mxk http://www.guardian.co.uk/environment/2007/dec/10/politics
19 5c4olc http://www.foe.co.uk/resource/press_releases/green_solutions_undermined_10012008.html
19 2fztd3 http://www.jalopnik.com/cars/alternative-energy/now-thats-some-high-quality-h20-car-runs-on-water-1777
19 26e8z http://news.bbc.co.uk/1/hi/sci/tech/3381425.stm
19 ykhayi http://politics.guardian.co.uk/terrorism/story/0,,1752937,00.html
20 16y5g http://www.grida.no/climate/ipcc_tar/wg1/fig3-1.htm
21 5qfkaw http://www.nap.edu/catalog.php?record_id=12181
21 2z2xg7 http://assets.panda.org/downloads/2_vs_3_degree_impacts_1oct06_1.pdf
21 yyxq2m http://www.bp.com/genericsection.do?categoryId=93&contentId=2014442
21 dzcqq http://www.defra.gov.uk/environment/climatechange/internat/pdf/avoid-dangercc.pdf
22 y98ys5 http://news.bbc.co.uk/1/hi/business/4933190.stm
32 5647rh http://www.dft.gov.uk/pgr/statistics/datatablespublications/tsgb/
33 27jdc5 http://www.dft.gov.uk/pgr/statistics/datatablespublications/energyenvironment/tsgbchapter3energyandthee
33 28abpm http://corporate.honda.com/environmentology/
33 nmn41 http://www.simetric.co.uk/si_liquids.htm
385 2hcgdh http://cta.ornl.gov/data/appendix_b.shtml
36 vxhhj http://www.cl.cam.ac.uk/research/dtg/weather/
36 tdvml http://www.phy.hw.ac.uk/resrev/aws/awsarc.htm
38 3fbufz http://www.ipcc.ch/ipccreports/sres/aviation/004.htm
38 3asmgy http://news.independent.co.uk/uk/transport/article324294.ece
38 9ehws http://www.boeing.com/commercial/747family/technical.html
38 3exmgv http://www.ryanair.com/site/EN/about.php?page=About&sec=environment
38 yrnmum http://www.grida.no/climate/ipcc/aviation/124.htm
39 36w5gz http://www.rolls-royce.com/community/downloads/environment04/products/air.html
48 3b7zdf http://www.communities.gov.uk/publications/planningandbuilding/generalizedlanduse
49 2rqloc http://www.metoffice.gov.uk/climate/uk/location/scotland/index.html
49 2szckw http://www.metoffice.gov.uk/climate/uk/stationdata/cambridgedata.txt
49 5hrxls http://eosweb.larc.nasa.gov/cgi-bin/sse/sse.cgi?+s01
49 6z9epq http://www.solarcentury.com/knowledge_base/images/solar_pv_orientation_diagram
49 39z5m5 http://news.bbc.co.uk/1/hi/world/europe/6505221.stm
49 2uk8q8 http://www.powerlight.com/about/press2006_page.php?id=59
51 2t17t6 http://www.reuk.co.uk/40-Percent-Efficiency-PV-Solar-Panels.htm
51 6hobq2 http://www.azonano.com/news.asp?newsID=4546
```

```
51 21sx6t http://www.udel.edu/PR/UDaily/2008/jul/solar072307.html
51 62ccou http://www.nrel.gov/news/press/2008/625.html
51 5hzs5v http://www.ens-newswire.com/ens/dec2007/2007-12-26-093.asp
52 2ahecp http://www.aps.org/meetings/multimedia/upload/The_Status_and_Outlook_for_the_Photovoltaics_Industry_
    David_E_Carlson.pdf
52 6kqq77 http://www.defra.gov.uk/erdp/pdfs/ecs/miscanthus-guide.pdf
62 ynjzej http://www.aceee.org/conf/06modeling/azevado.pdf
288 wbd8o http://www.ref.org.uk/energydata.php
70 25e59w http://news.bbc.co.uk/1/low/uk_politics/7135299.stm
70 2t2vjq http://www.guardian.co.uk/environment/2007/dec/11/windpower.renewableenergy
70 57984r http://www.businessgreen.com/business-green/news/2205496/critics-question-government
70 6oc3ja http://www.independent.co.uk/environment/green-living/donnachadh-mccarthy-my-carbonfree-year-767115.
70 5soq12 http://www.housebuildersupdate.co.uk/2006/12/eco-bollocks-award-windsave-ws1000.html
70 6g2jm5 http://www.carbontrust.co.uk/technology/technologyaccelerator/small-wind
83 5h69fm http://www.thepoultrysite.com/articles/894/economic-approach-to-broiler-production
84 5pwojp http://www.fertilizer.org/ifa/statistics/STATSIND/pkann.asp
84 5bj8k3 http://www.walkerscarbonfootprint.co.uk/walkers_carbon_footprint.html
84 3s576h http://www.permatopia.com/transportation.html
92 6xrm5q http://www.edf.fr/html/en/decouvertes/voyage/usine/retour-usine.html
99 yqbzl3 http://www.normanbaker.org.uk/downloads/Supermarkets\%20Fenal\%20Version.doc
100 yx7zm4 http://www.cancentral.com/funFacts.cfm
344 r22oz http://www-materials.eng.cam.ac.uk/mpsite/interactive_charts/energy-cost/NS6Chart.html
100 whrest http://www.transportation.anl.gov/pdfs/TA/106.pdf
100 y5as53 http://www.aluminum.org/Content/NavigationMenu/The_Industry/Government_Policy/Energy/Energy.htm
100 y2ktgg http://www.ssab.com/templates/Ordinary____573.aspx
100 y55ppn http://www.corusgroup.com/en/responsibility/environment/performance/climate_change/
101 61brab http://www.lindenau-shipyard.de/pages/newsb.html
102 354euo http://www.wasteonline.org.uk/resources/InformationSheets/Plastics.htm
108 slbae http://www.wisconsinproject.org/countries/israel/plut.html
108 yh45h8 http://www.usec.com/v2001_02/HTML/Aboutusec_swu.asp
108 t2948 http://www.world-nuclear.org/info/inf28.htm
109 yttg7p http://budget2007.treasury.gov.uk/page_09.htm
109 fcqfw http://www.mod.uk/DefenceInternet/AboutDefence/Organisation/KeyFactsAboutDefence/DefenceSpending.htm
109 2e4fcs http://press.homeoffice.gov.uk/press-releases/security-prebudget-report
109 33x5kc http://www.mod.uk/NR/rdonlyres/95BBA015-22B9-43EF-B2DC-DFF14482A590/0/gep_200708.pdf
109 35ab2c http://www.dasa.mod.uk/natstats/ukds/2007/c1/table103.html
109 yg5fsj http://siteresources.worldbank.org/DATASTATISTICS/Resources/GDP.pdf
109 yfgina http://www.sipri.org/contents/milap/milex/mex_major_spenders.pdf/download
118 uzek2 http://www.dti.gov.uk/energy/inform/dukes/
120 3av4s9 http://hdr.undp.org/en/statistics/
137 5qhvcb http://www.tramwayinfo.com/Tramframe.htm?http://www.tramwayinfo.com/tramways/Articles/Compair2.htm
142 4qgg8q http://www.newsweek.com/id/112733/output/print
143 5fbeg9 http://www.cfit.gov.uk/docs/2001/racomp/racomp/pdf/racomp.pdf
143 679rpc http://www.tfl.gov.uk/assets/downloads/environmental-report-2007.pdf
144 5cp27j http://www.eaton.com/EatonCom/ProductsServices/Hybrid/SystemsOverview/HydraulicHLA/index.htm
144 4wm2w4 http://www.citroenet.org.uk/passenger-cars/psa/berlingo/berlingo-electrique.html
```

[©] David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

List of web links 391

```
145 658ode http://www.greencarcongress.com/2008/02/mitsubishi-moto.html
147 czjjo http://corporate.honda.com/environment/fuel_cells.aspx?id=fuel_cells_fcx
147 5a3rvx http://automobiles.honda.com/fcx-clarity/specifications.aspx
162 36w8o7 http://www.nef.org.uk/gshp/gshp.htm
162 yok2nw http://www.eca.gov.uk/etl/find/_P_Heatpumps/detail.htm?ProductID=9868&FromTechnology=S_WaterSourcePacka
162 2dtx8z http://www.eca.gov.uk/NR/rdonlyres/6754FE19-C697-49DA-B482-DA9426611ACF/0/ETCL2007.pdf
162 2fd8ar http://www.geothermalint.co.uk/commercial/hydronicheatpumpranges.html
162 2wmuw7 http://news.yahoo.com/s/ap/20071231/ap_on_hi_te/solar_roads;_ylt=AuEFouXxz16nP8MRlInTJMms0NUE
169 yebuk8 http://www.dti.gov.uk/energy/sources/coal/index.html
169 e2m9n http://www.coal.gov.uk/resources/cleanercoaltechnologies/ucgoverview.cfm
169 yhxf8b http://www.worldenergy.org/wec-geis/publications/reports/ser/coal/coal.asp
184 5qntkb http://www.world-nuclear.org/info/reactors.htm
186 y3wnzr http://npc.sarov.ru/english/digest/132004/appendix8.html
186 32t5zt http://web.ift.uib.no/~lillestol/Energy_Web/EA.html
186 2qr3yr http://documents.cern.ch/cgi-bin/setlink?base=generic&categ=public&id=cer-0210391
186 ynk54y http://doc.cern.ch//archive/electronic/other/generic/public/cer-0210391.pdf
186 yl7tkm http://minerals.usgs.gov/minerals/pubs/mcs/1999/mcs99.pdf
186 yju4a4 http://www.uic.com.au/nip67.htm
186 yeyr7z http://taylorandfrancis.metapress.com/index/W7241163J23386MG.pdf
187 2k8y7o http://www.nei.org/resourcesandstats/
187 36y2e4 http://www.tatasteel.com/webzine/tatatech39/page14.htm
188 69vt8r http://www.osti.gov/energycitations/product.biblio.jsp?osti_id=7200593
188 6oby22 http://www.osti.gov/energycitations/product.biblio.jsp?osti_id=6773271&query_id=0
188 63121p http://pubs.acs.org/cgi-bin/abstract.cgi/jacsat/2002/124/i18/abs/ja003472m.html
188 wnchw http://www.feasta.org/documents/wells/contents.html?one/horelacy.html
188 t2948 http://www.world-nuclear.org/info/inf28.htm
188 ygwh8a http://www.world-nuclear.org/info/inf11.htm
189 321ouu http://www.npec-web.org/Essays/Essay050120Zalenski-FutureofNuclearPower.pdf
189 shrln http://www.enviros.com/vrepository/
215 ktd7a http://www.vrbpower.com/docs/news/2006/20060830\%20-\%20PR\%20-\%20Tapbury\%20Sale\%20-\%20Ireland\
    %20Windfarm.pdf
215 627ced http://www.vrbpower.com/docs/whitepapers/SEItechpaper1.pdf
215 5fas17 http://www.indexmundi.com/en/commodities/minerals/vanadium/vanadium_t7.html
216 2hxf6c http://www.eirgrid.com/EirGridPortal/DesktopDefault.aspx?tabid=Wind\%20Generation\%20Curve&TreeLinkMod
    1451&TreeLinkItemID=247
216 2199ht http://www.reuters.com/article/domesticNews/idUSN2749522920080228
216 3x2kvv http://www.reuters.com/article/rbssIndustryMaterialsUtilitiesNews/idUSL057816620080305
217 2n3pmb http://www.dynamicdemand.co.uk/pdf_fridge_test.pdf
217 2k8h4o http://www.int.iol.co.za/index.php?art_id=vn20080201045821205C890035
217 5cp27j http://www.eaton.com/EatonCom/ProductsServices/Hybrid/SystemsOverview/HydraulicHLA/index.htm
229 5os7dy http://tinyurl.com/5os7dy
229 yrw200 http://tinyurl.com/yrw200
236 2kz3hk http://www.sciamdigital.com/index.cfm?fa=Products.ViewIssuePreview&ARTICLEID_CHAR=EF195D69-2B35-221B-6
236 3717fr http://news.bbc.co.uk/1/low/sci/tech/6132826.stm
236 2qtr71 http://business.guardian.co.uk/story/0,,1971200,00.html
236 21q4j8 http://www.foe.co.uk/resource/briefings/paying_for_rail.pdf
236 2uraxb http://www.unlimited-spurt.org/
```

Prepublication draft 2.9.0. August 28, 2008 www.withouthotair.com

```
237 yu8em5 http://www.foe.co.uk/resource/reports/paying_for_better_transport.pdf
237 ylx4xq http://www.latimes.com/news/nationworld/nation/la-na-gatesx07jan07,0,4205044,full.story?coll=la-home-l
237 2nznsz http://www.greekembassy.org/Embassy/content/en/Article.aspx?office=3&folder=200&article=14269
237 3x2cr4 http://news.bbc.co.uk/1/hi/england/london/6151176.stm
237 2dd4mz http://news.bbc.co.uk/1/low/uk_politics/6391075.stm
239 7vlxp http://www.lse.ac.uk/collections/pressAndInformationOffice/newsAndEvents/archives/2005/IDCard_FinalRepo
239 2qhyw2 http://www.adfero.co.uk/news/news/buisness/government-spending-18-billion-on-external-advice-$461179.
    ht.m
239 2hddq9 http://news.bbc.co.uk/1/low/uk_politics/6316967.stm
239 324zyk http://www.planetark.com/dailynewsstory.cfm/newsid/38844/newsDate/7-Nov-2007/story.htm
239 2nfp2d http://www.statoil.com/statoilcom/svg00990.nsf?opendatabase&lang=en&artid=F5255D55E1E78319C1256FEF0044
239 39g2wz http://www.dillinger.de/dh/referenzen/linepipe/01617/index.shtml.en
239 3ac8sj http://www.hydro.com/ormenlange/en/
239 y7kg26 http://www.politics.co.uk/issue-briefs/economy/taxation/tobacco-duty/tobacco-duty-$366602.htm
240 8t7rd http://www.hermes-press.com/BushSaud.htm
240 2f3nar http://www.thirdworldtraveler.com/Zepezauer_Mark/SaudiArabia_Boomerang.html
240 2gajp8 http://www.nasa.gov/pdf/142459main_FY07_summary.pdf
240 ysncks http://news.bbc.co.uk/1/low/uk_politics/6205174.stm
240 r9fcf http://en.wikipedia.org/wiki/War_on_Drugs
240 2vq59t http://www.boston.com/news/globe/editorial_opinion/oped/articles/2007/08/01/the_63_billion_sham/
240 2f3nar http://www.thirdworldtraveler.com/Zepezauer_Mark/SaudiArabia_Boomerang.html
240 ym46a9 https://www.cia.gov/cia/publications/factbook/print/xx.html
240 99bpt http://www.guardian.co.uk/Iraq/Story/0,2763,1681119,00.html
241 do me http://www.guardian.co.uk/environment/2007/aug/13/renewableenergy.energy
241 do me http://image.guardian.co.uk/sys-files/Guardian/documents/2007/08/13/RenewablesTargetDocument.pdf
247 2ykfgw http://www.guardian.co.uk/environment/2007/jan/09/travelsenvironmentalimpact.greenpolitics
248 2nsvx2 http://www.number-10.gov.uk/output/Page10300.asp
248 yxq5xk http://commentisfree.guardian.co.uk/george_monbiot/2007/01/an_open_letter_to_the_prime_mi.html
253 25e5rv http://news.bbc.co.uk/1/hi/6441103.stm?lsm
257 2wegkm http://news.bbc.co.uk/1/hi/sci/tech/6266082.stm
262 3doaeg http://web.archive.org/web/20040401165322/http://members.cox.net/weller43/sunshine.htm
276 2bhu35 http://www.lafn.org/~dave/trans/energy/rail_vs_auto_EE.html
280 6by8x http://encarta.msn.com/encyclopedia_761553622/Internal-Combustion_Engine.html
280 348whs http://www.cleangreencar.co.nz/page/prius-petrol-engine
286 6086ec http://www.londonarray.com/london-array-project-introduction/offshore/
287 ydt7uk http://www.nrel.gov/business_opportunities/pdfs/31235sow.pdf
287 yaoonz http://www.windpower.org/en/tour/wres/shear.htm
287 6bkvbn http://www.timesonline.co.uk/tol/news/world/asia/article687157.ece
288 yekdaa http://www.windpower.org/en/stat/betzpro.htm
288 ymfbsn http://www.windpower.org/en/tour/wres/powdensi.htm
288 ypvbvd http://www.ref.org.uk/images/pdfs/UK_Wind_Phase_1_web.pdf
288 wbd8o http://www.ref.org.uk/energydata.php
297 33ptcg http://www.stevefossett.com/html/main_pages/records.html
299 6r32hf http://www.theaustralian.news.com.au/story/0,25197,23003236-23349,00.html
301 20atgv http://news.bbc.co.uk/2/hi/business/5251546.stm
301 2af5gw http://www.airliners.net/info/stats.main?id=100
301 32judd http://www.wildanimalsonline.com/birds/wanderingalbatross.php
```

© David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com

List of web links 393

```
301 2qbquv http://news.bbc.co.uk/1/low/sci/tech/6988720.stm
301 5h6xph http://www.goldcoastyachts.com/fastcat.htm
305 3ap71c http://www.biocap.ca/files/Ont_bioenergy_OPA_Feb23_final.pdf
306 2mxsj9 http://www.questia.com/PM.qst?a=o&se=gglsc&d=98559826
315 65h3cb http://www.dorset-technical-committee.org.uk/reports/U-values-of-elements-Sept-2006.pdf
317 5mo7fd http://www.heatpumpnet.org.uk/files/gir72.pdf
321 5r6c7t http://www.arct.cam.ac.uk/UCPB/Place.aspx?rid=97996&p=6&ix=11&pid=1&prcid=27&ppid=201
321 5dhups http://www.arct.cam.ac.uk/UCPB/Place.aspx?rid=943658&p=6&ix=8&pid=1&prcid=27&ppid=201
342 s8dry http://www.foe.co.uk/resource/briefings/severn_barrage_lagoons.pdf
343 2bqapk http://wwwphys.murdoch.edu.au/rise/reslab/resfiles/tidal/text.html
343 2bqapk http://wwwphys.murdoch.edu.au/rise/reslab/resfiles/tidal/text.html
344 r22oz http://www-materials.eng.cam.ac.uk/mpsite/interactive_charts/energy-cost/NS6Chart.html
357 voxbz http://news.bbc.co.uk/1/low/business/6247371.stm
357 yofchc http://news.bbc.co.uk/1/low/uk/7053903.stm
357 3e28ed http://www.grida.no/climate/ipcc_tar/wg1/118.htm
362 2tsyxe http://www.reuk.co.uk/UK-Traffic-Lights-57000-Tonnes-Of-C02.htm
380 6syoql http://arjournals.annualreviews.org/doi/abs/10.1146/annurev.energy.26.1.303
385 2hcgdh http://cta.ornl.gov/data/appendix_b.shtml
```

- W. A. Amos. Updated cost analysis of photobiological hydrogen production from Chlamydomonas reinhardtii green algae milestone completion report, January 2004. URL http://www.nrel.gov/docs/fy04osti/35593.pdf.
- K. Anderson, A. Bows, S. Mander, S. Shackley, P. Agnolucci, and P. Ekins. Decarbonising modern societies: Integrated scenarios process and workshops: Tyndall centre technical report 48. Technical report, Tyndall Centre, 2006. URL http://www.tyndall. ac.uk/research/theme2/final_reports/t3_24.pdf.
- M. D. Archer and J. Barber. Photosynthesis and photoconversion. In M. D. Archer and J. Barber, editors, *Molecular to Global Photosynthesis*. World Scientific, 2004. ISBN 978-1-86094-256-3. URL http://www.worldscibooks.com/lifesci/p218.html.
- W. Ashworth and M. Pegg. The history of the British coal industry. Vol. 5, 1946–1982: the nationalized industry. Clarendon, Oxford, 1986. ISBN 0198282958.
- G. Asplund. Sustainable energy systems with hvdc transmission. In *Power Engineering Society General Meeting*, volume 2, pages 2299–2303. IEEE, 2004. doi: 10.1109/PES.2004.1373296. URL http://www.trec-uk.org.uk/reports/HVDC_Gunnar_Asplund_ABB.pdf.
- B. Asselbergs, J. Bokhorst, R. Harms, J. van Hemert, L. van der Noort, C. ten Velden, R. Vervuurt, L. Wijnen, and L. van Zon. Size does matter the possibilities of cultivating jatropha curcas for biofuel production in cambodia, December 2006. URL http://environmental.scum.org/biofuel/jatropha/.
- P. Baer and M. Mastrandrea. High stakes: Designing emissions pathways to reduce the risk of dangerous climate change, 2006. URL http://www.ippr.org/publicationsandreports/.
- M. P. Bahrman and B. K. Johnson. The ABCs of HVDC transmission technology. *IEEE Power and Energy Magazine*, 5(2), 2007.
- J. A. Baines, V. G. Newman, I. W. Hanna, T. H. Douglas, W. J. Carlyle, I. L. Jones, D. M. Eaton, and G. Zeronian. Dinorwig pumped storage scheme. *Institution of Civil Engineers Proceedings pt.* 1, 74: 635–718, November 1983.
- J. A. Baines, V. G. Newman, I. W. Hanna, T. H. Douglas, W. J. Carlyle, I. L. Jones, D. M. Eaton, and G. Zeronian. Dinorwig pumped storage scheme. *Institution of Civil Engineers Proceedings pt. 1*, 80: 493–536, April 1986.
- C. Baker, J. Walbancke, and P. Leach. Tidal lagoon power generation scheme in swansea bay, 2006. URL http://www.dti.gov.uk/ files/file30617.pdf. A report on behalf of the Department of Trade and Industry and the Welsh Development Agency.
- J. J. Battjes, K. J. Noorman, and W. Biesiot. Assessing the energy intensities of imports. *Energy Economics*, 20(1):67–83, February 1998.
- Bayer Crop Science. Potential of GM winter oilseed rape to reduce the environmental impact of farming whilst improving farmer incomes, 2003. URL http://tinyurl.com/5j99df.

- M. Binder, M. Faltenbacher, M. Kentzler, and M. Schuckert. Clean urban transport for europe. deliverable d8 final report, 2006. URL http://www.fuel-cell-bus-club.com/.
- Black and Veatch. The UK tidal stream resource and tidal stream technology, 2005. report prepared for the Carbon Trust Marine Energy Challenge. http://www.carbontrust.co.uk/technology/technologyaccelerator/tidal_stream.htm.
- L. S. Blunden and A. S. Bahaj. Tidal energy resource assessment for tidal stream generators. *Proc. IMechE*, 221 Part A:137–146, 2007.
- J. S. Boyer. Plant productivity and environment. *Science*, 218(4571): 443 448, October 1982. doi: 10.1126/science.218.4571.443.
- A. L. Braslow. A History of suction-Type Laminar-Flow control with emphasis on Flight Research. Number 13 in Monographs in Aerospace History. NASA, 1999. URL http://www.nasa.gov/centers/dryden/pdf/88792main_Laminar.pdf.
- A. Burnham, M. Wang, and Y. Wu. Development and applications of GREET 2.7 the transportation vehicle-cycle model, February 2007. URL http://www.transportation.anl.gov/software/GREET/publications.html.
- Carbon Trust. Micro-CHP accelerator interim report, November 2007. URL http://www.carbontrust.co.uk/publications/publicationdetail.htm?productid=CTC726. report number CTC726.
- L. Carlsson. "Classical" HVDC: still continuing to evolve. *Modern Power Systems*, June 2002.
- D. E. Cartwright, A. C. Edden, R. Spencer, and J. M. Vassie. The tides of the northeast Atlantic Ocean. *Philos. Trans. R. Soc. Lond. Ser. A*, 298(1436):87–139, 1980.
- R. H. Charlier. Sustainable co-generation from the tides: A review. Renewable and Sustainable Energy Reviews, 7:187213, 2003a.
- R. H. Charlier. A "sleeper" awakes: tidal current power. Renewable and Sustainable Energy Reviews, 7:515529, 2003b.
- J. G. Charney, A. Arakawa, D. J. Baker, B. Bolin, R. E. Dickinson, R. M. Goody, C. E. Leith, H. M. Stommel, and C. I. Wunsch. Carbon dioxide and climate: A scientific assessment, 1979. URL http://www.nap.edu/catalog.php?record_id=12181.
- R. Chitrakar, H. Kanoh, Y. Miyai, and K. Ooi. Recovery of lithium from seawater using manganese oxide adsorbent (H_{1.6}Mn_{1.6}O₄) derived from Li_{1.6}Mn_{1.6}O₄. *Ind. Eng. Chem. Res.*, 40(9):2054–2058, 2001. URL http://pubs.acs.org/cgi-bin/abstract.cgi/iecred/2001/40/i09/abs/ie000911h.html.
- R. A. Church, A. Hall, and J. Kanefsky. The history of the British coal industry. Vol. 3, 1830–1913: Victorian pre-eminence. Clarendon, Oxford, 1986. ISBN 0198282842.
- B. L. Cohen. Breeder reactors: A renewable energy source. American Journal of Physics, 51(1):75-76, 1983. URL http://sustainablenuclear.org/PADs/pad11983cohen.pdf.
- D. Coley. Emission factors for walking and cycling, April 2001.

- URL http://www.centres.ex.ac.uk/cee/publications/reports/91.html.
- Committee on Radioactive Waste Management. Managing our radioactive waste safely, January 2006. URL http://www.corwm.org.uk/Pages/Current%20Publications/700%20-%20CoRWM%20July%202006%20Recommendations%20to%20Government.pdf.
- CUTE. Clean urban transport for europe. detailed summary of achievements, 2006. URL http://www.fuel-cell-bus-club.com/.
- D. Dajnak and F. C. Lockwood. Use of thermal energy from waste for seawater desalination. *Desalination*, 130:137–146, 2000.
- E. A. Davidson and I. A. Janssens. Temperature sensitivity of soil carbon decomposition and feedbacks to climate change. *Nature*, 440:165–173, March 2006. doi: doi:10.1038/nature04514. URL http://www.nature.com/nature/journal/v440/n7081/full/nature04514.html.
- K. S. Deffeyes and I. D. MacGregor. World uranium resources. *Scientific American*, pages 66–76, January 1980.
- P. Denholm, G. L. Kulcinski, and T. Holloway. Emissions and energy efficiency assessment of baseload wind energy systems. *Environ Sci Technol*, 39(6):1903–1911, March 2005. ISSN 0013-936X. URL http://www.ncbi.nlm.nih.gov/entrez/query.fcgi?cmd=Retrieve&db=pubmed&dopt=Abstract&list_uids=15819254.
- R. A. Denison. Life-cycle assessment for paper products. In National Research Council, editor, Wood in Our Future: The Role of Life-Cycle Analysis: Proceedings of a Symposium. National Academy Press, 1997. ISBN 0309057450. URL http://books.nap.edu/openbook.php?record_id=5734.
- Department for Transport. Transport statistics great britain, 2007. URL http://www.dft.gov.uk/pgr/statistics/datatablespublications/tsgb/.
- Department of Defense. More fight less fuel, February 2008.
- Department of Trade and Industry. DTI atlas of UK marine renewable energy resources, December 2004.
- Department of Trade and Industry. Energy consumption in the United Kingdom, 2002a. URL http://www.berr.gov.uk/files/file11250.pdf.
- Department of Trade and Industry. Future offshore, 2002b. URL www.berr.gov.uk/files/file22791.pdf.
- Department of Trade and Industry. Impact of banding the renewables obligation costs of electricity production, 2007. URL www.berr.gov.uk/files/file39038.pdf.
- A. E. Dessler and E. A. Parson. The Science and Politics of Global Climate Change – A Guide to the Debate. Cambridge Univ. Press, Cambridge, 2006. ISBN 9780521539418.
- P. E. di Prampero, G. Cortili, P. Mognoni, and F. Saibene. Equation of motion of a cyclist. *J. Appl. Physiology*, 47:201–206, 1979. URL http://jap.physiology.org/cgi/content/abstract/47/1/201.

J. Diamond. Collapse: How Societies Choose to Fail or Succeed. Penguin, 2004

- E4tech. A review of the UK innovation system for low carbon road transport technologies, March 2007. URL http://www.dft.gov.uk/pgr/scienceresearch/technology/lctis/e4techlcpdf.
- D. Eckhartt. Nuclear fuels for low-beta fusion reactors: Lithium resources revisited. *Journal of Fusion Energy*, 14(4):329-341, December 1995. ISSN 0164-0313 (Print) 1572-9591 (Online). doi: 10.1007/BF02214511. URL http://www.springerlink.com/content/35470543rj8t2gk1/.
- R. Eddington. Transport's role in sustaining the uk's productivity and competitiveness, December 2006.
- R. Eden and R. Bending. Gas/electricity competition in the UK, February 1985.
- D. L. Elliott, L. L. Wendell, and G. L. Gower. An assessment of windy land area and wind energy potential in the contiguous united states, 1991. URL http://www.osti.gov/energycitations/ servlets/purl/5252760-ccu0pk/.
- Energy for Sustainable Development Ltd. English partnerships sustainable energy review, March 2003.
- A. U. Erdincler and P. A. Vesilind. Energy recovery from mixed waste paper. Waste Management & Research, 11(6):507–513, 1993. doi: 10.1177/0734242X9301100605.
- D. Etheridge, L. Steele, R. Langenfelds, R. Francey, J.-M. Barnola, and V. Morgan. Historical CO₂ records from the Law Dome DE08, DE08-2, and DSS ice cores. In *Trends: A Compendium of Data on Global Change*. Carbon Dioxide Information Analysis Center, Oak Ridge National Laboratory, U.S. Department of Energy, Oak Ridge, Tenn., USA, 1998. URL http://cdiac.ornl.gov/trends/co2/lawdome.html.
- European Commission. Concentrating solar power from research to implementation, 2007. URL http://www.solarpaces.org/Library/library.htm.
- D. G. Evans. Liquid transport biofuels technology status report, 2007. URL http://www.nnfcc.co.uk/.
- R. K. Evans. An abundance of lithium, July 2008. URL www.worldlithium.com.
- T. E. Faber. Fluid dynamics for physicists. Cambridge University Press, Cambridge, 1995.
- D. Faiman, D. Raviv, and R. Rosenstreich. Using solar energy to arrest the increasing rate of fossil-fuel consumption: The southwestern states of the USA as case studies. *Energy Policy*, 35:567576, 2007.
- B. Fies, T. Peterson, and C. Powicki. Solar photovoltaics expanding electric generation options, December 2007. URL http://mydocs.epri.com/docs/SEIG/1016279_Photovoltaic_White_Paper_1207.pdf.
- K. Fisher, E. Wallén, P. P. Laenen, and M. Collins. Battery waste management life cycle assessment, 2006. URL http://www.defra.gov.uk/environment/waste/topics/batteries/pdf/erm-lcareport0610.pdf.

R. A. Flather. A tidal model of the north-west European continental shelf. *Memoires Société Royale des Sciences de Liège*, 10(6):141–164, 1976.

- M. W. Flinn and D. Stoker. The history of the British coal industry. Vol. 2, 1700–1830: the Industrial Revolution. Clarendon, Oxford, 1984. ISBN 0198282834.
- G. Francis, R. Edinger, and K. Becker. A concept for simultaneous wasteland reclamation, fuel production, and socio-economic development in degraded areas in india: Need, potential and perspectives of Jatropha plantations. *Natural Resources Forum*, 29 (1):12–24, 2005. doi: http://dx.doi.org/10.1111/j.1477-8947.2005. 00109.x.
- J. Franklin. Principles of cycle planning, 2007. URL http://www.cyclenetwork.org.uk/papers/071119principles.pdf.
- Friends of the Earth Cymru. A Severn barrage or tidal lagoons?, January 2004. URL http://www.foe.co.uk/resource/briefings/severn_barrage_lagoons.pdf.
- G. Gabrielli and T. von Kármán. What price speed? Mechanical Engineering, 72(10), 1950.
- C. Garrett and P. Cummins. The power potential of tidal currents in channels. *Proceedings of the Royal Society A*, 461(2060):2563–2572, 2005. URL http://dx.doi.org/10.1098/rspa.2005.1494.
- C. Garrett and P. Cummins. The efficiency of a turbine in a tidal channel. J Fluid Mech, 588:243–251, 2007. URL http://journals.cambridge.org/production/action/cjoGetFulltext?fulltextid=1346064.
- C. W. Gellings and K. E. Parmenter. Energy efficiency in fertilizer production and use. In C. W. Gellings and K. Blok, editors, *Efficient Use and Conservation of Energy*, Encyclopedia of Life Support Systems (EOLSS). Eolss Publishers, Oxford ,UK, 2004. URL http://www.eolss.net.
- German Aerospace Center (DLR) Institute of Technical Thermodynamics Section Systems Analysis and Technology Assessment. Concentrating solar power for the Mediterranean region, 2006. Study commissioned by Federal Ministry for the Environment, Nature Conservation and Nuclear Safety Germany. See also http://www.dlr.de/tt/med-csp.
- D. Goodstein. *Out of Gas.* W. W. Norton and Company, New York, 2004. ISBN 0393058573.
- J. E. Green. Civil aviation and the environment the next frontier for the aerodynamicist. *Aeronautical Journal*, 110(1110):469–486, August 2006.
- M. Grubb and D. Newbery. Pricing carbon for electricity generation: national and international dimensions. In T. J. Michael Grubb and M. G. Pollitt, editors, *Delivering a Low Carbon Electricity System: Technologies, Economics and Policy*. Cambridge University Press, Cambridge, 2008.
- J. A. Halkema. Wind energy: Facts and fiction, 2006. URL http://www.countryguardian.net/ halkema-windenergyfactfiction.pdf.
- G. Hammond and C. Jones. Inventory of carbon & energy (ICE), 2006. URL http://www.bath.ac.uk/mech-eng/sert/embodied/. version 1.5a Beta.

- T. J. Hammons. Tidal power. *Proceedings of the IEEE*, 8(3):419–433, March 1993.
- J. Hansen, M. Sato, P. Kharecha, G. Russell, D. Lea, and M. Siddall. Climate change and trace gases. *Phil. Trans. Royal. Soc. A*, 365:1925–1954, 2007. doi: 10.1098/rsta.2007.2052. URL http://pubs.giss.nasa.gov/abstracts/2007/Hansen_etal_2.html.
- R. Hastings and M. Wall. Sustainable Solar Housing: Strategies And Solutions. Earthscan, 2006. ISBN 1844073254.
- J. Hatcher. The History of the British Coal Industry: Towards the Age of Coal: Before 1700 Vol 1. Clarendon Press, 1993.
- E. Heaton, T. Voigt, and S. Long. A quantitative review comparing the yields of two candidate C4 perennial biomass crops in relation to nitrogen, temperature, and water. *Biomass and Bioenergy*, 27: 21–30, 2004.
- D. Helm, R. Smale, and J. Phillips. Too good to be true? the UK's climate change record, 2007. URL http://www.dieterhelm.co.uk/publications/Carbon_record_2007.pdf.
- J. Herring. Uranium and thorium resource assessment. In C. J. Cleveland, editor, *Encyclopedia of Energy*. Boston University, Boston, USA, 2004. ISBN 0-12-176480-X.
- V. Hird, C. Emerson, E. Noble, J. Longfield, V. Williams, D. Goetz, R. Hoskins, A. Paxton, and G. Dupee. Still on the road to ruin? an assessment of the debate over the unnecessary transport of food, five years on from the food miles report, 1999.
- P. Hodgson. *Nuclear Power, Energy and the Environment*. Imperial College Press, 1999.
- J. J. Hopfield and J. Gollub. Introduction to solar energy, 1978. URL http://www.inference.phy.cam.ac.uk/sustainable/solar/HopfieldGollub78/scan.html.
- H. Horie, Y. Tanjo, T. Miyamoto, and Y. Koga. Development of a lithium-ion battery pack system for ev. *JSAE Review*, 18(3):295– 300, July 1997.
- HPTCJ. Heat pumps: Long awaited way out of the global warming, 2007. URL http://www.hptcj.or.jp/about_e/ contribution/index.html.
- A. Indermuhle, T. Stocker, F. Joos, H. Fischer, H. Smith, M. Wahlen, B. Deck, D. Mastroianni, J. Tschumi, T. Blunier, R. Meyer, and B. Stauffer. Holocene carbon-cycle dynamics based on CO₂ trapped in ice at Taylor Dome, Antarctica. *Nature*, 398:121–126, 1999.
- International Energy Agency. Things that go blip in the night standby power and how to limit it, 2001. URL http://www.iea.
 org/textbase/nppdf/free/2000/blipinthenight01.pdf.
- W. S. Jevons. The Coal Question; An Inquiry concerning the Progress of the Nation, and the Probable Exhaustion of our Coal-mines. Macmillan and Co., London, second edition, 1866. URL http://oll.libertyfund.org/.
- I. S. F. Jones. The production of additional marine protein by nitrogen nourishment, 2008. URL http://www.oceannourishment. com/files/Jc08.pdf.
- P. M. S. Jones. Statistics and nuclear energy. *The Statistician*, 33(1):91–102, March 1984. URL http://www.jstor.org/pss/2987717.

B. Judd, D. P. Harrison, and I. S. F. Jones. Engineering ocean nourishment. In World Congress on Engineering WCE 2008, pages 1315– 1319. IAENG, 2008. ISBN 978-988-98671-9-5.

- T. Kaneko, M. Shimada, S. Kujiraoka, and T. Kojima. Easy maintenance and environmentally-friendly train traction system. *Hitachi Review*, 53(1):15–19, 2004. URL http://www.hitachi.com/ICSFiles/afieldfile/2004/05/25/r2004_01_103.pdf.
- C. Keeling and T. Whorf. Atmospheric CO₂ records from sites in the SIO air sampling network. In *Trends: A Compendium of Data on Global Change*. Carbon Dioxide Information Analysis Center, Oak Ridge National Laboratory, US Department of Energy, Oak Ridge, Tenn., USA, 2005.
- D. W. Keith, M. Ha-Duong, and J. K. Stolaroff. Climate strategy with ${\rm CO_2}$ capture from the air, 2005.
- J. King. The King review of low-carbon cars. part ii: recommendations for action, 2008. URL hm-treasury.gov.uk/king.
- J. G. Koomey. Estimating total power consumption by servers in the U.S. and the world, February 2007. URL http://blogs.business2.com/greenwombat/files/ serverpowerusecomplete-v3.pdf.
- Z. Kowalik. Tide distribution and tapping into tidal energy. Oceanologia, 46(3):291–331, 2004.
- R. Kuehr. Computers and the Environment: Understanding and Managing their Impacts (Eco-Efficiency in Industry and Science). Springer, October 2003. ISBN 1402016808. URL http://www.amazon.co.uk/exec/obidos/ASIN/1402016808/citeulike-21.
- B. Lawson. Building materials, energy and the environment: Towards ecologically sustainable development, 1996.
- D. B. Layzell, J. Stephen, and S. M. Wood. Exploring the potential for biomass power in ontario, 2006. URL http://www.biocap.ca/ files/Ont_bioenergy_OPA_Feb23_final.pdf.
- C. Le Quéré, C. Rdenbeck, E. Buitenhuis, T. J. Conway, R. Langenfelds, A. Gomez, C. Labuschagne, M. Ramonet, T. Nakazawa, N. Metzl, N. Gillett, and M. Heimann. Saturation of the southern ocean CO₂ sink due to recent climate change. *Science*, 316: 1735–1738, 2007. doi: 10.1126/science.1136188. URL http://lgmacweb.env.uea.ac.uk/e415/publications.html.
- S. Lemofouet and A. Rufer. Hybrid energy systems based on compressed air and supercapacitors with maximum efficiency point tracking, 2005. URL http://leiwww.epfl.ch/ publications/lemofouet_rufer_epe_05.pdf.
- S. Lemofouet-Gatsi. Investigation and optimisation of hybrid electricity storage systems based on compressed air and supercapacitors. PhD thesis, EPFL, 2006. URL http://library.epfl.ch/theses/?nr=3628.
- B. Lomborg. The skeptical environmentalist: measuring the real state of the world. Cambridge Univ. Press, Cambridge, 2001. ISBN 0-521-80447-7.
- J. Lovelock. The Revenge of Gaia: Why the Earth Is Fighting Back and How We Can Still Save Humanity. Allen Lane, 2006. ISBN 0713999144.
- W. E. Mabee, S. J. N., C. Nielsen, L. Henrik, and E. Steen Jensen. Renewable-based fuels for transport, 2006.

- URL http://www.risoe.dk/rispubl/Energy-report5/ris-r-1557_49-52.pdf. Riso Energy Report 5.
- J. M. MacDonald. The economic organization of u.s. broiler production, June 2008. URL http://www.ers.usda.gov/ Publications/EIB38/EIB38.pdf. Economic Information Bulletin No. 38. Economic Research Service, U.S. Dept. of Agriculture.
- P. MacDonald, A. Stedman, and G. Symons. The UK geothermal hot dry rock r&d programme. In *Seventeenth Workshop on Geothermal Reservoir Engineering*, 1992.
- D. J. C. MacKay. Enhancing electrical supply by pumped storage in tidal lagoons, 2007a. URL http://www.inference.phy.cam. ac.uk/mackay/abstracts/Lagoons.html.
- D. J. C. MacKay. Under-estimation of the UK tidal resource, 2007b. URL http://www.inference.phy.cam.ac.uk/mackay/abstracts/TideEstimate.html.
- I. MacLeay, K. Harris, and C. Michaels. Digest of United Kingdom energy statistics 2007, 2007. URL www.berr.gov.uk.
- P. Malanima. Energy crisis and growth 1650–1850: the European deviation in a comparative perspective. *Journal of Global History*, 1: 101–121, 2006. doi: 10.1017/S1740022806000064.
- G. Marland, T. Boden, and R. J. Andres. Global, regional, and national CO₂ emissions. In *Trends: A Compendium of Data on Global Change*. Carbon Dioxide Information Analysis Center, Oak Ridge National Laboratory, U.S. Department of Energy, Oak Ridge, Tenn., USA, 2007. URL http://cdiac.ornl.gov/trends/emis/tre_glob.htm.
- Massachusetts Institute of Technology. The future of geothermal energy, 2006. URL http://geothermal.inel.gov/publications/future_of_geothermal_energy.pdf.
- J. P. McBride, R. E. Moore, J. P. Witherspoon, and R. E. Blanco. Radiological impact of airborne effluents of coal and nuclear plants. *Science*, 202(4372):1045–1050, December 1978. doi: 10.1126/science. 202.4372.1045.
- D. R. Mills and P. L. Lièvre. Competitive solar electricity, 2004. URL http://www.ausra.com/pdfs/Paper_CompetitiveSolarElectricity.pdf.
- D. R. Mills and R. G. Morgan. Solar thermal electricity as the primary replacement for coal and oil in u.s. generation and transportation, 2008. URL http://www.ausra.com/technology/reports.html
- D. R. Mills and G. L. Morrison. Compact Linear Fresnel Reflector solar thermal powerplants. *Solar Energy*, 68(3):263–283, March 2000. doi: 10.1016/S0038-092X(99)00068-7.
- D. R. Mills, P. Le Lièvre, and G. L. Morrison. First results from Compact Linear Fresnel Reflector installation, June 2004. URL http://solarheatpower.veritel.com.au/MILLS_CLFR_ANZSES_FINAL.pdf.
- P. Mindl. Hybrid drive super-capacitor energy storage calculation, 2003. URL http://www3.fs.cvut.cz/web/fileadmin/documents/12241-BOZEK/publikace/2003/Supcap6_EDPE.pdf.
- D. Mollison. Wave climate and the wave power resource. In D. Evans and A. de O. Falcao, editors, *Hydrodynamic of Ocean Wave-Energy*

- Utilization, pages 133-156, Berlin, 1986. Springer. URL http://www.ma.hw.ac.uk/~denis/wave.html.
- D. Mollison. The UK wave power resource. In Wave Energy (Institution of Mechanical Engineers Seminar), pages 1-6. John Wiley & Sons, 1991. URL http://www.ma.hw.ac.uk/~denis/wave.html
- D. Mollison, O. P. Buneman, and S. H. Salter. Wave power availability in the ne atlantic. *Nature*, 263(5574):223-226, 1976. URL http://www.ma.hw.ac.uk/~denis/wave.html.
- J. L. Monteith. Climate and the efficiency of crop production in Britain. Philos. Trans. R. Soc. London, 281:277–294, 1977.
- National Bureau of Economic Research. Nber macrohistory database, 2001. URL http://www.nber.org/databases/macrohistory/contents/.
- A. Neftel, H. Friedli, E. Moor, H. Ltscher, H. Oeschger, U. Siegenthaler, and B. Stauffer. Historical CO₂ record from the Siple station ice core. In *Trends: A Compendium of Data on Global Change*. Carbon Dioxide Information Analysis Center, Oak Ridge National Laboratory, U.S. Department of Energy, Oak Ridge, Tenn., USA, 1994. URL http://cdiac.ornl.gov/trends/co2/siple.htm.
- Netherlands Environmental Assessment Agency. History database of the global environment, 2006. URL http://www.mnp.nl/hyde/.
- C. L. Nickol. Silent aircraft initiative concept risk assessment, February 2008. URL http://ntrs.nasa.gov/archive/nasa/ casi.ntrs.nasa.gov/20080012497_2008011089.pdf.
- H. Norrström. Low waste technology in pulp and paper industries. Pure & Appl. Chem., 52:1999–2004, 1980. URL http://www.iupac.org/publications/pac/1980/pdf/5208x1999.pdf.
- W. J. Nuttall. Nuclear Renaissance. Institute of Physics Publishing, 2004.
- OECD Nuclear Energy Agency. Forty Years of Uranium Resources, Production and Demand in perspective. OECD Publishing, 2006. ISBN 9264028064. URL http://books.google.com/books?id=HIT10985uKYC.
- J. Ongena and G. Van Oost. Energy for future centuries. will fusion be an inexhaustible, safe and clean energy source?, 2006. URL http://www.fusie-energie.nl/artikelen/ongena.pdf.
- J. Oswald, M. Raine, and H. Ashraf-Ball. Will British weather provide reliable electricity? *Energy Policy*, in press, 2008. doi: 10.1016/j.enpol.2008.04.03.
- R. Price and J. Blaise. Nuclear fuel resources: Enough to last?, 2002. URL http://www.ingentaconnect.com/content/ oecd/16059581/2002/00000020/00000002/6802021e.
- R. Putt. Algae as a biodiesel feedstock: A feasibility assessment, 2007. URL www.eere.energy.gov/afdc/pdfs/algae.pdf.
- T. Rice and P. Owen. *Decommissioning the Brent Spar*. Taylor and Francis, 1999.
- B. S. Richards and M. E. Watt. Permanently dispelling a myth of photovoltaics via the adoption of a new net energy indicator. Renewable and Sustainable Energy Reviews, 11:162172, 2007. URL http://www.sciencedirect.com/science/journal/13640321.

- H. G. Richards, R. H. Parker, A. S. P. Green, R. H. Jones, J. D. M. Nicholls, D. A. C. Nicol, M. M. Randall, S. Richards, R. C. Stewart, and J. Willis-Richards. The performance and characteristics of the experimental hot dry rock geothermal reservoir at Rosemanowes, Cornwall (1985-1988). *Geothermics*, 23(2):73–109, 1994. ISSN 0375-6505.
- T. M. Ridley and D. T. Catling. Principles and practice of train performance applied to London Transport's Victoria line, 1966.
- T. M. Ridley and D. T. Catling. The energy implications of the design of mass transit railways, 1982. Presented at Tunnelling '82 (Third International Symposium), Brighton.
- H.-H. Rogner. Energy resources. In World Energy Assessment - Energy and the challenge of sustainability, chapter 5. UNDP, New York, USA, 2000. URL http://www.undp.org/energy/ activities/wea/draft-start.html.
- Royal Commission on Environmental Pollution. Biomass as a renewable energy source, 2004. URL www.rcep.org.uk.
- Royal Society working group on biofuels. Sustainable biofuels: prospects and challenges, January 2008. URL royalsociety. org. Policy document 01/08.
- C. Rubbia, J. Rubio, S. Buono1), F. Carminati, N. Fitier, J. Galvez, C. Gels, Y. Kadi, R. Klapisch, P. Mandrillon, J. Revol, and C. Roche. Conceptual design of a fast neutron operated high power energy amplifier. Technical Report CERN/AT/95-44 (ET), European Organization for Nuclear Research, 1995. URL http://doc.cern.ch//archive/electronic/other/generic/public/cer-0210391.pdf.
- C. J. Rydh and M. Karlström. Life cycle inventory of recycling portable nickel-cadmium batteries. Resources, Conservation and Recycling, 34:289-309, 2002. URL http://homepage.te.hik.se/ personal/tryca/battery/abstracts.htm.
- S. H. Salter. Possible under-estimation of the UK tidal resource, 2005. URL http://www.berr.gov.uk/files/file31313. pdf. Submission for DTI Energy Review Question 2.
- H. J. Schellnhuber, W. Cramer, N. Nakicenovic, T. Wigley, and G. Y. (Editors). Avoiding Dangerous Climate Change. Cambridge University Press, 2006. URL http://www.defra.gov.uk/environment/climatechange/internat/pdf/avoid-dangercc.pdf.
- Q. Schiermeier, J. Tollefson, T. Scully, A. Witze, and O. Morton. Energy alternatives: Electricity without carbon. *Nature*, 454:816–823, August 2008. doi: 10.1038/454816a.
- M. R. Schmer, K. P. Vogel, R. B. Mitchell, and R. K. Perrin. Net energy of cellulosic ethanol from switchgrass. *PNAS*, 105(2):464–469, 2008. doi: 10.1073/pnas.0704767105. URL http://www.pnas.org/cgi/content/full/105/2/464.
- N. Seko, A. Katakai, S. Hasegawa, M. Tamada, N. Kasai, H. Takeda, T. Sugo, and K. Saito. Aquaculture of uranium in seawater by a fabric-adsorbent submerged system. *Nuclear Technology*, 144(2): 274–278, November 2003.
- H. Shapouri, J. A. Duffield, and M. S. Graboski. Estimating the net energy balance of corn ethanol, 1995. URL http://www.

- ethanol-gec.org/corn_eth.htm. United States Department of Agriculture Agricultural Economic Report Number 721.
- T. L. Shaw and M. J. Watson. The effects of pumping on the energy potential of a tidal power barrage. *Engineering Sustainability*, 156(2):111–117, June 2003a. ISSN 1478-4637. doi: 10.1680/ensu.156.2.111.37018. URL http://www.atypon-link.com/TELF/doi/abs/10.1680/ensu.156.2.111.37018?cookieSet=1&journalCode=ensu.
- T. L. Shaw and M. J. Watson. Flexible power generation from a Severn barrage, April 2006. URL http://www.dti.gov.uk/files/ file31332.pdf.
- T. L. Shaw and M. J. Watson. Flexible power generation from the tides. *Engineering Sustainability*, 156(2):119–123, 2003b. ISSN 1478-4629.
- D. W. Shepherd. Energy studies, 2003.
- W. Shockley and H. J. Queisser. Detailed balance limit of efficiency of p-n junction solar cells. *Journal of Applied Physics*, 32(3):510–519, 1961
- W. Shyy, M. Berg, and D. Ljungqvist. Flapping and flexible wings for biological and micro air vehicles. *Progress in Aerospace Sciences*, 35 (5):455–505, July 1999.
- U. Siegenthaler, E. Monnin, K. Kawamura, R. Spahni, J. Schwander, B. Stauffer, T. Stocker, J.-M. Barnola, and H. Fischer. Supporting evidence from the EPICA Dronning Maud Land ice core for atmospheric CO₂ changes during the past millennium. *Tellus B*, 57(1):51–57, 2005. doi: 10.1111/j.1600-0889.2005. 00131.x. URL ftp://ftp.ncdc.noaa.gov/pub/data/paleo/icecore/antarctica/maud/edml-co2-2005.xls.
- R. Sims, R. Schock, A. Adegbululgbe, J. Fenhann, I. Konstantinaviciute, W. Moomaw, H. Nimir, B. Schlamadinger, J. Torres-Martnez, C. Turner, Y. Uchiyama, S. Vuori, N. Wamukonya, and X. Zhang. Energy supply. In B. Metz, O. Davidson, P. Bosch, R. Dave, and L. Meyer, editors, Climate Change 2007: Mitigation. Contribution of Working Group III to the Fourth Assessment Report of the Intergovernmental Panel on Climate Change. Cambridge University Press, Cambridge, 2007. URL http://www.ipcc.ch/pdf/assessment-report/ar4/wg3/ar4-wg3-chapter4.pdf.
- G. Sinden. Variability of UK marine resources, 2005. URL http://www.carbontrust.co.uk/NR/rdonlyres/ EC293061-611D-4BC8-A75C-9F84138184D3/0/ variability_uk_marine_energy_resources.pdf.
- J. F. A. Sleath. Sea bed mechanics. Wiley, New York, 1984. ISBN 047189091X.
- R. Socolow. Stabilization wedges: An elaboration of the concept. In H. J. Schellnhuber, W. Cramer, N. Nakicenovic, T. Wigley, and G. Yohe, editors, Avoiding Dangerous Climate Change. Cambridge University Press, 2006. URL http://www.defra.gov.uk/environment/climatechange/internat/pdf/avoid-dangercc.pdf.
- M. Steinberg and V. Dang. Preliminary design and analysis of a process for the extraction of lithium from seawater. Technical Report 20535-R, Brookhaven National Lab., Upton, N.Y. (USA), 1975. URL http://www.osti.gov/energycitations/product.

- biblio.jsp?osti_id=7351225. Presented at Symposium on United States lithium resources and requirements by the year 2000; 22 Jan 1976; Lakewood, CO, USA.
- Subcommittee on Poultry Nutrition, National Research Council. *Nutrient Requirements of Poultry*. National Academy Press, Washington, ninth revised edition edition, 1994. URL http://www.nap.edu/openbook.php?isbn=0309048923.
- B. Supple. The history of the British coal industry. Vol. 4, 1913–1946: the political economy of decline. Clarendon, Oxford, 1987. ISBN 019828294X.
- B. D. T. and R. S. C. A two-basin tidal power scheme for the Severn estuary. In *Conference on new approaches to tidal power*, 1982.
- G. I. Taylor. Tidal friction in the Irish Sea. R. Soc. Lond. Ser. A, 220:1-33, 1920. doi: 10.1098/rsta.1920.0001. URL http://journals.royalsociety.org/content/lkq652823817/?p=072ed2c7a8674c119854d0c0a703eedf&pi=13.
- S. J. Taylor. The Severn barrage definition study for a new appraisal of the project, 2002. URL http://www.dti.gov.uk/files/file15363.pdf. ETSU REPORT NO. T/09/00212/00/REP.
- H. Tennekes. The Simple Science of Flight. MIT Press, 1997.
- The Earthworks Group. 50 Simple things you can do to save the earth.

 The Earthworks Press, Berkeley, California, 1989. ISBN 0-929634-06-3.
- G. J. Treloar, P. E. D. Love, and R. H. Crawford. Hybrid life-cycle inventory for road construction and use. *J. Constr. Engrg. and Mgmt.*, 130(1):43–49, 2004.
- F. Trieb and G. Knies. A renewable energy and development partnership EU-ME-NA for large scale solar thermal power and desalination in the Middle East and in North Africa, 2004. URL http://www.gezen.nl/wordpress/wp-content/uploads/2006/09/sanaa-paper-and-annex_15-04-2004.pdf.
- T. Tsuruta. Removal and recovery of lithium using various microorganisms. Journal of Bioscience and Bioengineering, 100(5):562–566, 2005. URL http://www.jstage.jst.go.jp/article/jbb/100/5/100-562/_article.
- W. C. Turkenburg. Renewable energy technologies. In World Energy Assessment Energy and the challenge of sustainability, chapter 7. UNDP, New York, USA, 2000. URL http://www.undp.org/energy/activities/wea/draft-start.html.
- A. Ucuncu. Energy recovery from mixed paper waste, 1993. URL http://www.p2pays.org/ref/11/10059.pdf.
- G. van den Berg. Effects of the wind profile at night on wind turbine sound. *Journal of Sound and Vibration*, 277:955–970, November 2004. URL http://www.nowap.co.uk/docs/windnoise.pdf.
- E. d. M. van Voorthuysen. Two scenarios for a solar world economy. *Int. J. Global Environmental Issues*, 8(3):233247, 2008.
- Water UK. Towards sustainability 2005-2006, 2006. URL http://www.water.org.uk/home/policy/reports/sustainability/indicators-2005-06/towards-sustainability-2005-2006.pdf.
- J. Watson, J. Hertin, T. Randall, and C. Gough. Renewable energy and combined heat and power resources in the UK, April

2002. URL http://www.tyndall.ac.uk/publications/working_papers/wp22.pdf. Tyndall Centre for Climate Change Research Working Paper 22.

- Wavegen. Islay Limpet project monitoring final report, 2002. URL http://www.wavegen.co.uk/pdf/art.1707.pdf.
- C. L. Weber and H. S. Matthews. Food-miles and the relative climate impacts of food choices in the united states. *Environ. Sci. Technol.*, 42(10):3508–3513, 2008. doi: 10.1021/es702969f.
- M. Weightman. Report of the investigation into the leak of dissolver product liquor at the Thermal Oxide Reprocessing Plant (THORP), Sellafield, notified to HSE on 20 april 2005, Feb. 2007. URL http://www.hse.gov.uk/nuclear/thorpreport.pdf.
- J. C. Wheatley, G. W. Swift, and A. Migliori. The natural heat engine. Los Alamos Science, Fall 1986, 1986.
- T. Wiedmann, R. Wood, M. Lenzen, J. Minx, D. Guan, and J. Barrett. Development of an embedded carbon emissions indicator producing a time series of input-output tables and embedded carbon dioxide emissions for the UK by using a MRIO data optimisation system, 2008. URL http://randd.defra.gov.uk/Document.aspx?Document=EV02033_7331_FRP.pdf.
- R. H. Williams. Advanced energy supply technologies. In World Energy Assessment — Energy and the challenge of sustainability, chapter 8. UNDP, New York, USA, 2000. URL http://www.undp. org/energy/activities/wea/draft-start.html.
- E. M. Wilson and M. Balls. Tidal power generation. In P. Novak,

- editor, Developments in Hydraulic Engineering, chapter 2. Taylor & Francis, 1990. ISBN 185166095X.
- B. Wood. Economic district heating from existing turbines. *Institution of Civil Engineers Proceedings pt. 1, 77:27–48, February 1985.*
- World Energy Council. Comparison of energy systems using life cycle assessment, July 2004. URL http://www.worldenergy.org/publications/313.asp.
- E. Worrell, L. Price, N. Martin, C. Hendriks, and L. O. Meida. Carbon dioxide emissions from the global cement industry. Annual Review of Energy and the Environment, 26: 303-329, November 2001. doi: 10.1146/annurev.energy.26.1. 303. URL http://arjournals.annualreviews.org/doi/abs/10.1146/annurev.energy.26.1.303.
- B. Yaros. Life-cycle thinking for wood and paper products. In National Research Council, editor, Wood in Our Future: The Role of Life-Cycle Analysis: Proceedings of a Symposium. National Academy Press, 1997. ISBN 0309057450. URL http://books.nap.edu/openbook.php?record_id=5734.
- C. P. Zaleski. The future of nuclear power in France, the EU and the world for the next quarter-century, February 2005. URL http://www.npec-web.org/Essays/ Essay050120Zalenski-FutureofNuclearPower.pdf. http://tinyurl.com/32louu.
- X.-G. Zhu, S. P. Long, and D. R. Ort. What is the maximum efficiency with which photosynthesis can convert solar energy into biomass? *Current Opinion in Biotechnology*, 19:153159, 2008.

	41 004	1 1
λ, 325	Alps, 224	bathymetry, 65
g, 325	altitude, 292	battery, 95, 145, 220
pumped storage, 204	altruism, 5	efficiency, 217
x CO ₂ -equivalent, 11	aluminium, 94, 103, 348	energy density, 214, 280
wind-farm	can, 94	lithium-sulphur, 217
Whitelee, 35	carbon footprint, 100	nickel-cadmium, 95
13 amps, 54	embodied energy, 100	rechargeable, 100
	always on, 103	battery charging, 212
747, 140	America, 21, 99, 190	battery exchange, 280
787, 236	American, 111, 263	Bavaria, 43, 51, 232
1698, 6, 19	Amonix, 197	BBC, 72, 75
1769, 6	amplifier, 74	beach, 325
1910, 7	amps, 54	Beatrice, 68, 70
1979, 21	analogy, 26	Bedford, 59
2050, 218	Andasol, 190	beef, 81
	answering machine, 74	Belgium, 21
A380, 140	Aptera, 145	Berlingo, 135
AA battery, 95	Aquamarine Power Ltd, 328	Betz, Albert, 283
academics, 312	area, 59, 381	bicycle, 127, 276, 283
accelerator-driven system, 175	frontal, 128	billiard ball, 85
action, 218	area per person, 34	billion, 11, 233, 380
addiction, 218	Arizona, 48, 197, 263	biodiesel, 220
Adelman, Kenneth, 42	arms	from algae, 47
advertisement, 256, 319	exports, 240	bioethanol, 220
advertising standards authority, 134	manufacture, 240	biofuel, 82
advocating acts of consumption, 4	Artemis Intelligent Power, 133	production, 220
aerodynamic efficiency, 293	Atkinson cycle, 144	biomass, 40
Afghanistan, 240	Atlantic, 77, 327, 330	cofiring, 227
agricultural waste, 221	Atlantic ocean	plantation, 227
air	tides, 85	yields, 45
energy consumption, 97	waves, 78	biomethanol, 220
hot, 55	atmosphere, 10	bird, 289
air resistance, 126	Atoms for Peace, 141	formation flying, 290, 298
air transport, 236	Australia, 190	longest flight, 297
air travel	automobile, 126	range, 296
neutralization, 226	average	speed, 292
air-conditioner, 159	travel, 32	theory of, 289
air-conditioning, 56	average windspeeds, 34	birds and windmills, 67
in vehicles, 140		Birmingham, 221
air-source heat pump, 56, 159, 220, 227	b, 380	Blair, Tony, 227, 244, 247
Airbus, 140	B&Q, 70	block, 348
aircraft, 140	background radiation, 181	BMW, 31
turboprop, 37	Bad Thing, 10	Hydrogen 7, 138, 147
aircraft carriers, 240	BAE Systems, 240	bn, 380
Al Yamamah, 240	Baer, 15	boat, see ship, see ship
albatross, 292	bag of crisps, 84	energy consumption, 97
albedo flip, 357	bailing the Titanic, 72	nuclear-powered, 141
Albert Hall, 364	bailing the Titanic with a teaspoon, 73	boats
alchemy, 93	Bangladesh, 190	as planes, 299
algae, 46, 48, 53	bar fire, 55	Boeing, 236
Algeria, 190	bar-tailed godwit, 297	Boltzmann, 292
alkaline battery	Barbados, 247	bomb, 108
energy density, 214	bath, 54	Bombardier Q400, 37
==-		

boundary, 32	Canada, 21	chicken, 81
BP, 3, 28, 237	capacity, 35, 67, 285	chicken feed, 81
brakes, 273	capacity factor, 35, 285, 288	China, 5, 21, 341
braking	capitalization, 360	CHP, 152
regenerative, 133	car, 31, 126, 273	Citroën Berlingo, 135
breeder reactor, 172, 173	eco-car, 127	civilization, 54
brick, 348	electric, 134	clay, 348
Brinkley, Mark, 70	embodied energy, 100	clean coal, 218, 227
Bristol channel, 89	fish, 145	cliff, 10
Britain, 21, 99	hybrid, 134	climate change, 5, 10
electricity demand, 201, 203, 376	lights, 61	greater threat than terrorism, 4
heights, 59	carbohydrate, 45	is about energy, 5
rainfall, 59, 60	carbon capture, 227	climate modelling, 10
British Isles, 87	carbon dioxide, 20	climate-change inactivists, 9
British person, 32	climate change, 5	clock-radio, 74
BritNed, 212	data, 6, 8	clothes-dryer, 55
Brooklyn windmill, 284	equivalent, 11	clothes-washing, 54
Brown, Gordon, 22	greenhouse effect, 5	cloud cover, 40
BTU, 363	carbon footprint	clutter, 93
bulb, 62	aluminium, 100	coal, 9, 100, 221, 306
incandescent, 62	carbon neutralization, 226	British resource, 6
LED, 62	carbon price, 226	calorific value, 214
low-energy, 62	carbon sequestration	clean, 218, 227
bus	by cofiring biomass, 226	energy density, 214
electric, 128	carbon trading, 236	UK, 167
Bush, George W., 44	carbon-dioxide emissions	coal mine
butter, 31, 33	electric car, 139	open-cast, 169
calorific value, 31	cardboard, 306	coal mines, 223
caronne varue, 51	Cardiff, 89	coal power station, 5, 167
C3 plants, 53		coal power stations, 361
	cargo vessel	<u>*</u>
C5, 70, 135	nuclear-powered, 141	coal production, 6
cable modem, 72	carnivore, 81	coal substitution, 44
California 107	cartoon, 218	coastline, 69, 78
California, 197	bicycle, 277	coefficient of performance, 162, 316
calm weather, 201	car, 272	cofiring, 227
Calories, 80	flight, 290	cofiring biomass, 226
calorific value, 31, 33, 45, 229, 306	train, 279	cogeneration, 152
butter, 31	wind power, 282	coke, 94, 100
coal, 214	windmill, 283	Colorado, 48
DERV, 214	cartoon Britain, 124, 219	combustion, 33
diesel, 214	cartoon of flight, 292	commuting
ethanol, 214	cartoon-Britain, 124	data, 147
firewood, 214	2008, 124	compact linear fresnel reflector, 199
fuel, 31, 214	cassette-player, 74	computer, 72, 73, 95
gross, 33	cats, 67, 82	concentrating solar power, 42, 191, 199
hydrogen, 214	cavity-wall insulation, 150	parabolic trough, 190
kerosene, 214	cellulosic bioethanol, 220	concentrator photovoltaics, 197
methanol, 214	Celsius, 308, 360	concrete, 348
net, 33	cement, 348	condensation, 315
propane, 214	ceramics, 93	confusion
wood, 306	Chancellor, 3	power and efficiency, 49
Caltech, 2	channel tunnel, 241	power and energy, 25
Cambridge, 48, 56, 96	charger, 72, 73, 256	congestion, 132, 236
Cameron	charging	congestion charging, 143
David, 285	electric vehicle, 212	conservation of energy, 27
can	cheese, 80	Conservative Party, 122
aluminium, 94	chemical energy, 28, 33	consumption, 23

European, 111	electric car, 135	diversity, 222
container, 96, 381	emissions of cars, 144	DIY planet repairs, 256, 319
continent, 103	energy consumption, 112, 113	do your bit, 3
continental Europe, 152, 380	freight, 97	dog, 82
continental shelf, 86	G-Wiz, 135	door, 312
continental shelves, 357	gas demand, 216	double decker bus, 364
contraction and convergence, 15	GDP, 112, 113	double glazing, 312
convective heat loss rate, 309	height, 59	double-decker bus, 3
conventions, 328	incineration, 222	Dover, 330
cooker, 54, 55	land use, 190	drag, 126
cooking, 54, 222	landfill, 222	drag coefficient, 145, 272–274
cooling tower, 152	nuclear power by country, 170	drag-to-lift ratio, 293
copper, 348	offshore wind, 68	Drax, 361
cordless phone, 73	oil price, 5	drinks can, 94
Coriolis force, 86	oil production, 5–8	driving, 83
cornish pasties, 96	population, 8, 190	duck
Cornwall, 96	power station closures, 5	Salter, 327
Coronation Street, 212	pumped storage, 217	duvet, 10
cost, 233	recycling, 222	DVD player, 73
arms, 240	sea depths, 65	Dynamic Demand, 217
offshore wind, 70	sunniness, 40, 48	dynamic demand, 211
counter-current heat exchange, 318	waste, 222	
countries, 17, 112, 113	water depths, 65	e500, 145
civilized, 54	wind	eagle, 67
countryside, 224	Ireland, 202	earth, 10, 85, 348
cow, 80, 81, 83	wind power fluctuations, 203	area, 381
CPV, see concentrator photovoltaics, see	decommissioning, 236	easily turn-off-and-onable, 201
concentrator photovoltaics	deep offshore wind, 64, 70	EastEnders, 212
crisps, 84	definition	Eco Cute, 162
crock of manure, 9	sustainable, 167	eco-boat, 138
Croesor, 207	degree-day, 310, 311	Eco-Bollocks award, 70
CRT (cathode ray tube), 74	deliberate inaccuracy, 16	eco-car, 127
Cruachan, 206	delivery vehicle	economic costs, 24
crude oil, 19, 221	electric, 146	economics, 70, 218, 226
production, 5	demand	of wind, 36
cruise-ship, 93	electricity, 201, 203, 376	economies of scale, 36
crust, 103	demand management, 204, 211	economist, 2
CSP, see concentrating solar power, see	Denmark, 35, 36, 67, 212	economy, 31
concentrating solar power	density, 33, 282	EdF, 5, 376
current, 88	Department of Defense, 109	efficiency, 123, 206, 217
Curtis, Jamie Lee, 138	depths, 65	confused with power, 49
CUTE, 138	DERV	improvements, 44
cyclist, 283	calorific value, 214	more-efficient planes, 39
Czech Republic, 21	energy density, 214	of incineration, 46
,	desalination, 98	of plants, 53
dairy, 80, 83	desert, 191	of solar panels, 49
dam, 59	deuterium fusion, 182	scope for improvement, 23
damp, 315	Diamond, Jared, 190	efficiency legislation, 161
Darth Vader, 72	diesel, 33	Eggborough, 361
data	calorific value, 214	Einstein, 296
x CO ₂ concentrations, 6, 8	energy density, 214	Eisenhower, D.D., 107, 141
area, 190	digital hydraulics, 133	electric bus, 128
bathymetry, 65	digital radio, 74	electric car
coal production, 6–8	Dinorwig, 60, 206–208, 341, 360	\times CO ₂ emissions, 139
commuting, 147	direct normal irradiance, 194	data, 135
countries, 190	dishwashing, 54, 55	range, 279, 280
depths, 65	district heating, 152	theory, 280

electric fan heater, 55	ethanol, 214	fetch, 77, 329
electric tram, 147	firewood, 214	Fetish, 145
electric vehicle, 212, 221	fuel, 31, 214	Ffestiniog, 205, 206
battery cost, 139	hydrogen, 214	fibreglass, 348
in cold places, 140	kerosene, 214	Fido, 82
in hot places, 139	lead-acid battery, 214	filling station
lifetime, 139	lithium-ion battery, 214	role in electric transport, 280
electric vehicles, 204	methanol, 214	finesse, 293
electrical energy, 28	of waves, 329	finger millet, 53
electricity, 54, 73, 218	propane, 214	fire
demand management, 211	energy efficiency, 62	electric, 55
demand varies, 201	energy gap, 5, 376	firewood
greening of, 139	energy intensity, 123	calorific value, 214
grid, 212	energy waste league, 72	energy density, 214
hydroelectric, 59	energy yield ratio, 43, 44	Fischer
mains, 211	solar PV, 44	Joschka, 190
supply, 54, 139, 219, 376	wind, 44	fish, 145
'energy gap', 5	engineer, 33	flight
electrification	England	boats that fly, 299
of heating, 220	rainfall, 59	emissions, 16
of transport, 220	England-France	formation, 290
Elettrica, 135	interconnector, 198	optimal speed, 292
embedded, 94	entertainment system, 73	optimum height, 297
embodied, 94	entropy, 27, 28	flight record, 297
embodied energy	environmental costs of renewables, 24	flood defences, 239
aluminium, 100	equator, 40	Florø, 91, 332
car, 100	estimation, 283	flow, 26, 88
glass, 100	Estonia, 21	fluctuations, 201, 220, 225
paper, 101	ethanol	fluorescent bulb, 62
PET, 100	calorific value, 214	flux
plastic, 102	energy density, 214	sunlight, 40
steel, 100	Etheridge, D. M., 20	flying, 226
water, 101	ethical assertions, 17	emissions, 16
emissions	ethics, 11	flying wing, 298
flight, 16	breeder reactor, 172	flywheel, 213
flying, 16	pollution, 14	fog, 10
travel, 16	Europe, 45, 111, 115, 190, 222	food, 40
emissions trading, 233	continental, 152, 154, 380	waste, 237
enemy of the people, 4	European Union, 239	food miles, 96
energy, 25	EV1, 145	football field, 365
chemical, 33	Evans, R. Keith, 147	footprint, 147
conservation, 27	every little helps, 3, 62, 72	foreigners, 5
contrasted with power, 25	evil, 72	forest, 220
geothermal, 103	exa, 365	formation flying, 290, 298
kinetic, 29	exchange rate, 28	formula
low-grade, 41	Exxon, 237	kinetic energy, 32
of vaporization, 33		wave, 325
spending, 233	factory, 93	Formula One, 236
wave, 325	factual assertions, 17	Fossett, Steve, 297
energy amplifier, 175	Fair Isle, 212	fossil fuel, 218
energy demand	fallacy	backup for wind, 202
variations, 201, 216	Limits to Growth, 185	fossil fuels, 5
energy density, 31, 306	fast breeder reactor, 172	peaking of, 5
butter, 31	fast breeder reactors, 171	Foyers, 206
coal, 214	fat is 6000 metres per second, 296	fractal, 69
DERV, 214	faucet, 26	France, 21, 181
diesel, 214	fertilizer, 45, 82, 84	freezer, 54

freight, 141	gnuplot, 270	high heat value, 33
energy consumption, 97	godwit, 297	highlands, 59
fridge-freezer, 54, 73	good-against-evil, 107	rainfall, 59
Friends of the Earth, 19	goods, 93	history, 115
frontal area, 128, 273	Goodstein, David, 2	hockey stick graph, 20
fuel	government, 239	Holland, 359
calorific value, 31, 214	gown, 312	home, 361
energy density, 31, 214	granite, 318, 322, 323, 348	Honda, 33, 147
fuel cell bus, 138	grass, 44	FCX Clarity, 138
fuel efficiency	grazing, 82	fuel-cell car, 138
of heavy goods vehicle, 96	Great Yarmouth, 288	hoop, 282
plane, 38	green algae, 48, 53	Horns Reef, 65, 69
fully developed sea, 329	Green Party, 225	horse, 82
fusion, 241	greenhouse effect, 5, 10	horsepower, 27
,	greenhouse gas, 10	hot air, 55
G-Wiz, 134, 135	greening electricity supply, 139	hot dry rock, 104
data, 135	Greenland icecap, 10	hot water, 28, 54
gadget, 73	Greenpeace, 4, 19, 170, 225	hours of sunshine, 48
Gaia, 2	Gretar Ívarsson, 103	house, 313
gallium arsenide, 42	gross calorific value, 33	Housebuilder's Bible, 70
galvanised steel, 348	ground-source heat pump, 220	household waste incineration, 45
gas, 221	guerrilla physics, 33	Hull, 330
landfill, 304	GW, 27	Hummer, 137
methane, 304	gypsum, 348	HVDC, 193, see high voltage DC, see
•	gypsum, 540	high voltage DC
national demand, 216	hair driver 02	hybrid car, 134
gas charges, 255	hair-dryer, 93	hybrid cars
gas mantle, 175	Haishan, 341, 343	
gas pipeline, 66	hardboard, 348	compared, 134
gasoline, 33	hardwood, 306, 348	misleading advertising, 134
GDP, 112, 113	hate, 4	hydraulics
geese, 298	Hawaii, 6, 8	digital, 133
General Motors, 145	health, 239	hydrocarbon, 31, 33
genetic engineering, 46	heat, 10	hydrodynamically underprivileged
genetic modification, 45, 48, 52, 53	waste, 152	area, 327
geothermal, 103	heat capacity, 54, 318	hydroelectricity, 59, 221
geothermal energy, 103	heat exchanger, 318	hydrofoil, 300
geothermal mining, 103	heat flux, 104	hydrogen, 48, 137, 138
geothermal power, 28, 103	heat loss parameter, 320	calorific value, 214
Germany, 21, 35	heat pump, 28, 56, 154, 220	energy cost of, 147
giga, 365	air source, 159	energy density, 214
gigaton, 355	heat pumps	for fusion, 183
gigawatt, 27, 203	winter, 161	from algae, 48
gigawatt-hour, 27	heat-loss coefficient, 148, 149	from bacteria, 44
giggle, 27	heat-loss parameter, 313, 314	plane, 297
Glasgow, 35, 60	Heathrow Airport, 236	production by nuclear power, 186
glass, 93, 348	heating, 218	storage efficiency, 211
embodied energy, 100	under-floor, 159	hydrogen car, 147
glasswool, 348	Heaton, Emily, 45	hydrogen fuel initiative, 236
glazing, 312	heavy goods vehicle, 96	
Glendoe, 60	hectare, 365	i MiEV, 144
glide number, 293	height	ice cores, 6, 8
glide ratio, 293	of flight, 297	ice-breaker, 141
global warming, 10	heights, 59	Iceland, 103, 106
GlobalFlyer, 297	Heliodynamics, 42, 52	imported power, 221
glorification of travel, 4	Helston, 96	imports
GM EV1, 145	Herne Bay, 64	energy, 224, 226
gmt, 270	HEU, 108	imprecision, deliberate, 16

inaccuracy deliberate 16	Keeling, C. D., 20	lighthulb 62
inaccuracy, deliberate, 16	0, ,	lightbulb, 62
inactivist, 9	keeping the lights on, 72	incandescent, 62
incineration	kelvin, 308	LED, 62
efficiency, 46	Ken, 256, 319	low-energy, 62
waste, 45	Kentish Flats, 64, 68, 71	lights
Independent, 9, 20, 70	kerosene	on cars, 61
Indermuhle, A., 20	calorific value, 214	Limits to Growth, 185
India, 21, 175	energy density, 214	Limpet, 79
Industrial Revolution, 6, 8	kettle, 54	LiPo, 275
information systems, 72	kilo, 365	liquid salt
infrared, 10	kilowatt, 54	energy storage, 190
insulation, 220, 315	kilowatt-hour, 25	litany, 10, 21
insurance, 233	kilowatt-hour per day, 25	lithium, 147, 183, 187
	1 2	
interconnector	kinetic energy, 29, 273, 282, 325	lithium fusion, 182
England–France, 198	kinetic energy storage, 213	lithium-ion, 145
intercontinental flight	king coal, 9	lithium-ion battery
emissions, 16	Kinlochewe, 59, 60	efficiency, 217
intermittency, 66	knot, 88	energy density, 214
internet, 21		lithium-ion polymer battery
investment, 233	la Rance, 91	energy density, 214
IPCC, 38, 179	Labour, 19	lithium-sulphur, 217
Iraq war, 240	laminar flow control, 294, 298	Llyn Stwlan, 205
Ireland, 77, 91, 202, 216, 217, 332	laminated wood, 348	load factor, 35, 68, 69, 285, 288
wind output, 202	landfill, 45, 93, 101, 222	Loch Lomond, 208
irresponsible journalism, 9	landfill gas, 304	Loch Sloy, 208
irrigation, 45	Y	logarithmic scale, 7, 8
	landlord, 249	Lomborg, Bjørn, 2
Isaac Asimov, 123	Langeled, 66, 67, 239	
island	laptop computer, 74	London, 221, 236, 256, 319
nuclear, 186	Larry, 249	London Array, 70
Islay, 79	laser-printer, 73, 74	Los Angeles, 3
Isles of Scilly, 87	laundry, 54	love, 4
ITER, 241	laws of physics	Lovelock, James, 2
	conservation of energy, 27	low heat value, 33
J-Power, 209	Lawson, Dominic, 9, 20	low-enriched uranium, 108
jack-up barge, 67, 223, 232	layer (chicken), 81	low-grade energy, 41
jack-up barges, 67, 71	LCA, see lifecycle analysis, see lifecycle	low-grade heat, 104
Japan, 21, 152, 159, 184, 190	analysis	lowlands, 59
efficiency legislation, 161	LCD (liquid crystal display), 74	rainfall, 59
Jersey Police, 145	lead, 349	LPG, 100
Jersey Water, 98	lead-acid battery	lumber, 348
	and the second s	lumens per watt, 62
JET, 213	efficiency, 217	-
jet fuel, 33	energy density, 214	lunar energy, 86
jet travel, 226	leadership, 248	Luxembourg, 21
emissions, 16	leakiness, 149, 310, 312, 313	
jet-ski, 138	Learjet, 295	m, 380
Jevons, William Stanley, 20, 167, 168,	LED, 62, 220	Mühlhausen, 43, 51, 232
201	lego, 93	magma, 105
joule, 26, 80, 360	LEU, 108	Magnus platform, 67
journalism	Lexus, 134	mains electricity, 211
bad, 9	misleading advertising, 134	maize, 53
journalist, 147	Liberal Democrats, 225, 229	makeup, 239
junk mail, 4	Libya, 190	Malin Head, 332
Jutland, 69	life cycle analysis, 139	manufacturing, 72, 139
januara, 07		manure, 9
Vog 145	life-cycle	•
Kaz, 145	of stuff, 93	map, 10
Kazakhstan, 190	life-cycle analysis, 93	Maplin, 72
kcal, 80	lift-to-drag ratio, 293, 298	Marchetti, C., 186

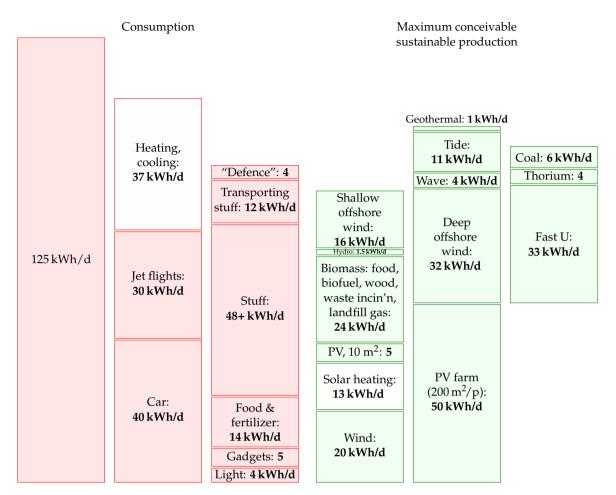
		•
margarine, 31	motorway, 236	data
Mastrandrea, 15	Mrd, 380	power by country, 170
Mayor of London, 256, 319	mSv, 181	decommissioning, 236
Mazda, 140	Mt, 380	hydrogen production, 186
McCarthy, Donnachadh, 70	Mtoe, 380	reactor
McMahon, Richard, 76	multinational chemicals, 94	breeder, 172
McNuggets, 44	multiple-junction photovoltaics, 51	energy amplifier, 175
MDF, 348	municipal solid waste, 222, 306	fusion, 182
meat, 81	mutton, 82	once-through, 171
meat-eating	MyCar, 145	weapon
argument for, 82	myth	testing, 241
		9
mega, 365	food, 83	weapons, 107
Mega City, 145	hydroelectricity, 60	nuclear decommissioning, 236
megaton, 108	nuclear power build rate, 181	nuclear decommissioning authority,
mercury, 62	solar panels, 49	176, 186
metal, 93	walking, 83	nuclear power, 2, 4, 19, 72, 221
metapost, 270		costs, 173, 176
methane, 45, 221, 304	Nant-y-Moch, 59	decommissioning, 173
methane hydrates, 357	National Academy of Sciences, 20	inflexibility, 201
methanol, 224	national gas demand, 216	station, 171
calorific value, 214	National Renewable Energy Laboratory,	area, 176
energy density, 214	48	build rate, 181
metre, 360	natural gas, 221, 304	construction, 179
Mexican wave, 325	demand varies, 216	fuel required, 173
microturbine, 67	national demand, 216	nuclear power stations, 5
microwave, 54, 55	Nature, 146	nuclear reactor
microwave oven, 54		fast breeder, 172
	Nature magazine, 137	
Middle Ages, 115	neap tide, 85, 89	nuclear stockpile, 241
middlehen, 82	Neftel, A., 20	numbers, 4
middlesow, 82	net calorific value, 33	07 161 100
migration, 298	New Jersey, 263	O'Leary, Michael, 38
military, 240	New Mexico, 197	ocean, 85
aid, 240	New Scientist, 4, 19	uranium extraction, 173
milk, 80	New Zealand, 283, 284	ocean conveyor belt, 171
milliard, 380	newspaper, 95, 99, 101, 304, 306	ocean liners, 140
million, 380	newsprint, 101	Ocean Power Delivery, 327
millisievert, 181	newton, 360	offshore, 288
millpond, 78	nickel, 349	offshore wind, 64
mine, 201	nickel cadmium battery	cost, 70
mini-SUV, 145	energy density, 214	data, 68
mining	nickel metal hydride battery	deep, 64
geothermal, 103	energy density, 214	jack-up barges, 67, 223, 232
Mio, 380	nickel-cadmium, 100	shallow, 64
mirror, 42	nickel-cadmium battery, 95	oil, 221
miscanthus, 45, 220	NIMBY, 224	North Sea, 5
misleading advertising, 134	nitrogen, 292	price, 5
MIT, 104, 105	nitrous oxides, 38	oil field, 68
mobile-phone charger, 72, 256	nomenclature, 360	oil platform, 68
Modec, 146	North Hoyle, 68, 288	oil power stations, 5
modem, 72	North Sea, 77, 87	oilrig, 64
molten salt, 190	oil, 5	oilspinner, 10
monazite, 175	Northern Ireland, 91	Okinawa, 209
moon, 85, 86, 103	Norway, 67, 144, 239, 332	Olympics, 237
Moore, Patrick, 170	nose, 318	once-through, 171
mortar board, 312	nostril, 318	open-cast coal, 169
motivations, 5	NS Savannah, 141	orange, 103
motorcycle, 10	nuclear, 226	Orkney, 86, 288

Otto cycle, 144	plan N, 224	pronunciation, 27
Out of Gas, 2	plane, 37	propane
outlet, 54	efficiency improvements, 39	calorific value, 214
oven, 54, 55	turboprop, 37	energy density, 214
oxygen, 292		0,
	planes	public transport, 220
Oxygen Cargo, 146	boats as an example of, 299	pumped storage, 205–207, 225
Oyster, 328	planet, 10	efficiency, 206, 217
ozone, 38	destruction, 72	PVC, 348
	planet Dorkon, 31	
p-km, 126	plant	Qatar, 21
packaging, 93	yields, 45	quad, 363
paddling pool, 86	plants	quartz, 318
paint, 348	C3, 53	± .
paper, 3, 94, 95, 101, 306, 344	C4, 52	Queen's University Belfast, 328
embodied energy, 101	more efficient, 53	
parabolic trough, 190	plaster, 348	racing, 236
particleboard, 348	plasterboard, 348	radiator, 55
passenger-kilometre, 126	plastic, 93, 348, 349	radio, 74
pasties, 96	embodied energy, 102	radioactive decay, 103
patio heater, 56	plywood, 348	rail
peak, 285	politics, 218	energy consumption, 97
peak nuclear, 2	polluter pays, 14	
peak oil, 2, 5, 20	pollution, 62, 93, 239	rail investment, 236
peak power, 67	pool, 86	railway, 236
pedant, 33, 69	•	rainfall, 59
-	population	Rance, 91
pee, 98	population	ranch, 44
Pelamis, 78, 223, 327	growth, 123	range, of bird, 296
perfume, 239	population density, 35, 190, 227	Rapley, Chris, 123
period, 325	population growth, 7, 8	Rau, Nick, 19
PET	population reduction, 4, 123	RAV4, 144
embodied energy, 100	pork, 81	reactive power, 76
peta, 365	Porritt, Jonathan, 2	reactor
petagram, 355	positive feedback, 357	breeder, 172
petrol, 33	potential energy, 325	fast breeder, 172
petrol engine, 144	power, 25	rechargeable battery, 95, 100
petroleum substitution, 44	confused with efficiency, 49	, e
philanthropy, 237	definition, 25	record
Phoenix SUT, 145	of sunshine, 40	flight, 297
phone, 72	power density	recycling, 93
phone charger, 4, 72	offshore wind, 64	data, 222
photosynthesis, 45, 48	wind, 283	refrigeration, 28
efficiency, 52	wind farm, 34	refrigerator, 54
photovoltaic, 40, 41	power meter, 72	regenerative braking, 133
physicist, 2	power per unit area, see power density,	rem, 182
physics, 32	see power density	renewable energy
laws of	power per unit length	research and development, 238
conservation of energy, 27	tide, 87, 331	renewable obligation certificate, 70
	wave, 78	renewables
pick-ups, 212		intermittency, 201
pig, 81	power station, 5, 28, 361, 376	reporters, 72
pig-iron, 8	closures, 5	-
pilot, 297	coal, 361	research and development, 238
pipeline, 239	President Dwight D. Eisenhower, 107,	REVA, 134
plan, 172	141	reverse osmosis, 98, 211
plan D, 222	Prestatyn, 68	Rijndam, 140
plan E, 226	printer, 74	river
plan G, 225	Prius, 134, 144	uranium, 173
plan L, 224	projector, 74	roadmap, 218

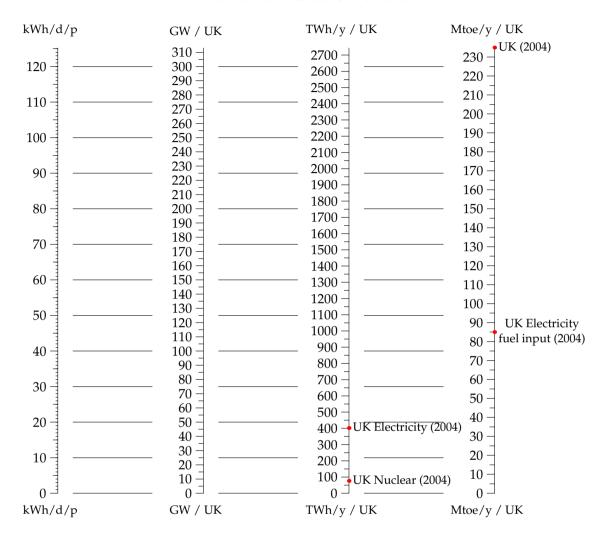
ROC, see renewables obligation	shallow, 64	spelling, 360
certificate, see renewables	shallow offshore wind, 64	spring tide, 85, 89
obligation certificate	shallow water, 328	square, 191
rock, 103	sheep, 82	stack, 23
rolling resistance, 278	Shell, 70, 237	stadium, 325
Rolls Royce, 39	Shell UK, 64	stainless steel, 348
Rosemanowes, 105	Shetland, 288	standby, 73
rotor, 285	ship, 8	STE, 199
Royal Albert Hall, 364	container, 96	steak, 81, 83
rubber, 276, 348	cruise-ship, 93	steam engine, 6, 8
Rubbia, Carlo, 175	energy consumption, 97	steel, 94, 100, 348, 349
rubbish, 93	nuclear-powered, 141	embodied energy, 100
runaway feedbacks, 357	painting, 3	steel production, 66
Russia, 21, 141	shipping, 96, 141	stereo, 73
Ryanair, 38		
Kyarian, 56	Shockley–Queisser limit, 51	Stern review, 240, 248
Cabara 101	shop, 93	Stiglitz, Joseph, 240
Sahara, 191	shower, 54	stockpile stewardship, 241
Saint-Malo, 91	SI, 360	stop-gap, 103
salad nicoise, 80	Siberia, 357	stop-sign, 273
salt	Siegenthaler, U., 20	storage
energy storage, 190	sievert, 181	kinetic energy, 213
Salter, Stephen, 143	simplification, 16	molten salt, 190
duck, 327	Sinclair C5, 70, 135	stove, 54
San Francisco, 128	slateworks, 60	Strangford Lough, 91
Sandia Labs, 105	sleep, 73	straw, 103, 348
Saudi Arabia, 6, 190, 240	slew rate, 203	streamlined, 273
Saudi oil, 8	slime, 48	streetlight, 63
sausage, 290, 292	Smart Car, 144	stuff, 72, 93
Sauven, John, 19	Smith, James, 64	submarine, 240
Savannah, 141	smoking, 239	subsidy, 239
Scaled Composites, 297	Smola, 67	Sudan, 190
sceptic, 6, 9	Snowdonia, 206, 207	sugarcane, 53
Schwarzenegger, Arnold, 137	social costs, 24	sun, 103
Scotland, 68, 88, 207, 213	softwood, 306, 348	sunniness, 40, 48
rainfall, 60	solar	sunroof, 140
screen, 73	concentrating, 42	sunshine, 40
Scroby Sands, 288	farm, 43, 223	superjumbo, 140
sea	photovoltaics, 41	sustainable
fully-developed, 329	power station, 190	definition, 167
sea depths, 65	solar heating, 41	sustainable coal, 167
sea snake, 327	solar hot water, 220	Sustainable Development Commission,
sea water, 186	solar panels, 41	2
uranium extraction, 173, 186	solar power, 40	sustainable energy
sea-level rise, 10, 17	concentrating	environmental costs, 24
sea-water, 170	parabolic trough, 190	social costs, 24
SeaBus, 128	in vehicles, 140	SUV
seawater, 98, 183, 187	solar thermal electricity, 199	electric, 145
second, 360	solar warrior, 42	Sv, 181
security of energy supply, 5, 117	Solarpark, 43, 51, 232	sweater wearing, 220
wind, 202	sorghum, 53	swimming pool, 381
SELCHP, 232	Southampton Geothermal District	swirling air, 273
separative work unit, 108	Heating Scheme, 105, 106	switchgrass, 53, 303
servant, 25	space shuttle, 240	SWU, 108, 184
set-top box, 72	spaceship, 31, 273	, ,
Severn barrage, 91	Spain, 190	t-km, 126
sexy personalities, 220	speed, 325	tap, 26
Shadowfax, 82	speed-boat, 138	tax, 236, 239
DIMAGNIUM, OL	speed body 100	un, 200, 200

taxman, 3	tonne, see ton, see ton	cost, 173
tea, 54	Toyota Prius, 144	depleted, 172
Team Crocodile, 127	Toyota RAV4 EV, 144	extraction from sea water, 186
teaspoon, 73	toys, 72	from sea water, 173, 186
technology, 123	traffic	reserves, 2, 171
telephone, 72	congestion, 132, 236	URL, see web pointer, see web pointer
television, 72	pollution, 239	US military, 109
temperature, 54	traffic lights, 63	USA, 105
temperature demand, 310	train, 126–128	crops, 53
tenant, 249	tram, 147	1 /
tepid, 28	electric, 147	Vader, Darth, 72
tera, 365	transformer, 73	Valentia, 332
terrorism, 4	translation, 30	value-added tax, 252
Tesco, 237	transmission, 224	Vectrix, 146
Tesla, 135	transmission lines, 226	vegan, 81
Tesla Roadster, 135	transport, 218	vegetarian, 4, 81
TEU, 96, 381	efficiency, 83	vegetarianism, 82
Texas, 197, 202, 216	bicycle, 127, 142, 277	vehicle
Thames Estuary, 68, 88	car, 32	electric, 134
Thames estuary, 86	eco-car, 127	vehicle to grid, 213
The Skeptical Environmentalist, 2	electric car, 135	Venturi Fetish, 145
thermal	electric scooter, 146	Vestas, 68
solar, 40	plane, 38, 294	vicious cycle, 357
thermal conductivity, 318	train, 127, 142	Virgin, 297
thermal fly-tipping, 317	efficiency measures, 127	Virgin trains, 236
thermal transmittance, 308	transport efficiency	Virgin traits, 230 Viridian Solar, 41
thermostat, 4, 319	freight, 97	viscosity, 329
	travel	*
Think, 144	average, 32	VLS-PV, see very large scale photovoltaics, see very large
thorium, 175		1 , ,
reserves, 175	emissions, 16 Trident, 240	scale photovoltaics
resources, 175		Volkswagen, 273
thorium oxide, 175	trolleybus, 128	volt, 54
tidal barrage, 221	tropics, 52	volume, 26, 381
tidal larger 221, 226, 242	truth, 72	vortex, 290
tidal lagoon, 221, 226, 343	tsunami, 87, 330	M.1. FO. (0. (4. (0. 02. 20F. 200. 2(4.
tidal power, 86, 89	tube of air, 273	Wales, 59, 60, 64, 68, 82, 205, 288, 364
two basins, 340	tumble dryer, 55	Walkers crisps, 84
tidal stream, 221	turboprop, 37	walking, 83
tidal wave, 87	turn down, 319	wall, 312
Tiddles, 82	turn-off-and-onable, 201	war, 107, 240
tide, 86	TV pick-ups, 212	Iraq, 240
as waves, 330	tyre, 276	on drugs, 240
compared with wind, 90	TI 1 200 212	warhead, 240
explanation, 85	U-value, 308, 312	Wartsila–Sulzer, 281
in oceans, 85	UK, 21	waste
UK resource, 343		
	UK coal, 6–8	food, 237
tide is like wind, 335	UK coal, 6-8 UK territorial waters, 65	food, 237 incineration, 222
tide is like wind, 335 tide speed, 86	UK coal, 6–8 UK territorial waters, 65 uncertainty, 10	food, 237 incineration, 222 waste heat, 152
tide is like wind, 335 tide speed, 86 tidepool, 87	UK coal, 6–8 UK territorial waters, 65 uncertainty, 10 under-floor heating, 159	food, 237 incineration, 222 waste heat, 152 waste incineration, 30, 45, 221, 227
tide is like wind, 335 tide speed, 86 tidepool, 87 timber, 348	UK coal, 6–8 UK territorial waters, 65 uncertainty, 10 under-floor heating, 159 understanding, 16	food, 237 incineration, 222 waste heat, 152 waste incineration, 30, 45, 221, 227 efficiency, 229
tide is like wind, 335 tide speed, 86 tidepool, 87 timber, 348 Tina, 249	UK coal, 6–8 UK territorial waters, 65 uncertainty, 10 under-floor heating, 159 understanding, 16 underwater windmill, 87	food, 237 incineration, 222 waste heat, 152 waste incineration, 30, 45, 221, 227 efficiency, 229 waste to energy, 221
tide is like wind, 335 tide speed, 86 tidepool, 87 timber, 348 Tina, 249 tinyURL, iii	UK coal, 6–8 UK territorial waters, 65 uncertainty, 10 under-floor heating, 159 understanding, 16 underwater windmill, 87 United Kingdom, 17	food, 237 incineration, 222 waste heat, 152 waste incineration, 30, 45, 221, 227 efficiency, 229 waste to energy, 221 efficiency, 229
tide is like wind, 335 tide speed, 86 tidepool, 87 timber, 348 Tina, 249 tinyURL, iii Titanic, 72, 73	UK coal, 6–8 UK territorial waters, 65 uncertainty, 10 under-floor heating, 159 understanding, 16 underwater windmill, 87 United Kingdom, 17 units, 25, 360	food, 237 incineration, 222 waste heat, 152 waste incineration, 30, 45, 221, 227 efficiency, 229 waste to energy, 221 efficiency, 229 water, 26, 54, 98
tide is like wind, 335 tide speed, 86 tidepool, 87 timber, 348 Tina, 249 tinyURL, iii Titanic, 72, 73 toaster, 54	UK coal, 6–8 UK territorial waters, 65 uncertainty, 10 under-floor heating, 159 understanding, 16 underwater windmill, 87 United Kingdom, 17 units, 25, 360 translation, 30	food, 237 incineration, 222 waste heat, 152 waste incineration, 30, 45, 221, 227 efficiency, 229 waste to energy, 221 efficiency, 229 water, 26, 54, 98 cost of, 99
tide is like wind, 335 tide speed, 86 tidepool, 87 timber, 348 Tina, 249 tinyURL, iii Titanic, 72, 73 toaster, 54 tobacco, 239	UK coal, 6–8 UK territorial waters, 65 uncertainty, 10 under-floor heating, 159 understanding, 16 underwater windmill, 87 United Kingdom, 17 units, 25, 360 translation, 30 unplug, 256	food, 237 incineration, 222 waste heat, 152 waste incineration, 30, 45, 221, 227 efficiency, 229 waste to energy, 221 efficiency, 229 water, 26, 54, 98 cost of, 99 embodied energy, 101
tide is like wind, 335 tide speed, 86 tidepool, 87 timber, 348 Tina, 249 tinyURL, iii Titanic, 72, 73 toaster, 54	UK coal, 6–8 UK territorial waters, 65 uncertainty, 10 under-floor heating, 159 understanding, 16 underwater windmill, 87 United Kingdom, 17 units, 25, 360 translation, 30	food, 237 incineration, 222 waste heat, 152 waste incineration, 30, 45, 221, 227 efficiency, 229 waste to energy, 221 efficiency, 229 water, 26, 54, 98 cost of, 99

shallow, 328	Wellington, 283, 284	Windermere, 207
water depths, 65	Wembley, 364	windmill, 285
water power, 59	White, David J., 64	underwater, 87
water vapour, 77	white-tailed eagles, 67	window, 312
watercraft, 299	Whitelee wind-farm, 35	Windsave WS1000, 70
waterwheel, 60	Whitstable, 64	windspeed, 285
watt, 72, 360	Whorf, T. P., 20	Ĉairngorm, 34
Watt, James, 6, 8, 360	willow, 220	Cambridge, 34, 36
wave, 77, 325, 326	wind, 34, 225, 325	data, 285
deep-water, 325	arguments against, 202	wing, 290
Mexican, 325	compared with tide, 90	winter
shallow-water, 331	data, 34, 36, 202, 285, 287	heat pumps, 161
source of, 77	deep offshore, 65, 70	wood, 95, 101, 306
tides as waves, 330	intermittency, 202	world, 17, 112, 113, 190, 240
wave speed, 86	Irish, 203	world coal, 6–8
wave-farm, 78	micro-wind, 67, 70	world coal production, 7
Wavegen, 79	offshore, 64	
wavelength, 325	cost, 70	Xebra, 145
waves	jack-up barges, 67, 223, 232	
production by boats, 97	London Array, 70	Yamal, 141
we should have a plan that adds up, 172	power density, 64	yield, 45
weapons, 240	origin of, 77	you can have only one row, 335
web pointer, iii	wind farm, 233	
Weetabix, 44	wind turbine, 36	Ze-0, 145
Weier, Sven, 76	wind-farm, 34	zinc, 349



Power translation chart

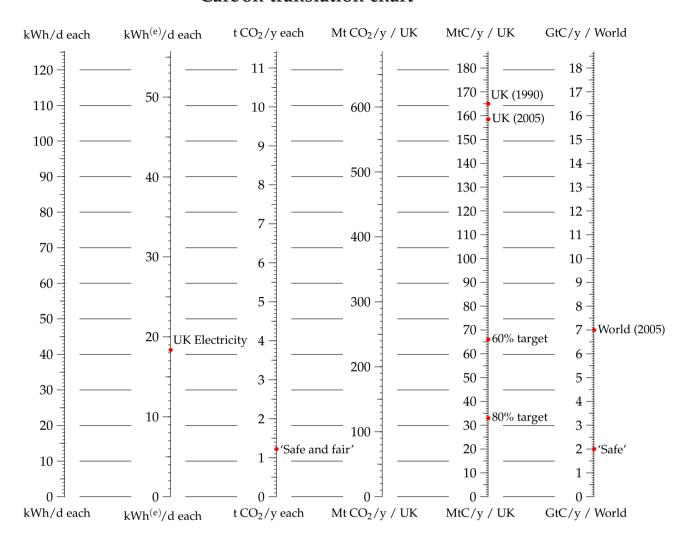


1 kWh/d the same as 1/24 kW 'UK' = 60 million people

GW often used for 'capacity' (peak output)

TWh/y often used for average output USA: 300 kWh/d per person 1 Mtoe 'one million tons of oil equivalent' Europe: 125 kWh/d per person

Carbon translation chart



kWh thermal energy exchange rate: $1 \text{ kWh} \leftrightarrow 250 \text{ g of CO}_2$ (oil, petrol) = 60 million people 'UK' (for gas, $1 \text{ kWh} \leftrightarrow 200 \text{ g}$) 'World' = 6 billion people kWh^(e) electrical energy is more costly: UK: 160 Mt C per year (2005) $1 \text{ kWh}^{(e)} \leftrightarrow 445 \text{ g of CO}_2 \text{ (gas)}$ USA: $20 \text{ t CO}_2/\text{y}$ each (1.5 GtC/y total)(Coal costs twice as much CO₂) World: 7 Gt C per year (2005) To avoid 2C global warming, need < 2 GtC/ytCO₂ ton of CO₂ Mt C million tons of Carbon

⁽c) David J.C. MacKay. Draft 2.9.0. August 28, 2008 www.withouthotair.com